

# Final results of $\mu\text{p}$ capture rate $\Lambda_S$ and pseudoscalar coupling $g_P$

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**Abstract.** We present the final results of muon capture on proton  $\mu^- + p \rightarrow \nu_\mu + n$ , which were obtained by the MuCap Collaboration at the Paul Scherrer Institute. The singlet  $\mu\text{p}$  capture rate  $\Lambda_S$  is determined as the difference between the lifetimes of  $\mu\text{p}$  and  $\mu^+$ . Our result is  $\Lambda_S^{\text{MuCap}} = 714.9 \pm 5.4_{\text{stat}} \pm 5.1_{\text{syst}} \text{ s}^{-1}$  in excellent agreement with the prediction of chiral perturbation theory  $\Lambda_S^{\text{CHPT}} = 712.7 \pm 4.3 \text{ s}^{-1}$ . The induced pseudoscalar coupling constant results as  $g_P^{\text{MuCap}} = 8.06 \pm 0.48_{\text{exp}} \pm 0.28_{\text{th}}$  whereas  $g_P^{\text{CHPT}} = 8.26 \pm 0.23$ .

## 1 Introduction

The MuCap collaboration has now concluded a big and long lasting effort to determine the induced pseudoscalar coupling constant (electro-weak form factor)  $g_P$ , by a precision measurement of the nuclear muon capture rate  $\Lambda_S$  on proton



in the singlet  $\mu\text{p}$  system [1]. The theoretical interest is given by the fact that  $g_P$  is by far the least known of the electro-weak coupling constants. On the other hand,  $g_P$  has been precisely predicted by chiral perturbation theory [2] as

$$g_P^{\text{CHPT}}(q^2) = (2 m_\mu g_{\pi NN} F_\pi) / (m_\pi^2 - q^2) - 1/3 g_A(0) m_\mu M r_A^2 = 8.26 \pm 0.23. \quad (2)$$

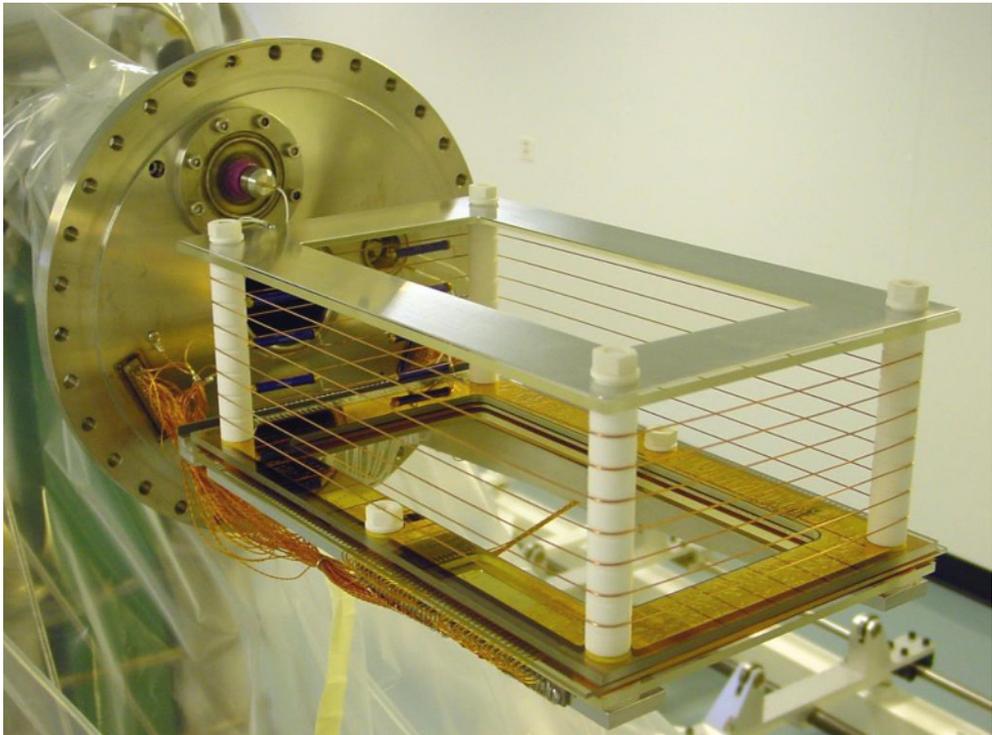
MuCap's aim was a 1% measurement of  $\Lambda_S$  which determines  $g_P^{\text{exp}}$  to a precision of 6%. The measurement of the  $\mu\text{p}$  capture rate is the only enough sensitive method to reach such a precision. Experimentally, we had to overcome a number of big challenges which have nullified several previous efforts to reach the anticipated precision:

