Composite Higgs under LHC Experimental Scrutiny

J.R. Espinosa\textsuperscript{1,a}, C. Grojean\textsuperscript{2,b}, and M. Mühleitner\textsuperscript{2,c}

\textsuperscript{1} ICREA at IFAE, Universitat Autònoma de Barcelona, 08193 Bellaterra, Barcelona, Spain
\textsuperscript{2} CERN, Physics Department, Theory Unit, CH–1211 Geneva 23, Switzerland
\textsuperscript{3} Institute for Theoretical Physics, Karlsruhe Institute of Technology, D-76128 Karlsruhe, Germany

Abstract. The LHC has been built to understand the dynamics at the origin of the breaking of the electroweak symmetry. Weakly coupled models with a fundamental Higgs boson have focused most of the attention of the experimental searches. We will discuss here how to reinterpret these searches in the context of strongly coupled models where the Higgs boson emerges as a composite particle. In particular, we use LHC data to constrain the compositeness scale. We also briefly review the prospects to observe other bosonic and fermionic resonances of the strong sector.

1 The need for a UV completion of the electroweak Goldstone bosons

One important charge of the LHC, if not the main one, is to understand the dynamics responsible for the breaking of the electroweak (EW) symmetry. A massive spin-one particle corresponds to three physical polarizations: two transverse ones plus an extra longitudinal one which is known to decouple in the massless limit. Precision EW measurements have established the Brout–Englert–Higgs mechanism and the longitudinal $W^\pm$ and $Z$ certainly correspond to the eaten Nambu–Goldstone bosons associated to the breaking of the global chiral symmetry SU(2)$_L \times$ SU(2)$_R$ to its diagonal subgroup. The gauge field masses are conveniently rewritten as the kinetic terms for these Goldstones ($a^\mu$, $a = 1, 2, 3$, are the usual Pauli matrices and $v = 1/\sqrt{2}G_F \approx 246$ GeV):

$$\mathcal{L}_{\text{mass}} = \frac{v^2}{4} \text{Tr} \left( D_\mu \Sigma \right) \Sigma^\dagger D^\mu \Sigma \quad \text{with} \quad \Sigma = e^{ib^\mu a^\mu/v},$$

which indeed exactly reproduces the standard mass Lagrangian in the unitary gauge ($\Sigma = 1$). However, this is a description that is not self-consistent at very high energy since it leads to scattering amplitudes growing with the energy as it follows from the Goldstone equivalence theorem by expanding the Lagrangian (1) ($V$ denotes $W^\pm$ or $Z$):

$$\mathcal{A}(V_L V_L \rightarrow V_L V_L') = \mathcal{A}(s) d^{\alpha \beta} d^{\gamma \delta} + \mathcal{A}(t) d^{\alpha \delta} d^{\beta \gamma} + \mathcal{A}(u) d^{\alpha \gamma} d^{\beta \delta}$$

$$\quad \text{with} \quad \mathcal{A}(s) \approx \frac{s}{v^2}.$$  

In the absence of any new weakly coupled elementary degrees of freedom canceling this growth, perturbative unitarity will be lost around $4\pi v^2 \approx 3$ TeV (or $2\sqrt{2} \pi v \approx 1.2$ TeV, depending on the exact criterion used to define strong coupling) and new strong dynamics will kick in and soften the UV behavior of the amplitude, for instance via the exchange of massive bound states similar to the $\rho$ meson of QCD.

