

## FP-LMTO investigation of the structural, electronic and magnetic properties of Heusler compounds Ru<sub>2</sub>CrZ (Ge, Sn, Si)

Z. Aarizou, S. Bahlouli and M. Elchikh

Laboratoire de Physique des Matériaux et des Fluides, Département de Physique, Université des Sciences et de la Technologie d'Oran-MB, BP 1505 Oran El Mnaouer, Algeria

**Abstract.** The electronic structure of the antiferromagnetic full Heusler alloys Ru<sub>2</sub>CrZ (Ge, Sn, Si) have been studied by first principal calculations using Full-Potential linearized Muffin Tin Orbital (FP-LMTO) method based on the generalized Gradient Approximation (GGA). It was shown that obtained equilibrium lattice parameters agree well with available experimental data. The influence of Z-elements on the electronic structure and magnetic properties of these compounds is analysed.

### 1 introduction

During the last two decades, full-Heusler alloys have been investigated both theoretically and experimentally in a series of papers; see for instance the paper by C. Felser et al. [1]. They are suitable materials for spintronic applications since they can show 100 % spin-polarized carriers at the Fermi level. In fact, Half-Metallic Heusler Ferromagnets (HMF) have an energy-band gap for minority spin bands and the conduction electrons at the Fermi level ( $E_F$ ) show 100 % spin polarization and can be used as spin-polarized electron sources along with metal oxides and IIIV group semiconductors.

Full Heusler compounds are ternary intermetallics with general formula X<sub>2</sub>YZ, where X and Y denote the transition metals and Z may be any one of the large number of s-p elements belonging to the IIIB-VB group, element such as Al, Ga, Si, Ge, Sn, Sb, etc. These materials crystallize in L21 structure, which consists of four FCC sublattices with space group Fm $\bar{3}$ m, with the following Wyckoff positions: X (1/4, 1/4, 1/4) and (3/4, 3/4, 3/4), Y (0, 0, 0) and Z (1/2, 1/2, 1/2).

Some of the full Heusler alloys show other interesting properties like semiconducting or semimetallic and ferrimagnetic or antiferromagnetic behaviors. For instance, crystals of the type Ru<sub>2</sub>MnZ, where Z stands for Si, Ge and Sn have been found to be antiferromagnets with Neel temperatures near room temperature [2]. Recently, Okada et al. succeeded in synthesizing Ru<sub>2</sub>CrGe and Ru<sub>2</sub>CrSn, and found that Ru<sub>2</sub>CrGe is an antiferromagnet with Néel temperature  $T_N = 13$  K and Ru<sub>2</sub>CrSn shows a spin-glass-like behavior below  $T_g = 7$  K [3]. Furthermore, the phase transition to ferromagnetic state of full-Heusler alloys Ru<sub>2-x</sub>Fe<sub>x</sub>Si and Ru<sub>2-x</sub>Fe<sub>x</sub>Ge have

been studied [4–6] where Fe are partially or totally substituted for Ru.

In this note, we recall the first-principle calculations method we used, then we show and discuss the results obtained on the structural optimization, the electronic properties and magnetic behavior of Ru<sub>2</sub>CrSi, Ru<sub>2</sub>CrGe and Ru<sub>2</sub>CrSn. Finally we give a brief summary.

### 2 Computational details

As first-principle method we applied the FP-LMTO method [7, 8] as embedded in LmtART MStudio Mind-Lab 7 code developed by S.Y Savrasov [8,9]. We assumed the functional of exchange and correlation (GGA) as proposed by Perdew Wang (PW) [10]. We took the different muffin tin radius RMT as listed in Table 1:

**Table 1.** RMT(a.u.) of Ru, Cr and Z atoms for Ru<sub>2</sub>CrZ compounds.

Margin	Ru <sub>2</sub> CrSi	Ru <sub>2</sub> CrGe	Ru <sub>2</sub> CrSn
Ru	2.477	2.509	2.535
Cr	2.38	2.413	2.535
Z	2.38	2.413	2.535

