

On direct proton decay of the Gamow-Teller giant resonance

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Abstract. The semi-microscopic approach to the description of giant resonances in medium-heavy mass closed-shell nuclei is implemented to treat partial probabilities of direct-proton decay of the Gamow-Teller giant resonance (GTGR) in ^{208}Bi . The corresponding experimental data are reasonably explained.

1 Introduction

Partial probabilities of direct nucleon decay of giant resonances (GRs) carry information about the particle-hole (p-h) structure and damping mechanisms of GRs. Therefore, these probabilities should be related to the main properties of GRs and included in their full description. As applied to medium-heavy mass closed-shell nuclei, this aim can be achieved within the semi-microscopic approach to the description of giant resonances (SMAGR). The present formulation of this approach has been initially given in [1] and then extended to a number of implementations (see the reviews [2,3]). The SMAGR is a generalization of the standard and non-standard versions of the continuum-Random-Phase-Approximation (cRPA) developed to take into account a spreading effect. The latter is described phenomenologically in terms of the energy-dependent imaginary part of an effective optical-model potential directly used in cRPA equations [2,3].

Being the spin-flip partner of the isobaric analog resonance (IAR), the GTGR corresponds to the 1^+ collective proton-(neutron-hole)-type nuclear excitations. In spite of a lot of experimental studies of the GTGR (predominantly via the direct (p,n)- and ($^3\text{He,t}$)-reactions), the proton decay of the GTGR in ^{208}Bi has only been studied by the coincident $^{208}\text{Pb}(^3\text{He,tp})$ experiments [4]. The same method has later been used for studying proton decay of the GTGR overtone, isovector giant spin-monopole resonance (IVGSMR⁽⁻⁾) in ^{208}Bi [5]. The unique experiment on excitation of the GTGR in ^{118}Sb with the resonance $^{117}\text{Sn}(p,n_{tot})$ -reaction [6] should be also mentioned. Along with the anomalously small total width (≈ 1 MeV), the partial (elastic) proton width of the mentioned GTGR has been measured as well.

Using the modern version of the SMAGR [1–3], in the present work we revise the previous calculations of the partial direct-proton-decay probabilities performed in [7] for the GTGR in ^{208}Bi . The new elements of our analysis are: (i) taking the spreading effect on the escaped-proton wave function into account; (ii) the use of the energy-averaged decay-channel strength function (instead of the Breit-Wigner parametrization of the proper cRPA strength function); (iii) the use of the proton optical-model penetrability (instead of the penetrability calculated for a

schematic single-particle potential). The method and results briefly described in Sect. 2 will be published soon together with the study of the GT strength distribution in a wide excitation energy interval [8].

2 Direct-proton-decay probabilities for the GTGR in ^{208}Bi

As applied to description of charge-exchange excitations, the cRPA radial equations for the basic quantities are given in [7]. Extension of these equations on taking the spreading effect into account is described in [2,3] in a rather schematic form. As applied to the semi-microscopic description of 0^+ charge-exchange excitations (including IAR), the radial equations for the energy-averaged basic quantities are explicitly given in [9]. These quantities are: the effective field $\tilde{V}^{(-)}(x, \omega)$ and strength function $S^{(-)}(\omega)$, corresponding to an external single-particle field $V^{(-)} = V(r)\tau^{(-)}$ (ω is the excitation energy counted off the ground-state energy of the parent (even-even) nucleus); the proton-escape amplitude $M_{\nu}^{(-)}(\omega)$ and partial proton-decay-channel strength function $S_{\nu}^{(-)}(\omega) = |M_{\nu}^{(-)}(\omega)|^2$ ($\nu = n_r, (\nu)$ is the full set of the quantum numbers of a neutron-hole state, populated after direct proton decay, $(\nu) = j_{\nu}, l_{\nu}$). In the semi-microscopic description of the 1^+ charge-exchange excitations we suggest to use, for short, the equations of Ref. [9] after the following substitutions:

$$\tau^{(-)} \rightarrow \sigma_M \tau^{(-)}, \quad V(r) \rightarrow 1, \quad F' \rightarrow G'. \quad (1)$$

$$\sum_{(\pi)} n_{\nu} (2j_{\nu} + 1) \delta_{(\pi)(\nu)} \rightarrow \frac{1}{3} \sum_{(\pi)} n_{\nu} \langle (\pi) || \sigma || (\nu) \rangle^2. \quad (2)$$