2 Effective Lagrangian for a composite Higgs

The simplest example of new dynamics that can restore perturbative unitarity consists of a single (canonically normalized) scalar field, $h$, coupled to the longitudinal $V$’s and to the SM fermions as [1–4]:

$$\mathcal{L}_{\text{ew}} = \frac{v^2}{4} \text{Tr} \left( D_\mu \Sigma \right) \Sigma^\dagger D^\mu \Sigma + \left( 1 + 2a + v^2 ight) + b^2 h_3^2 + \left( 1 + c + d \right) h_3^3 + \ldots$$

$$\quad - \frac{v}{\sqrt{2}} \left( i \delta^\mu_\lambda d_i \right) \Sigma \left( 1 + c + d + e \right) h_3^3 + \ldots$$

$$\quad + \left( 1 + c + d + e \right) h_3^3 + \ldots$$

The scalar self-interactions can be parametrized as

$$V(h) = \frac{1}{2} m_h^2 \delta^2 + d_3 \left( \frac{m_h^2}{2v} \right) h_3^3 + d_4 \left( \frac{m_h^2}{8v^2} \right) h_3^4 + \ldots$$

For $a = 1$, the scalar exchange cancels the growing piece (3) of the $V_L V_L$ amplitude at high energy. Furthermore for $b = a^2$, the inelastic $V_L V_L \rightarrow hh$ amplitude also remains finite at high energy, while, for $ac = 1$ the $V_L V_L \rightarrow f \bar{f}$ amplitude does not grow either. The point $a = b = c = 1$ (and also $d_1 = d_2 = 1, c_2 = b_3 = 0$, see Table 1) defines the SM Higgs boson and the scalar resonance then combines with the EW Goldstones to form a doublet transforming linearly under SU(2)$_L \times$ SU(2)$_R$. When $a \neq 1$, the Higgs boson alone fails to fully unitarize the $V_L V_L$ scattering amplitude but the breakdown of perturbative unitarity is pushed to a higher scale of the order of $4\pi v / \sqrt{1-a^2}$. The residual growth of the scattering amplitude $\mathcal{A}(s) \approx (1-a^2)s/v^2$ is ultimately cancelled via the exchange of other degrees of freedom, for instance some vector resonances, which however do not have to be light and could escape any detection at the LHC [5].

\textsuperscript{a} e-mail: espinosa@ifae.es
\textsuperscript{b} e-mail: christophe.grojean@cern.ch
\textsuperscript{c} e-mail: maggie@particle.uni-karlsruhe.de

This is an Open Access article distributed under the terms of the Creative Commons Attribution License 2.0, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Article available at http://www.epj-conferences.org or http://dx.doi.org/10.1051/epjconf/20122808004
Away from the SM point, this set-up (4)–(5) introduces minimal deviations in the physics of the Higgs boson: all the Higgs couplings have the same Lorentz structure as in the SM and they are only rescaled by appropriate factors of \( a, b \) and \( c \) (note that \( c \) is flavor-universal and the only source of flavor violation are the usual SM Yukawa couplings, \( y^d, y^e \)); this minimal flavor violation structure actually emerges naturally in the dynamical models that will be considered below:

\[
g_{hVV} = a g_{hVV}^S, \quad g_{hAVV} = b g_{hAVV}^S, \quad \text{and} \quad g_{hf \phi} = c g_{hf \phi}^S. \tag{6}
\]

In addition, there are also new couplings, for instance \( b_3 \) between three Higgses and two gauge bosons or \( c_2 \) between two Higgses and two fermions, that will contribute to multi-Higgs production [1–4].

Since the NLO QCD corrections do not affect the Higgs couplings, at the LHC the relevant Higgs production cross-sections simply rescale as [6]:

\[
\frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}} = c^2, \quad a^2, \quad a^2, \quad c^2 \tag{7}
\]

The loop-induced gluon fusion production could in principle be sensitive to new colored degrees of freedom, e.g. new quarks, running in the loop. But it was shown [7] that in explicit Little Higgs models as well as in Composite Higgs models, a delicate cancelation holds and the cross-section is independent of the masses and couplings of these new quarks.