The basis set of our FP-LMTO calculations, are made of the 4d<sup>7</sup>5s<sup>1</sup> and 3d<sup>5</sup>4s<sup>1</sup> states for the transition elements Ru and Cr respectively. The valence states for the Z atoms are 3s<sup>2</sup>3p<sup>2</sup> of Si, 4s<sup>2</sup>4p<sup>2</sup> of Ge or 5s<sup>2</sup>5p<sup>2</sup> of Sn. The filled

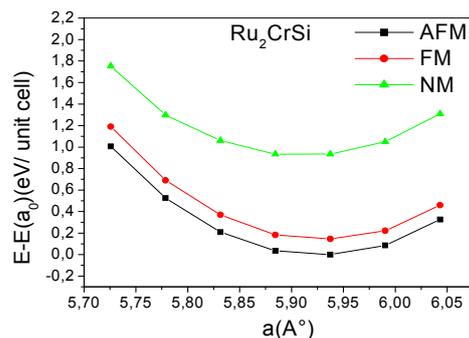
states  $4d^{10}$  of Sn and  $3d^{10}$  of Ge may also be considered as valence states, that are the default input in the code since the energy needed to separate semi-core and valence electrons was set to above  $-2Ry$  from the vacuum zero, which results in treating of Si, Ge and Sn semi-core electrons as valence electrons. The charge density and potential are expanded in spherical harmonics inside the spheres up to  $l_{max} = 6$  and Fourier transformed in the interstitial region. The maximum value of angular momentum  $l_{max} = 6$  is also taken for wave function expansion inside the atomic spheres. The lattice constants used in the present study, were obtained by minimizing the total energy  $E_{tot}$  with respect to the experimental lattice parameters. The energy convergence criterion was set to  $10^{-6}$  Ry. For k-space integration over the Brillion zone, we found that our calculations converge for a  $10 \times 10 \times 10$  tetrahedron mesh [11]. The energy cut-off and the number of plane waves used in our calculations are, respectively: (80.70 Ry; 9204) for  $Ru_2CrGe$ , (75.40Ry; 9204) for  $Ru_2CrSn$  and (84.09Ry; 9204) for  $Ru_2rSi$ . In our study the magnetic unit cell being twice that of the unit cell used in crystallography (defined above) if the AFM phase is considered. For this AFM phase, we adopt the so called FCC-AFM type II order. The magnetic moments on the atoms are ferromagnetically coupled on the (111) planes and antiferromagnetically coupled in adjacent planes. In fact, this arrangement (AFM type II) has been revealed experimentally for  $Ru_2CrGe$  [6].

### 3. Results and descussion

#### 3.1 Structural optimisation

We performed structural optimizations on our three Heusler compounds of interest,  $Ru_2CrSi$ ,  $Ru_2CrGe$  and  $Ru_2CrSn$ , for the Nonmagnetic (NM), ferromagnetic (FM) and AFM phases. For the three Heusler compounds, the results of structural optimization are quite similar, so only the  $Ru_2CrSi$  structural optimization is shown in Fig. 1. The total energy differences  $\Delta E = E_{AFM} - E_{FM}$  are negative, thus all our compounds  $Ru_2CrZ$  are stable in the AFM phase which confirm the experimental results. We also computed the total energies for several lattice constants and fitted them with the empirical Murnaghan equation of state [12] the values of the optimized lattice constants for the three compounds are listed in Table 2. Our calculated lattice constants for  $Ru_2CrGe$  and  $Ru_2CrSn$  are in agreement with the experimental values, and to the best of our knowledge, no experimental data have been reported for  $Ru_2CrSi$ .

One can note that the theoretical lattice constant in  $Ru_2CrZ$  ( $Z=Si, Ge$  and  $Sn$ ) increases with the increasing atomic number of  $Si \rightarrow Ge \rightarrow Sn$  due to the increasing size of atomic radius while the absolute value of the energy differences  $\Delta E$  decreases.