- the end products of reaction (1) are  $n$  and  $\nu$ : the neutrino escapes, while as far as the neutrons are concerned, it is technically too difficult to achieve 1% accuracies in direct rate measurements. Therefore, MuCap chose the lifetime method, i.e. a high precision measurement of the  $\mu\text{p}$  lifetime  $\tau_{\mu\text{p}}$  which is compared with the  $\mu^+$  lifetime  $\tau_{\mu^+}$ . The difference of the inverse lifetimes just yields the capture rate
 
$$\Lambda_S = \tau_{\mu\text{p}}^{-1} - \tau_{\mu^+}^{-1}. \quad (3)$$
- meso-molecular physics of muons in hydrogen.  $\mu\text{p}$  atoms in collisions with  $\text{H}_2$  molecules form  $\mu\text{p}\mu$  mesic molecules which exist in ortho and para states, each with very different capture probabilities. There is a transition rate  $\lambda_{\text{op}}$  between these states which is badly known (the ‘‘ortho-para’’ problem [3]). MuCap avoided this problem by using hydrogen gas at low density ( $\sim 1\%$  of liquid  $\text{H}_2$ ) where  $\mu\text{p}\mu$  formation occurs at a sufficiently small probability.

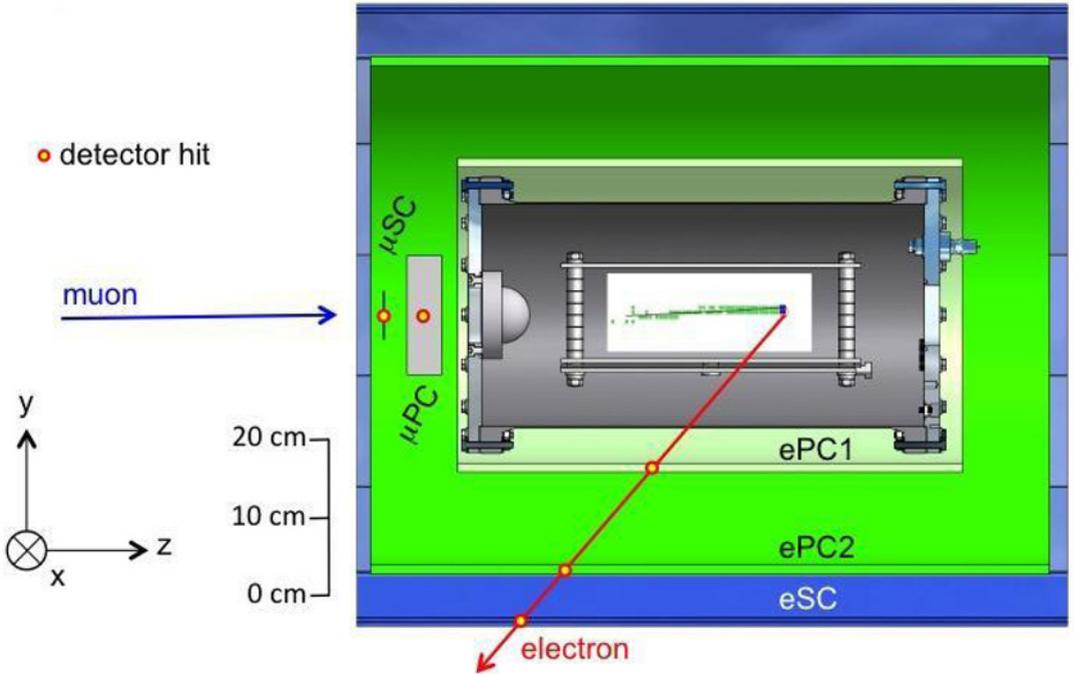
- clean muon stops. Each muon must be verified with  $\sim 99.999\%$  certainty to stop in hydrogen, because stops in surrounding materials with higher  $Z$  distort the lifetime measurement due to much larger capture rates. MuCap developed a time projection chamber (TPC) to record the track of every muon [4].
- highest purity hydrogen gas.  $\mu p$  atoms colliding with nuclei of impurities get quickly transferred and captured with much larger rates, thus distorting the muon decay curve. MuCap developed a special circulation and purification system [5] to keep the gas clean.
- isotopically pure hydrogen (protium). Collisional transfers  $\mu p + d \rightarrow \mu d + p$  lead also to distortions of the lifetime distribution, because  $\mu d$  atoms can diffuse out of the sensitive TPC volume (Ramsauer-Townsend effect). MuCap constructed a special isotope separation column which cleaned the gas to isotopic purities with concentrations  $c_p < 7$  ppb.
- high data rate. To reach the anticipated precision, more than  $10^{10}$  single good muon decay events within a  $\pm 25\mu s$  period had to be collected. This statistics was achieved with the muon kicker from the MuLan experiment [6]. It allowed to kick single muons into the target without pile-up from other  $\mu$ . This method increased the data collection rate by a factor 2 to 3.