Similarly, the decay widths also have a simple rescaling:

\[
\Gamma(H \rightarrow f \bar{f}) = c^2 \Gamma^M(H \rightarrow f \bar{f}), \tag{8}
\]

\[
\Gamma(H \rightarrow VV) = a^2 \Gamma^M(H \rightarrow VV), \tag{9}
\]

\[
\Gamma(H \rightarrow gg) = c^2 \Gamma^M(H \rightarrow gg), \tag{10}
\]

\[
\Gamma(H \rightarrow \gamma\gamma) = \left(\frac{a + c\alpha_s}{a + a\alpha_s}\right)^2 \Gamma^M(H \rightarrow \gamma\gamma), \tag{11}
\]

where

\[
I_f = \frac{4}{3} F_{1/2}(4 m_f^2 / m^2_h), \quad J_f = F_{1/2}(4 m_f^2 / m^2_h), \quad F_{1/2}(x) \equiv 2 \left[ 1 + (1 + x) f(x) \right], \quad F_{1}(x) \equiv 2 + 3x \left[ 1 + (2 - x) f(x) \right], \tag{12}
\]

\[
f(x) = \begin{cases} \arcsin[1/\sqrt{1-x}]^2 & \text{for } x \geq 1 \\ -\frac{1}{2} \left[ \log \frac{1 + \sqrt{1-x}}{1 - \sqrt{1-x}} \right]^2 & \text{for } x < 1 \end{cases}
\]

The scalar \( h \) could correspond to the usual SM Higgs boson mixed for instance with a gauge singlet but it could also be a composite bound state emerging from a strongly interacting sector. When such a composite Higgs boson appears as a fourth Goldstone boson associated to the spontaneous breaking of a global symmetry \( G \) of the strong sector to a subgroup \( H \), there is a natural mass gap between \( f \), the dynamical scale of the strong interactions, i.e. the Goldstone decay constant, and \( v \), the electroweak scale that is generated radiatively. These composite Higgs models appear as a natural generalization of the SM with new Goldstones in addition to the \( W_L \) and \( Z_L \) (see Table 2). Without knowing the details of the physics of the strongly interacting theories giving rise to the composite Higgs and other possible resonances, a general effective chiral Lagrangian can capture the low-energy physics of the composite particles [1]. The strong sector is broadly parametrized by two quantities: the typical mass scale, \( m_f \), of the heavy vector resonances and the dynamical scale, \( f \), associated to the global symmetry pattern \( G/H \). The effective chiral Lagrangian includes only four operators that are genuinely sensitive to the strong interactions and affect qualitatively the physics of the strongly interacting light Higgs (SILH) boson:

\[
\mathcal{L}_{\text{SILH}} = \frac{f}{v^2} \bigg( \partial_\mu \left( H^\dagger H \right) \bigg)^2 + \frac{f^2}{v^4} \left( H^\dagger D_\mu H \right)^2 - \frac{c_f}{f^4} \left( H^\dagger H \right)^3 + \text{h.c.} \quad \tag{13}
\]

Whenever this chiral Lagrangian emerges from a strong sector that is invariant under a custodial symmetry, the coefficient \( c_f \) vanishes. The values of the couplings \( a, b, c \) obtained from this SILH Lagrangian are given in Table 1.

The SILH Lagrangian can be extended in several ways (see Refs. [5, 8]) to include some heavy vector resonances of the strong sector in addition to the Goldstone bosons.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>SILH</th>
<th>MCHM4</th>
<th>MCHM5</th>
</tr>
</thead>
<tbody>
<tr>
<td>( a )</td>
<td>( 1 - c_b \xi / 2 )</td>
<td>( \sqrt{1 - \xi} )</td>
<td>( \sqrt{1 - \xi} )</td>
</tr>
<tr>
<td>( b )</td>
<td>( 1 - 2 c_b \xi )</td>
<td>( 1 - 2 \xi )</td>
<td>( 1 - 2 \xi )</td>
</tr>
<tr>
<td>( c )</td>
<td>( 1 - (c_b / 2 + c_b \xi) )</td>
<td>( \sqrt{1 - \xi} )</td>
<td>( \frac{1 - 2 \xi}{\sqrt{1 - \xi}} )</td>
</tr>
<tr>
<td>( c )</td>
<td>( (c_b / 2 + c_b \xi) )</td>
<td>( -\xi / 2 )</td>
<td>( -2 \xi )</td>
</tr>
<tr>
<td>( d_1 )</td>
<td>( 1 + (c_b - 3 c_b / 2) \xi )</td>
<td>( \sqrt{1 - \xi} )</td>
<td>( \frac{1 - 2 \xi}{\sqrt{1 - \xi}} )</td>
</tr>
<tr>
<td>( d_4 )</td>
<td>( 1 + (6 c_b - 25 c_b / 3) \xi )</td>
<td>( 1 - 7 \xi / 3 )</td>
<td>( 1 - 26 c_b / 3 - \xi / 3 )</td>
</tr>
</tbody>
</table>