In Eq. (1) σ_M are the spherical Pauli matrices; $F' = Cf'$, $G' = Cg'$ ($C = 300 \text{ MeV fm}^3$) are the intensities of the isovector part of the Ladau–Migdal particle-hole interaction: $F(x_1, x_2) \rightarrow (F' + G' \sigma_1 \sigma_2) \tau_1 \tau_2 \delta(\mathbf{r}_1 - \mathbf{r}_2)$. In Eq. (2) $(\pi) = j_{\pi}, l_{\pi}$ are the single-proton quantum numbers linked to (ν) via the corresponding selection rules; n_{ν} are the neutron occupation numbers. The partial proton-decay-channel strength functions for the GTGR are properly

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modified: $S_v^{(-)}(\omega) = \sum_{(\pi)} S_{(\pi),v}^{(-)}(\omega)$. These strength functions determine the corresponding partial direct-proton-decay branching ratios as follows:

$$b_v^{(-)}(\delta) = \frac{\int S_v^{(-)}(\omega) d\omega}{\int S^{(-)}(\omega) d\omega}, \quad (3)$$

where integration is performed over the resonance. It is noteworthy that almost the same equations determine within SMAGR the partial branching ratios for direct proton decay of the IVGSMR⁽⁻⁾. The difference is in the choice of the radial dependence of the external field $V(r) \rightarrow R^2 - \eta$, where the scaling parameter η is chosen from the condition of “non-exciting” the GTGR [3, 10].

A mean field and particle-hole interaction together with the imaginary part $W(r, \omega)$ of the effective optical-model potential are the input quantities for calculations within the SMAGR the giant-resonance strength function. The partial direct-nucleon-decay branching ratios are then calculated without the use of additional model parameters. In our calculations a phenomenological mean field and Landau–Migdal interaction are used. The mean-field parameters (together with the parameter f') are found, as described in [11] but with the use of another mean-field geometrical parameter $r_0 = 1.21$ fm. In calculations of the strength function of the GTGR in ²⁰⁸Pb we used two adjustable parameters: the intensity g' of the Landau–Migdal interaction to reproduce in calculations the observed GTGR energy; the intensity of $W(r, \omega)$ to reproduce in calculations the total width of the considered GTGR. The calculated strength function $S^{(-)}(\omega)$ is shown in figure 1.

Before comparing the calculated partial direct-proton-decay branching ratios $b_v^{(-)}$ of Eq. (3) with the corresponding experimental values, we recalculate the partial proton-decay-channel strength functions $S_{(\pi),v}^{(-)}$ to take into account two points: (i) the difference of the experimental neutron-hole state excitation energies \mathcal{E}_v^{exp} of the product nucleus ²⁰⁷Pb from the calculated energies $\mathcal{E}_v = \mathcal{E}_v^{calc} - \mathcal{E}_{p1/2}^{calc}$ (\mathcal{E}_v^{calc} are determined by the mean field); (ii) the difference of the experimental spectroscopic factors S_v for the mentioned one-hole states from unity. (Both of these differences are shown in Table 1). In view of the discussed points we recalculate the partial proton-decay-channel strength functions to the following effective values:

$$\check{S}_{(\pi),v}^{(-)}(\omega) = S_v S_{(\pi),v}^{(-)}(\omega) T_{(\pi)}(\mathcal{E}^{exp}) / T_{(\pi)}(\mathcal{E}^{calc}). \quad (4)$$

Here, $\mathcal{E} = \mathcal{E}_v + \omega$ is the escaped-proton energy; $T_{(\pi)}(\mathcal{E})$ is the optical-model penetrability (the seizure coefficient) for the partial proton wave. Because of changing over the GTGR the potential-barrier penetrability for escaped protons, the energy dependence of the calculated decay-channel strength functions $\check{S}_v^{(-)}(\omega)$ is noticeably different from that of the giant-resonance strength function $S^{(-)}(\omega)$ (figure 1). The proton branching ratios \check{b}_v , calculated for the GTGR in ²⁰⁸Bi in accordance with Eqs. (3), (4) for the energy interval $\omega = 12$ –26 MeV are found in a reasonable agreement with the corresponding experimental data (Table 1).