## 2 MuCap apparatus

The central part of the MuCap apparatus is the TPC shown in Fig. 1. It was specially developed for this experiment [4] and is made from UHV compatible materials (metals, ceramics) which could be baked up to 130 C and led to extremely low outgasing rates. In addition the protium gas was continuously circulated at 10 bar and purified by a system using thermodynamical cycles [5]. During the main runs we determined impurity levels (mostly water) below 20 ppb.



**Figure 1.** The MuCap Hydrogen TPC acting simultaneously as muon stop detector and active target. Sensitive volume  $30 \times 15 \text{ cm}^2$  with 12 cm vertical drift space. Gas filling 10 bar ultra-purified, deuterium-depleted hydrogen at 300 K. Electrical field 2 kV/cm. Drift time velocity of electrons 5.5 mm/ $\mu s$ . Two-dimensional readout by a MWPC at the bottom. 3D reconstruction of muon tracks by measurement of the drift time.



**Figure 2.** Cross-sectional view of the MuCap apparatus showing a typical muon stop and decay electron. Muon identification by scintillator  $\mu$ SC, wire chamber  $\mu$ PC and the track in the TPC showing the Bragg peak. Electron identification by cylindrical wire chambers ePC1, ePC2 and double scintillator hodoscope eSC.

Fig. 2 shows a cross-section of the full MuCap apparatus with illustration of a typical event. Every muon was tracked individually to its stopping point. The electrons were tracked back to the muon stop location. Thanks to fiducial cuts, background from accidental electrons was suppressed to the  $10^{-4}$  level.

### 3 Final results

During three independent production runs we have collected  $1.2 \cdot 10^{10}$  fully reconstructed  $\mu^-$  decays plus  $0.6 \cdot 10^{10}$   $\mu^+$  decays for systematic controls. The final results of lifetime fits and systematics are summarized in Table 1. The systematic corrections include distortion effects due to impurities,

**Table 1.** Final numbers of  $\mu$ p lifetime fits, correction factors and capture rates

	run-2004 (Ref. [7])	run-2006	run-2007	units
statistics	$1.6 \cdot 10^9$	$5.5 \cdot 10^9$	$5.0 \cdot 10^9$	events after cuts
systematic corrections	$-32.1 \pm 8.4$	$-23.3 \pm 5.2$	$-14.7 \pm 3.9$	$s^{-1}$
$\lambda_\mu = 1 / \tau_\mu$ ( $\mu$ p lifetime)	$455'851.4 \pm 15.1$	$455'857.3 \pm 9.3$	$455'853.1 \pm 9.1$	$s^{-1}$
$\Delta\Lambda_{\mu p}$ correction	$19.8 \pm 1.9$	$17.7 \pm 1.9$	$17.7 \pm 1.9$	$s^{-1}$
$\Lambda_S$ (singlet $\mu$ p capture rate)	$713.4 \pm 15.2$	$717.3 \pm 9.5$	$713.1 \pm 9.4$	$s^{-1}$

removal of  $\mu p$  scatter events,  $\mu p$  and  $\mu d$  diffusion, uncertainties of fiducial volume cuts, inefficiencies and electron track definitions. For more details we refer to Ref. [1].