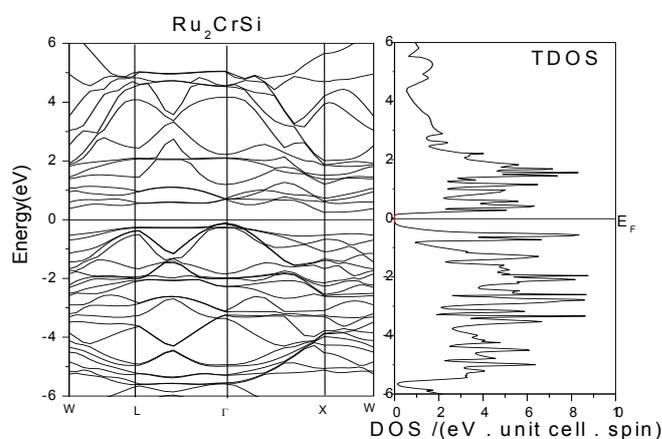
**Fig. 1.** Relative total energy (per unit cell) as a function of the lattice parameter for  $Ru_2CrSi$ ,  $E(a_0)$  being the ground state energy.

**Table 2.** Equilibrium lattice constants  $a_0$ ( $\text{\AA}$ ) and total energy differences  $\Delta E$ (eV/unit cell) for  $Ru_2CrSi$ ,  $Ru_2CrGe$  and  $Ru_2CrSn$ .

Compound	Calculation	$a_0$	$\Delta E$
$Ru_2CrSi$	Our work	5.93	-0.1414
	Experimental		
	Other [4]	5.94	
$Ru_2CrGe$	Our work	6.05	-0.110
	Experimental [3,6]	5.97	
	Other [4]	6.02	
$Ru_2crSn$	Our work	6.26	-0.0984
	Experimental [3]	6.19	
	Other [13]	6.233	

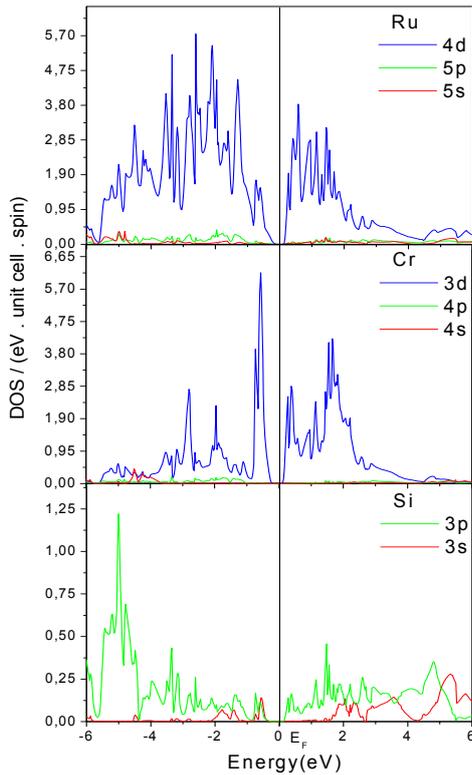
#### 3.2. Electronic and magnetic properties

The calculated band structures and the density of states of the AFM state of  $Ru_2CrSi$ ,  $Ru_2CrGe$  and  $Ru_2CrSn$ , being quite similar, so only the  $Ru_2CrSi$  electronic structure will be presented here. Furethermore, our three compounds are all antiferromagnets, then the electronic properties of the two spin-channels are similar, consequently we reported only one spinchannel in Fig. 2.