## Table 2. Global symmetry breaking patterns and the corresponding Goldstone boson contents of the SM, the minimal composite Higgs model, the next to minimal composite Higgs model, the minimal composite two Higgs doublet model. Note that the SU(3) model does not have a custodial invariance. \( a \) denotes a CP-odd scalar while \( h \) and \( H \) are CP-even scalars.

<table>
<thead>
<tr>
<th>Model</th>
<th>Symmetry Pattern</th>
<th>Goldstones</th>
</tr>
</thead>
<tbody>
<tr>
<td>SM</td>
<td>SO(4)/SO(3)</td>
<td>( W_L, Z_L )</td>
</tr>
<tr>
<td>MCHM</td>
<td>SO(5)/SU(2)×U(1)</td>
<td>( W_L, Z_L, h )</td>
</tr>
<tr>
<td>NMCHM</td>
<td>SO(6)/SO(5)×U(1)</td>
<td>( W_L, Z_L, h, a )</td>
</tr>
<tr>
<td>MCHMH</td>
<td>SO(6)/SO(4)×SO(2)×U(1)</td>
<td>( W_L, Z_L, h, H, H^\ast, a )</td>
</tr>
</tbody>
</table>
3 Explicit 5D composite Higgs models

The SILH Lagrangian should be seen as an expansion in $\xi = (v/f)^2$. It can therefore be used in the vicinity of the SM limit ($\xi \to 0$), whereas the technicolor limit ($\xi \to 1$), when the scale of the strong interaction becomes degenerate with the weak scale, requires a resummation of the full series in $\xi$. Explicit models provide concrete examples of such a resummation. Here we refer to the Holochromatic Higgs models of Refs. [9], which are based on a five-dimensional gauge theory in Anti-de-Sitter (AdS) space-time. Via the AdS/CFT correspondence, these 5D models describe 4D strongly coupled models, the components of the gauge fields along the fifth dimension being interpreted as the Goldstone bosons of the strong sector (see Fig. 1). The minimal models are based on an SO(5)×U(1)$_Y$ symmetry in the bulk, broken to the SM SU(2)$_L$×U(1)$_Y$ gauge group on the UV brane and to SO(4)×U(1) on the IR brane. These models contain exactly four massless $A_5$ degrees of freedom which transform as a doublet of SU(2)$_L$ and whose wave-functions are peaked on the IR. Radiative corrections generate a finite potential for these $A_5$ degrees of freedom, the finiteness results in 5D from the fact that gauge invariance forbids any local term and the potential emerges from non-local effects along the fifth dimension. The 4D interpretation is simply that the Higgs doublet is a composite field and the radiative corrections are screened by the compositeness scale. The exact form of the potential depends on the way the SM fermions are embedded in representations of SO(5): when they belong to spinorial representations (MCHM4), the potential is of the form

$$V(h) = \alpha \cos(h/f) - \beta \sin^2(h/f), \quad (14)$$

which after expanding around the EW vacuum leads to the particular values of $d_3$ and $d_4$ reported in Table 1. When the SM fermions are part of fundamental representations of SO(5) (MCHM5), the Higgs potential takes the form:

$$V(h) = \alpha \sin^2(h/f) - \beta \sin^2(2h/f), \quad (15)$$

leading to different values of $d_3$ and $d_4$.