Averaging these data and using the  $\mu^+$  decay constant measured by the MuLan experiment [6],  $\lambda_{\mu^+} = 455'170.05 \pm 0.46 \text{ s}^{-1}$ , we obtain our final singlet muon capture rate on proton

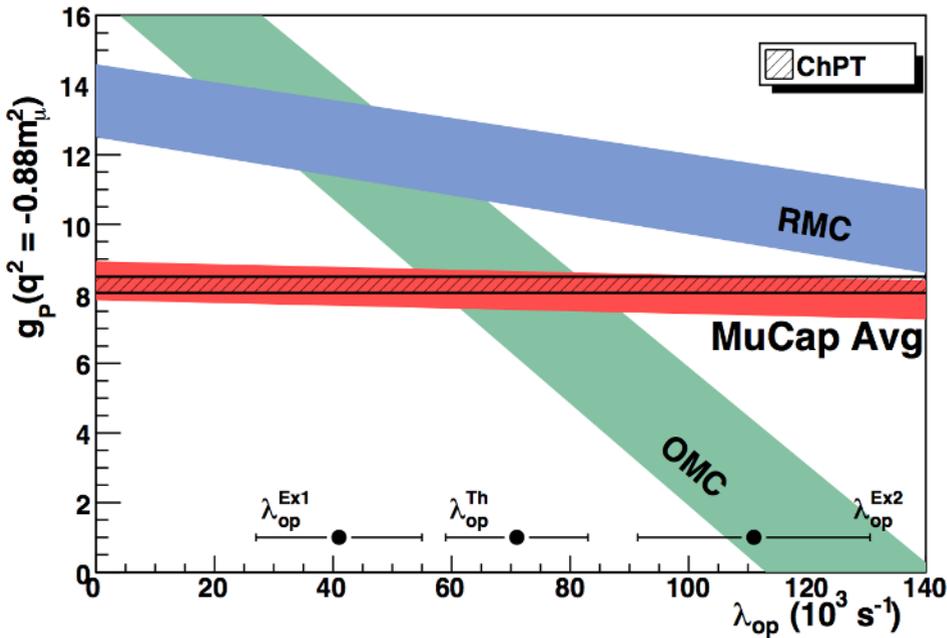
$$\Lambda_S^{\text{MUCAP}} = 714.9 \pm 5.4_{\text{stat}} \pm 5.1_{\text{sys}} \text{ s}^{-1}, \quad (4)$$

which is in excellent agreement with theory  $\Lambda_S^{\text{CHPT}} = 712.7 \pm 4.3 \text{ s}^{-1}$ .

From  $\Lambda_S^{\text{MUCAP}}$  we deduct [1]

$$g_p^{\text{MUCAP}} = 8.06 \pm 0.48_{\text{exp}} \pm 0.28_{\text{th}} \quad (5)$$

also in excellent agreement with chiral perturbation theory  $g_p^{\text{CHPT}} = 8.26 \pm 0.23$ . Fig. 3 shows  $g_p$  values as function of the poorly known transition rate  $\lambda_{op}$  of  $\mu p p$  molecules (ortho-para problem). In contrast to earlier experiments which were carried out using liquid hydrogen, the MuCap experiment is rather insensitive to  $\lambda_{op}$  which solves finally this longstanding problem.



**Figure 3.** Extracted values for  $g_p$  as a function of the poorly known molecular transition rate  $\lambda_{op}$ . OMC = Saclay experiment [8], RMC = TRIUMF experiment [9]. Also shown are results of two inconsistent  $\lambda_{op}$  measurements (Ex1 from Saclay, Ex2 from TRIUMF), and the theoretical calculation  $\lambda_{op}^{\text{Th}}$  by the Ponomarev group [10].

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