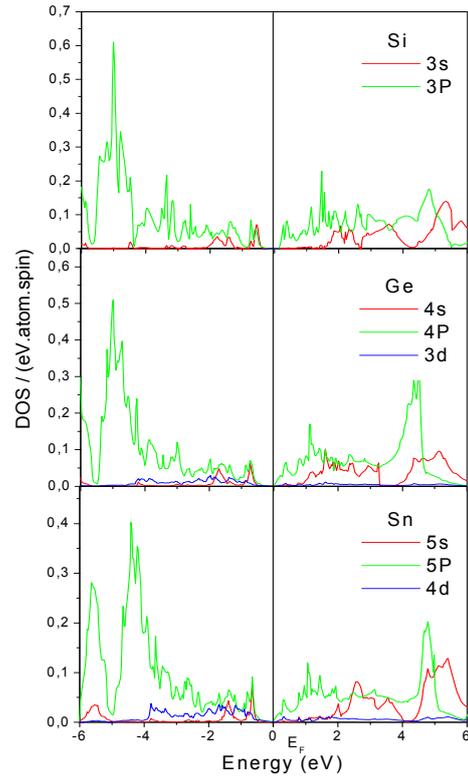
**Fig. 2.** Electronic structure of  $Ru_2CrSi$ : band structure (left side) and total density of states (right side).

The three Heusler compounds  $\text{Ru}_2\text{CrZ}$  present an indirect energy gap along  $\Gamma - X$ , i.e. in the  $(\Delta)$  direction and the Fermi energy of these materials is just at the top of the valence band. We calculated the energy gaps (in eV) and found 0.35 for  $\text{Ru}_2\text{CrSi}$ , 0.14 for  $\text{Ru}_2\text{CrGe}$  and 0.02 for  $\text{Ru}_2\text{CrSn}$ . We note that our Heusler Z-atoms have an influence on the energy gap, therefore, the gap decreases as the number of valence Z increases. The partial density of states (PDOS) of  $\text{Ru}_2\text{CrSi}$  as a function of energy is shown in Fig. 3, the PDOS of  $\text{Ru}_2\text{CrSi}$  and  $\text{Ru}_2\text{CrSn}$  being also almost the same. The high DOS around  $E_F$  is associated with hybridization of Ru(4d) and Cr(3d) electrons. We notice that the Cr compound exhibits a considerably larger gap compared with the Ru compound. In order to understand the influence of Z element on the gap width we plotted the PDOS of Z elements in Fig 4. The energy of (p) electrons is strongly dependent on the Z atom in  $\text{Ru}_2\text{CrZ}$ , so the hybridization between (p) electrons with different energy and the (d) electrons affects the formation of the energy gap. We can see



**Fig. 3.** Partial density of states of  $\text{Ru}_2\text{CrSi}$ .

that the local magnetic moments of Cr become large with increasing the atomic number of the Z atoms but also the lattice constant has an influence on the magnetic properties, on the other hand the Ru atom carries negligible local moment as it was deduced from experiment [6]. However, the individual magnetic moment of Cr atoms found in our study, is about fifty



**Fig. 4.** Compared Partial density of states of Z elements.

percent greater than the value of  $1.45 \mu_B$ , estimated experimentally in the case of  $\text{Ru}_2\text{CrGe}$  at 5 K [6], which indicates that itinerant exchange mechanism alone cannot explain this difference.

**Table 3.** The calculated absolute local magnetic moment ( $\mu_B$ ) of Cr and Ru atoms in  $\text{Ru}_2\text{CrZ}$  compounds.

	$ M_{Cr} $	$ M_{Ru} $
<b><math>\text{Ru}_2\text{CrSi}</math></b>	2.477	2.509
<b><math>\text{Ru}_2\text{CrGe}</math></b>	2.38	2.413
<b><math>\text{Ru}_2\text{CrSn}</math></b>	2.38	2.413

It is interesting to note that when Ru is replaced by other elements like Co [14,15] or Mn [16], Heusler alloys exhibit half metallic ferromagnetic behavior. The conduction band minimum consists mostly of Ru(4d), Cr(3d) and smaller contribution of Z(p) orbitals; the valence band maximum is composed of Cr(3d), Ru(4d) and Z(p) electrons. Moreover, Z atoms create four fully occupied bands, comprising of one Z(s) and three Z(p) bands. This Z(s) is very low in energy and also well separated from other bands, on the other hand, Z(p) bands hybridize with p electron Ru and Cr, but they (Z(p) bands) are also low energy bands. The d- states of the transition metal atoms (Ru and Cr) extend from occupied

and unoccupied states and hybridize with each other. The widely spread d states are mainly due to the strong hybridization of the (3d) metals.

