

Interlaminar Deformation in Thermoplastic Composite Laminates: Experimental-Numerical Correlation

Min SHEN^{1,a}, Jingwei TONG¹, Shibin WANG¹, and Yihong Fang¹

¹ Department of Mechanics, Tianjin University, Tianjin 300072, PR China

Abstract. The interlaminar deformation behaviors of thermoplastic AS4/PEEK composite laminates subjected to static tensile loading are investigated by means of microscopic moiré interferometry with high spatial resolution. The fully three-dimensional orthotropic elastic-plastic analysis of interlaminar deformation for the thermoplastic laminates is developed in this paper, and used to simulate the stress-strain curves of tensile experiment for its angle-ply laminates. Under uniaxial tensile loading, the 3D orthotropic elastic-plastic FE analysis and microscopic moiré interferometry of interlaminar deformations are carried out for the $[\pm 25]_{S4}$ laminates. The quantitative local-field experimental results of interlaminar shear strain and displacements at free-edge surface of the laminate are compared with corresponding numerical results of the orthotropic elastic-plastic FE model. It is indicated that the numerical tensile stress-strain curves of angle-ply laminates computed with 3D orthotropic elastic-plastic model are agree with experimental results. The numerical interlaminar displacement U and shear strain γ_{xz} are also consistent with the experimental results obtained by moiré interferometry. It is expected the elastic-plastic interlaminar stresses and deformations analysis for the optimal design and application of AS4/PEEK laminates and its structures.

1 INTRODUCTION

AS4/PEEK laminates is a high-performance thermoplastic composite material which is now widely used in the aerospace industry [1]. Due to the ductility of matrix in AS4/PEEK laminates increase, the mechanical behaviours of full laminates have evidently plasticity.

The subject of free edge delamination of composite laminated plates, as one of the most frequently encountered types of failure in composite materials, has attracted considerable attention. A difficulty arises in quantifying the three-dimensional state of stress near a free-edge of the laminate. Since the original paper of Pipes and Pagano [2], numerous papers have been published on the subject over the years. They have included the finite difference solution of Pipes and Pagano, approximate analytical solution [3], finite element solution [4-6], and several experimental investigations [7-13]. A complete review can be found in Ref. [14]. The most of these researches including analyses and experiments are carried for thermoset composite laminates in linear elastic range. There are a few researches of the nonlinear behaviours and damage [15-20] for the

^a e-mail : minshen@tju.edu.cn

AS4/PEEK laminates. However, in contrast to the free edge problem of thermoset composite laminates, the understanding of the corresponding behaviour in thermoplastic AS4/PEEK composite laminates is virtually nonexistent. It is expected the elastic-plastic interlaminar stresses and deformation analysis for the optimal design and application of AS4/PEEK laminates and its structures.

In present work the interlaminar deformation of thermoplastic composite AS4/PEEK laminates subjected to static tensile loading are investigated by means of microscopic moiré interferometry and three-dimensional orthotropic elastic-plastic finite element (FE) method. The orthotropic linear hardening material model is selected to describe the elastic-plastic behaviour of anisotropy in its unidirectional AS4/PEEK laminate. The elastic-plastic finite element model of AS4/PEEK angle-ply laminates is developed. The interlaminar deformations and tensile behaviour of the laminates are simulated.

The intent of this paper is to present accurate experimental results for the interlaminar displacement and strain at free edge for the AS4/PEEK angle-ply laminates, and to compare the experimental results with above FE numerical results obtained using the three-dimensional orthotropic elastic-plastic model. Interlaminar deformations, such as shear strain and displacements, are emphasized because the moiré interferometry technique, which is used for the experimental measurements, provides displacements directly. The gradients of these displacements are the shear strains that can be compared with the strains obtained from the FE numerical solution. The comparisons between numerical and experimental results can verify the three-dimensional orthotropic elastic-plastic FE model of thermoplastic AS4/PEEK laminates. A second goal of this investigation is to gain a better understanding of the influence of PEEK matrix ductility on interlaminar elastic-plastic deformation in AS4/PEEK thermoplastic composite laminates.

2 MATERIALS AND ITS ANISOTROPIC PLASTIC NUMERICAL MODEL

2.1 Material system

The material system, AS4/PEEK, used in this study consisted of AS4 graphite fibers in PEEK matrix. It was supplied by Fiberite Corporation in the form of 16-ply $[\pm 25]_{s4}$ stacking sequences laminates. The fibres content was 61.0 percent by volume. The main mechanical properties determined on unidirectional laminates by standard static tests are reported in Table 1.