Both in MCHM4 and in MCHM5, the quadratic terms in the $W$ and $Z$ bosons read:

$$m_W^2(h) = \frac{g_W^2}{2} \sin \frac{h}{f} \quad \text{and} \quad m_Z^2(h) = \frac{g_W^2}{2} \cos \frac{h}{f} \quad \text{with} \quad m_W(h) = \frac{g_W}{2} \sin \frac{h}{f}, \quad (16)$$

and the values of the coefficients $a$ and $b$ reported in Table 1.

In MCHM4, the interactions of the Higgs to the fermions take the form

$$\mathcal{L}_{\text{Yuk}} = -m_f(h)\bar{f}f \quad \text{with} \quad m_f(h) = M \sin(h/f). \quad (18)$$

We then obtain

MCHM4: $c = \sqrt{1-\xi}$ and $c_2 = -\xi/2$. \quad (19)

In MCHM5, the interactions of the Higgs to the fermions is changed to

$$\mathcal{L}_{\text{Yuk}} = -m_f(h)\bar{f}f \quad \text{with} \quad m_f(h) = M \sin(2h/f), \quad (20)$$

and therefore

MCHM5: $c = (1-2\xi)/\sqrt{1-\xi}$ and $c_2 = -2\xi$. \quad (21)

Note that in MHC5, the Higgs boson becomes fermiophobic for $\xi = 0.5$.

4 Direct and indirect constraints on composite Higgs models

4.1 EW precision data constraints

Within the SM, the Higgs boson ensures the proper decoupling of the longitudinal polarization of the massive gauge bosons at high energy. But it is also there to screen the radiative corrections to the propagators of the transverse polarizations which otherwise will be logarithmically divergent. This screening is the result of a cancelation between a gauge-boson loop and a Higgs loop. Clearly this cancelation does not hold any longer when the Higgs couplings are modified, more precisely, when $a$, the linear coupling to gauge fields, is different than its SM value. This translates into a logarithmic contribution to the oblique parameters $S$ and $T$ [10]:

$$\Delta S \approx \frac{1}{8\pi v} \left( \log(m_h/m_Z) - (1-a^2) \log(m_h/A) \right) \quad \Delta T \approx -\frac{3}{8\pi v} \left( \log(m_h/m_Z) - (1-a^2) \log(m_h/A) \right) \quad (22)$$

The usual fit of EW data can then be used to constrain the $(m_h, a)$ plane, see for instance Fig. 2. For a given Higgs mass, the allowed range of values of the parameter $a$ depends on possible additional contributions to $S$ and $T$ from UV physics, like a positive contribution to $S$ from heavy vector resonances and positive or negative contributions from new quarks.
4.2 Direct searches

In explicit models, the Higgs production cross-sections and decay branching-ratios are simple functions of the parameter $\xi$ that measures the amount of compositeness of the Higgs boson. Therefore, the searches for the SM Higgs boson can be trivially rescaled with the parameter $\xi$ once we notice that only the signal rates and not the background ones are changed by the parameter $\xi$, see Fig. 3. Stringent exclusion bounds in the 2D parameter space $(m_h, \xi)$ are obtained when the LHC various channels [11] are combined. Figures 4 and 5 present the results when the various channels are simply added in quadrature. A more proper statistical combination of the individual channels leads to similar results [12].

The Higgs searches at the LHC have a chance to establish a deviation away from the SM. Nonetheless, measuring $a \neq 1$ would not necessarily establish that EW symmetry breaking is triggered by a new strong force since possible weakly coupled deformations of the SM could also lead to Higgs anomalous couplings. The true nature of the strong interactions would be revealed in some particular processes like $V_L V_L \to h h [1]$ or $V_L V_L \to h h [2]$. Other processes like $V_L V_L \to h h h [4]$ could even teach us about some discrete symmetries of the strong interactions.