Let us note that the half metallic ferromagnetic behavior can be present in  $\text{Ru}_{2-x}\text{Fe}_x\text{CrSi}$  for a particular range of Fe concentration  $x$  starting at  $x = 0.5$  [4,5].

## 4 Summary

We have performed first principles calculations on structural, electronic and magnetic properties of  $\text{Ru}_2\text{CrSi}$ ,  $\text{Ru}_2\text{CrGe}$  and  $\text{Ru}_2\text{CrSn}$  using the Full-Potential Linear Muffin Tin Orbitals, these compounds are all Antiferromagnets, which is in agreement with the experimental results. The electronic properties show that these compounds have a semiconductor behavior with indirect gap along  $\Gamma - X$ . We found that the Z elements have an influence on the electronic properties as well as on the magnetic properties. Therefore the energy gap decreases as the number of valence Z increases also the theoretical values of the Cr local moments become larger with increasing of the Z atomic number. The high density of states around  $E_F$  is associated with hybridization of Cr(3d) and Ru(4d) electrons. Here we did not deal with the spin-glass behavior of  $\text{Ru}_2\text{CrSn}$  below  $T_g = 7\text{K}$ [3], which cannot be simply explained by our method of calculations.

## References

1. T. Graf, C. Felser and S. S.P. Parkin, Progress in Solid State Chemistry **39**, (2011) 1.
2. M. Gotoh, M. Phashi, T. Kanomata, and Y. Yamaguchi, Physica B **306**, (1995) 213.
3. H.Okada et al., App. Phys.Lett. **92**, (2008) 062502.  
H.Okada et al., Journal of Physics: Conference Series **150**, (2009) 042153.
4. S. Mizutani, S. Ishida, S. Fujii, S. Asano, Mater. Trans. **47**, (2006) 25.  
S. Ishida, S. Mizutani, S. Fujii, S. Asano, Mater. Trans. **47**, (2006) 31.
5. M. Hiroi et al., Phys. Rev. B **79**, (2009) 224423.  
M. Hiroi et al., Journal of Physics: Conference Series **150**, (2009) 042058.
6. P.J Brown et al., J. Phys.: Condens.Matter **20**, (2008) 455201.
7. S.Y. Savrasov and D. Savrasov, Phys.Rev. B **46**, (1992) 12181.
8. S.Y. Savrasov, Phys. Rev. B **54**, (1996) 16470.
9. <http://physics.ucdavis.edu/mindlab>
10. J. P. Perdew, S. Burke and M. Ernzerhof, Phys. Rev. Lett. **77**, (1996) 3865.
11. P.E. Blchl, O. Jepsen, O.K. Andersen, Phys. Rev. B **49**, (1994) 16223.
12. F.D Murnaghan, Proc. Nat. Acad. Sci. of U.S.A **30** (1944) 244.  
F. Birch, Phys. Rev. **71** (1947) 809.
13. M. Gillessen, R. Dronskowski, Journal Of Computational Chemistry, **30**, (2009) 1290.
14. H.C Kandpal, G. H Fecher and C. Felser; J. Phys. D: Appl. Phys **40** (2007) 1507.
15. Z. Aarizou, A. Akriche, S. Bahlouli and M. Elchikh, (Unplished work).
16. H. Luo et al, J. Magn. Magn. Mater. **320** (2008) 421.