Table 1. The mechanical properties of unidirectional AS4/PEEK

E_1 (GPa)	$E_2=E_3$ (GPa)	$\nu_{12}=\nu_{13}$	ν_{23}	$G_{12}=G_{13}$ (GPa)	G_{23} (GPa)	X (MPa)	Y (MPa)	S (MPa)
134	10	0.3	0.47	5.6	3.38	2200	88	68

2.2 3D orthotropic elastic-plastic finite element models

Assuming that the AS4/PEEK lamina is a homogenous, orthotropic and elastic-plastic continuum. The elastic-plastic behaviour of anisotropy in its unidirectional laminate is described using the orthotropic linear hardening.

The constitutive of anisotropic plasticity of AS4/PEEK uses Hill's yield criterion, which accounts for differences in yield strength in orthogonal directions, as modified by Shih and Lee [21], accounting for differences in yield strength in tension and compression. An associated flow rule is assumed and work hardening as presented by Valliappan et al. is used to update the yield criterion [22]. Based on the mechanical-properties of AS4/PEEK tested by Martin etc. [16], the orthotropic

parameters of linear hardening of AS4/PEEK were determined by means of analysis of its orthotropic property in present work.

2.3 Finite element model of as4/peek laminates

Consider the rectangular, symmetric angle-ply laminate shown in Fig. 1. It has sixteen plies, each of thickness h , and is loaded with a uniform axial strain ϵ_0 in the x -direction.

For $[\pm 25]_{s4}$ angle-ply laminate, it has a symmetry with respect to the x - y plane at $z=0$. Therefore, the analysis has been executed only for the upper half of the laminate. Thus it has eight plies. The length and width of the laminate are $2a$ and $2b$, respectively, with $a= b= 1.75$ mm, where the ply thickness $h= 0.1275$ mm, as shown in Fig.1. In such a case, the displacement boundary conditions are

$$\begin{aligned} u(0, y, z) &= 0, \\ u(2a, y, z) &= 2a\epsilon_0, \\ v(a, 0, 0) &= 0, \\ w(x, y, 0) &= 0. \end{aligned} \quad (\text{B.C. 1})$$

The isoparametric eight-node block element is employed to calculate the model. There are 20 elements in the x -direction that is equally divided 24 elements in the y -direction and they are gradually refined to the edge in the y - and z -directions. There are 9920 elements and 11613 nodes in all.

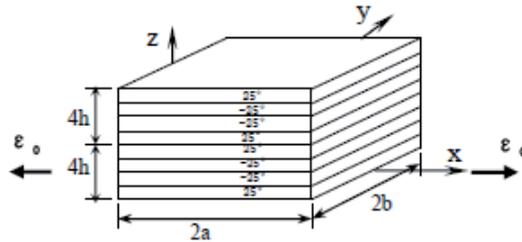


Fig. 1 Finite element model for the upper half of the $[\pm 25]_{s4}$ laminated rectangular plate subjected to a uniform axial strain ϵ_0

3 EXPERIMENTAL PROCEDURES

The specimens are laminates of AS4/PEEK with approximately 134-mm long, 3.0-mm wide and 2.04-mm thick. The tensile loads were from low to high, generating axial strains typically ranging about 1.10 percent for these laminates. Specimen heads were reinforced by aluminum tabs 1.0 mm thick bonded by epoxy resin depicted in Fig.2. The axial tensile strain ϵ_0 is measured by the strain gage that adhered to the face of the specimen.

A high frequency reflection crossed-line grating of 1208 lines/mm was applied to the edge surface of the specimen by a replication process. Its sensitivity is in the subwavelength range, viz. $0.417 \mu\text{m}$ per fringe order, using a reference grating of 2416 lines/mm. Microscopic moiré interferometry developed in this work is an optical system that combines a four-beam moiré interferometry with a long distance microscope (LDM) as shown in Fig.3. It effectively enhances the spatial resolution of the usual moiré interferometry and can be able to measure real-time the micromechanical behaviour of the small deformation field on the free edge of a loaded laminate.