4.3 Direct searches of other resonances

Of course the direct observation of other states belonging to the strong sector, like vector resonances [5, 8] or some fermionic composite particles [13], would be tantalizing signatures auguring a new era in the history of high-energy physics. Quite generically, the vector resonances have only tiny couplings to the light SM quarks via their mixing to the SM EW gauge bosons and therefore their main decay channels are into a pair of longitudinal $W^\pm_L, Z_L$ or a longitudinal $W^\pm_L, Z_L$ together with a Higgs boson. The current most stringent limit of such vector resonances is coming from the search for $WZ$-resonances at the LHC via DY production after mixing with a $W^*$ boson [16] and constrains their masses to be above around 950 GeV for $\xi = 0.1$ [5, 4]. The 14 TeV run could push this bound up to 1.5 TeV [4]. Even if more model-dependent, the production of fermionic resonances in the top sector is quite promising as the large top mass generically implies the existence of light fermionic resonances, possibly the lightest non-Goldstone particles of the strong sector [13, 17]. These fermionic resonances have an exotic 5/3 electric charge and can be produced in pairs or alone, see Fig. 6, with a cross section large enough to make a discovery plausible even with a limited integrated luminosity [13]. The existence of these light fermionic states could also be inferred indirectly through the modification they induce in Higgs physics. If their effects on $gg \to h$ actually cancel [7], they give sizable contributions to $gg \to hh$ [18].
Fig. 4. Limits from Higgs searches at LEP, Tevatron and LHC in the plane \((m_h, \xi)\) for MCHM4. For the LHC constraints, we have used the data reported at the EPS-HEP 2011 conference [14], the Lepton-Photon 2011 symposium [15] and the ones announced in December 2011 at CERN [11]. The individual channels are appropriately rescaled according to Eqs. (7)–(11) and they are then simply combined in quadrature. The red continuous line delineates the region favoured at 99% CL by EW precision data (with a cutoff scale of 2.5 TeV and after marginalizing over \(\epsilon_2\) and \(\epsilon_b\)), the region below the red dashed line survives for an additional 50% cancellation of the oblique parameters.

Fig. 5. Same as Fig. 4 but for MCHM5.

5 Conclusion

The LHC has been built to understand the dynamics at the origin of the breaking of the electroweak symmetry. The SM Higgs boson, namely a fundamental scalar field with appropriate couplings to the SM particles, is a very compelling UV completion to the Higgs mechanism which ensures the proper decoupling at high energy of the extra polarization associated to the masses of the EW gauge bosons, and at the same time also screens the radiative corrections to the propagators of these \(W\) and \(Z\). The main virtue of this scenario is that it can remain perturbative, hence calculable, up to very high energy, possibly the GUT or the Planck scale. Nonetheless, strong dynamics could also be responsible for the EW breaking. And surprisingly enough, these strong models can be very similar to the SM if a scalar field with the same quantum number as the Higgs boson emerges as composite bound state from the strong sector. Viewed from the low-energy perspective, this new setup will appear as a deformation of the SM itself.

Acknowledgments

CG would like to thank the organizers of the HCP symposium for their invitation to present our results. This work has been partly supported by the European Commission under the contract ERC advanced grant 226371 ‘MassTeV’, the contract PITN-GA-2009-237920 ‘UNILHC’, and the contract MRTN-CT-2006-035863 ‘ForcesUniverse’, as well as by the Spanish Consolider Ingenio 2010 Programme CPAN (CSD2007-00042) and the Spanish Ministry MICNN under contract FPA2010-17747 and FPA2008-01430. MM is supported by the DFG SFB/TR9 ‘Computational Particle Physics’.

References

12. A. Azatov, R. Contino, J. Galloway, in preparation