In conclusion of this Section we note, that the similar description of the partial (and total) direct-proton-decay

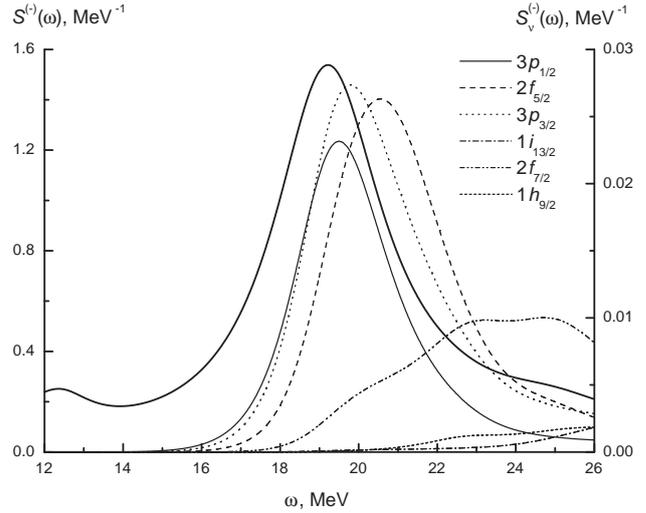


Fig. 1. The giant-resonance strength function (thick line) and partial proton-decay-channel strength functions calculated for the GTGR in ²⁰⁸Bi.

Table 1. The calculated partial direct-proton-decay branching ratios for the GTGR in ²⁰⁸Bi in a comparison with the experimental data. Some characteristics of the decay channels are also given.

ν^{-1}	S_ν [11]	\mathcal{E}_ν^{calc} , keV*	\mathcal{E}_ν^{exp} , keV** [4]	$\check{b}_\nu(\delta)$, %	b_ν^{exp} , % [4]
$3p_{1/2}$	1.0	0	0	1.0	1.8 (5)
$2f_{5/2}$	0.98	895	570	1.3	2.7 (6)
$3p_{3/2}$	1.0	1078	898	1.4	0.2 (2)
$1i_{13/2}$	0.91	2011	1633	0.05	0.4 (2)
$2f_{7/2}$	0.5	3614	2340	0.7	
$1h_{9/2}$	0.61	4373	3413	0.1	
\sum_ν				4.55	4.9 (1.3)

$$*\mathcal{E}_\nu^{calc} = \mathcal{E}_{3p_{1/2}}^{calc} - \mathcal{E}_\nu^{calc}, \mathcal{E}_{3p_{1/2}}^{calc} = -7.55328 \text{ MeV.}$$

$$**\mathcal{E}_\nu^{exp} = -\mathcal{E}_\nu^{exp} - B_N^{exp}(\text{208Pb}),$$

$$B_N^{exp} = 7.36787 (5) \text{ MeV (Nuclear Data Sheets).}$$

branching ratios for the IVGSMR⁽⁻⁾ in ²⁰⁸Bi leads to different results [3, 10]. The total branching ratios (about 50%) is in reasonable agreement with the experimental data of [5], while the calculated and experimental distributions of the partial branching ratios over decay channels are noticeably different: population of deep neutron-hole states in ²⁰⁷Pb has been unexpectedly observed in [5]. Up to now there is no explanation of this observation.

3 Conclusive remarks

Within the semi-microscopic approach to description of giant resonances in closed-shell nuclei the reasonable description of the experimental data on direct proton decay of the Gamow-Teller giant resonance in ²⁰⁸Bi is obtained. Extension of experimental studies of direct proton decay of the GTGR and its overtone for other nuclei seems to be necessary together with generalization of the semi-microscopic approach on description of giant-resonance damping for open-shell nuclei.

Acknowledgement

This work is partially supported by the Russian Foundation for Basic Research under grant no. 12-02-01303-a.

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