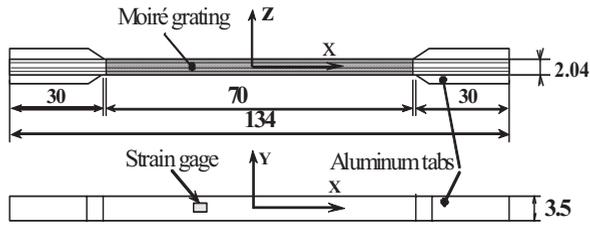


Fig. 2 AS4/PEEK laminate specimen geometry (mm)

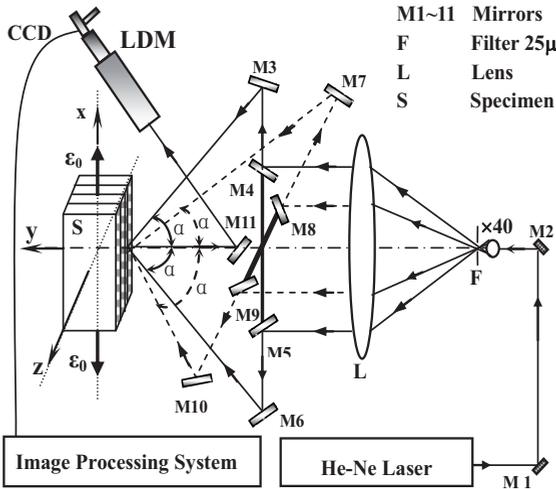


Fig. 3 Optical paths and arrangement for LDM four-beam moiré interferometry

4 RESULTS AND DISCUSSION

4.1 3D orthotropic elastic-plastic FE-simulation of AS4/PEEK tensile curves and its experimental verification

The one-parameter orthotropic plasticity model was introduced by Sun and Chen (1989) [23], to describe the nonlinear behavior of orthotropic fiber-reinforced composite materials. Based on the assumption that plastic deformation in the fiber direction is negligible, the plastic potential function for an orthotropic layer under plane-stress conditions reduces to the form

$$2f = \sigma_2^2 + 2a_{66}\tau_{12}^2 \quad (2)$$

where 1 is the fiber direction and 2 is the transverse direction. The single plastic parameter a_{66} is the material constant found from off-axis tension.

Fig. 4 shows the predictions of the stress/strain response of representative AS4/PEEK angle-ply specimens obtained from both the present 3D orthotropic elastic-plastic FE model and the one-parameter orthotropic plasticity FE model by Meili and Priolo [24]. Comparing with experimental

dates, the predictions of the present model are shown to agree fairly well the experimental results over a wide range of loading levels for various AS4/PEEK angle-ply laminates.

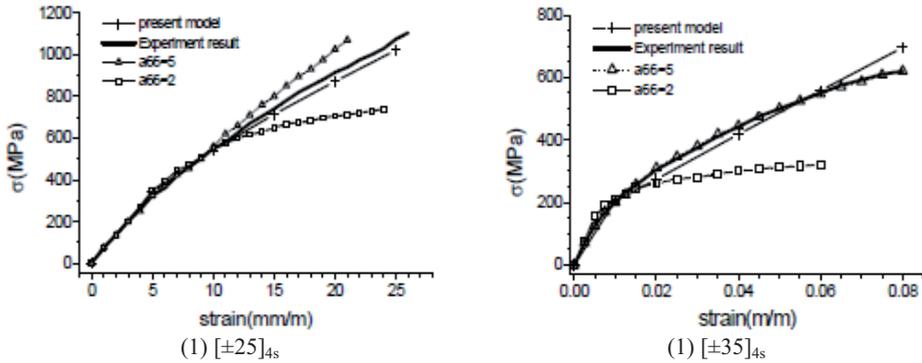


Fig. 4 Comparison of numerical predictions of present orthotropic elasto-plastic FE model and one-parameter model by Meili and Priolo with experimental dates for tension tests

4.2 3D orthotropic elastic-plastic interlaminar deformations and their experimental verification

Fig. 5(1) shows the moiré fringe patterns of interlaminar displacement U field for AS4/PEEK $[\pm 25]_{s4}$ laminate under axial tensile loading. The distributions of U and shear strain obtained from the FE model are given in Figs. 5(2) and (3).

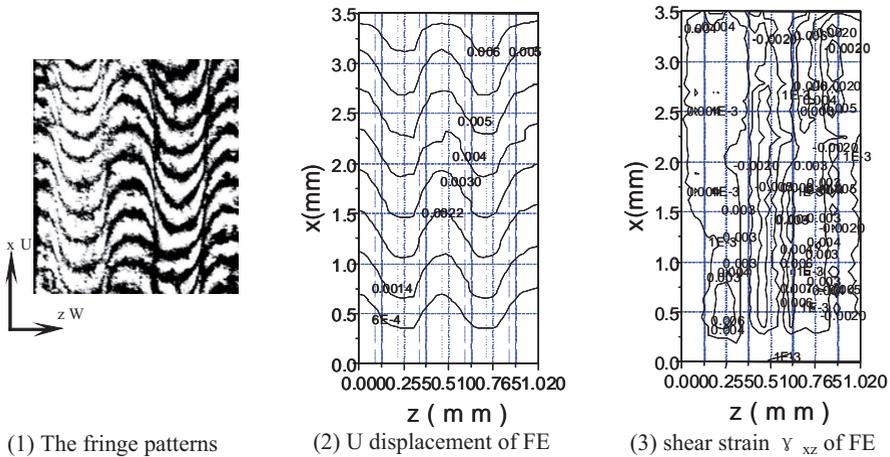


Fig. 5 The interlaminar deformation at the free edge of the $[\pm 25]_{s4}$ laminated rectangular plate subjected to a uniform axial strain ϵ_0 (1) The moiré fringe patterns of U field, (2) U displacement and (3) shear strain γ_{xz} distribution obtained from the FE model.

Fig.6(1) shows the moiré fringe patterns of interlaminar displacement U field for $[\pm 25]_{s4}$ laminate under axial tensile loading. Experimental and numerical distributions of interlaminar displacement u and shear strain γ_{xz} on free edge of $[\pm 25]_{s4}$ laminate are given in Fig.6(2) and (3) while axial tensile loading P is 882N. It is found that interlaminar shear strain γ_{xz} is very large, and achieves its maximal values near four interfaces between ± 25 plies. The numerical interlaminar displacement u

and shear strain γ_{xz} are also consistent with the experimental results obtained by moiré interferometry, especially shear strain concentrations near the interfaces between ± 25 plies at the edge of the laminate. Comparison of the FE numerical and experimental results indicates that the 3D orthotropic elastic-plastic FE analysis for interlaminar deformations of AS4/PEEK composite is reliable and validity, and can fairly reflect influence of ductility of PEEK matrix on the elastic-plastic behaviour of whole AS4/PEEK laminate.

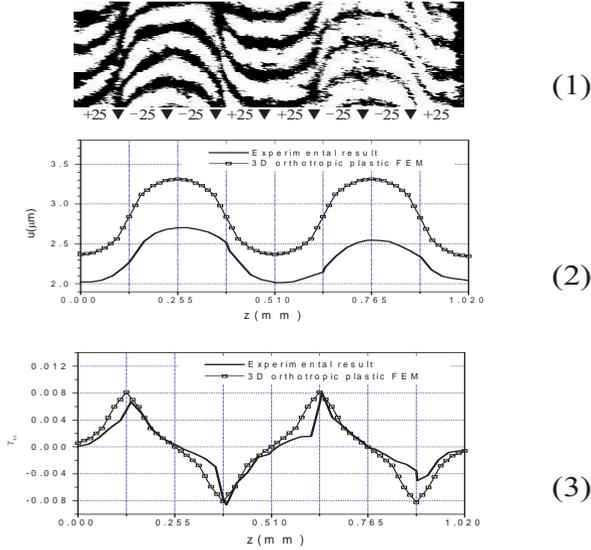


Fig. 6 Interlaminar deformations of $[\pm 25]_{s4}$ laminate loaded at 882N

- (1) U Fringe Patterns, ▼ Actual Ply Boundaries
- (2) experimental vs numerical interlaminar displacement u
- (3) experimental vs numerical interlaminar shear strain γ_{xz}

5 CONCLUSIONS

1. The interlaminar deformation behaviors of thermoplastic AS4/PEEK composite laminates subjected to static tensile loading are investigated by means of microscopic moiré interferometry with high spatial resolution.
2. Based on the mechanical-properties of AS4/PEEK tested by Martin etc., the orthotropic parameters of linear hardening of its laminar were determined by means of analysis of its orthotropic property in this work. Using Shih's theory of anisotropic plasticity its elastic-plastic behavior of anisotropy was described in this paper.
3. A three-dimensional orthotropic elastic-plastic finite element model of AS4/PEEK laminates is developed, and used to simulated the stress-strain curves of tensile experiment for the angle-ply laminates. The numerical tensile stress-strain curves of the laminates computed with 3D orthotropic elastic-plastic model are agreed with experimental results.
4. Under uniaxial tensile loading, the 3D orthotropic elastic-plastic FE analysis of interlaminar deformations are carried out for $[\pm 25]_{s4}$ laminate.
5. It is obvious that comparing between numerical and experimental results, the nonlinear stress-strain behavior of AS4/PEEK laminates can be predicted using the orthotropic elastic-plastic FE model. This comparison also indicates that the 3D orthotropic elastic-plastic FE analysis for interlaminar deformations of AS4/PEEK composite is reliable, and can fairly reflect influence of ductility of PEEK matrix on the elastic-plastic behavior of

whole AS4/PEEK laminate.

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