Antiproton–to–electron mass ratio determined by two-photon laser spectroscopy of antiprotonic helium atoms

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Abstract. The ASACUSA collaboration of CERN has recently carried out two-photon laser spectroscopy of antiprotonic helium atoms. Three transition frequencies were determined with fractional precisions of 2.3–5 parts in 10^9. By comparing the results with three-body QED calculations, the antiproton-to-electron mass ratio was determined as 1836.1526736(23).

1 Introduction

Antiprotonic helium ($\overline{p}\mathrm{He}^+$) is a three-body atom [1–4] consisting of a helium nucleus, an electron in the 1s state, and an antiproton occupying a Rydberg state with high principal and angular momentum quantum numbers $n \sim \ell + 1 \sim 38$. The transition frequencies of $\overline{p}\mathrm{He}^+$ have been calculated by QED calculations to fractional precisions of 1×10^{-9} [5]. The calculations included relativistic and radiative recoil corrections up to order $m_e c^2 \alpha^6/h$, and nuclear size effects. By comparing the measured and calculated transition frequencies, the antiproton-to-electron mass ratio was determined [4] as 1836.1526736(23).

We have previously measured some $\overline{p}\mathrm{He}^+$ transition frequencies with a fractional precision of $10^{-7} - 10^{-8}$, by single-photon laser spectroscopy [6–9]. The precision was limited by the Doppler broadening of the resonance lines which arose from the thermal motions of the $\overline{p}\mathrm{He}^+$. Recently [4], two-photon transitions of the type $(n, \ell) = (n - 2, \ell - 2)$ [Fig. 1(a)] were excited using two counterpropagating laser beams, such that the Doppler broadening was partially canceled [10].

2 Experiment and results

The two-photon transitions were induced between $\overline{p}\mathrm{He}^+$ states with microsecond and nanosecond-scale lifetimes against Auger emission of the electron. After Auger decay, the remaining two-body
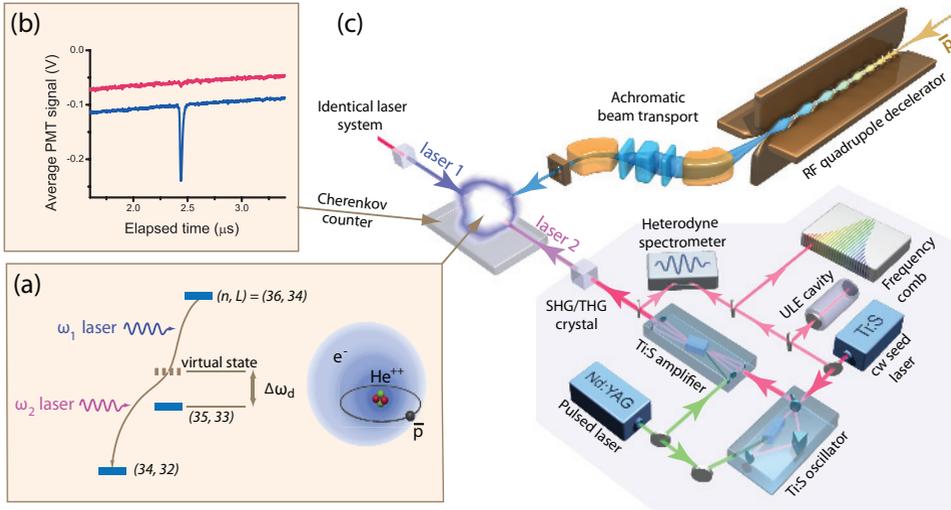
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Figure 1. Energy level diagram of $\overline{p}{}^4\mathrm{He}^+$ involved in the two-photon transition $(n, \ell) = (36, 34) \rightarrow (34, 32)$ (a). Cherenkov detector signals for two-photon transition (b). Experimental layout (c). From Ref. [4].

$\overline{p}\mathrm{He}^{2+}$ ion [11] was destroyed by Stark collisions with other helium atoms in the experimental target. The charged pions emerging from the resulting antiproton annihilations were detected by Cherenkov detectors [12] placed around the target. The two-photon resonance condition between the laser and $\overline{p}\mathrm{He}^+$ was revealed as a sharp spike in the rate of antiproton annihilations [Fig. 1 (b)].

Two sets of Ti:Sapphire lasers [13] of pulse length 30-100 ns with a spectral linewidth of ~ 6 MHz and a pulse energy of 50–100 mJ were used to excite the antiprotonic transitions. The system included continuous-wave (cw) lasers whose frequencies were measured to a precision of $< 1 \times 10^{-10}$ against a femtosecond optical frequency comb [14].

The experiments were carried out at the Antiproton Decelerator (AD) facility of CERN as part of its atomic physics [15] program. The AD provided 200-ns-long pulsed beams, which contained $\sim 10^7$ antiprotons of kinetic energy 5.3 MeV. The antiprotons were decelerated to ~ 70 keV using a radiofrequency quadrupole decelerator [7]. Secondary electron emission detectors measured the spatial profiles of the beam [16]. The $\overline{p}\mathrm{He}^+$ atoms were produced by stopping the antiprotons in a target filled with $^4\mathrm{He}$ or $^3\mathrm{He}$ gas at temperature $T \sim 15$ K and pressure $p = 0.8 - 3$ mbar. Two horizontally-polarized laser beams of energy density ~ 1 mJ/cm^2 fired through the target excited the two-photon transitions.

The Cherenkov signal corresponding to some 10^7 $\overline{p}\mathrm{He}^+$ atoms is shown in Fig. 1(b), as a function of time elapsed since the arrival of antiproton pulses at the experimental target. Lasers of wavelengths $c/\nu_1 = 417$ and $c/\nu_2 = 372$ nm were tuned to the two-photon transition $(n, \ell) = (36, 34) \rightarrow (34, 32)$, so that the virtual intermediate state lay $\Delta\nu_d \sim 6$ GHz away from the real state $(35, 33)$. This arrangement strongly enhanced the transition probability. The annihilation spike which corresponds to the two-photon transition can be seen at $t = 2.4\mu s$. The intensity of the spike reflects the number of antiprotons populating state $(36, 34)$ [17, 18]. When the 417-nm laser was tuned some ~ 0.5 GHz off the two-photon resonance condition, the signal disappeared as indicated in the same figure.

Fig. 2(b) shows the resonance profile measured by detuning the ν_1 laser to $\Delta\nu_d = -6$ GHz, whereas the ν_2 laser was scanned between -1 and 1 GHz around the two-photon resonance defined by $\nu_1 + \nu_2$.
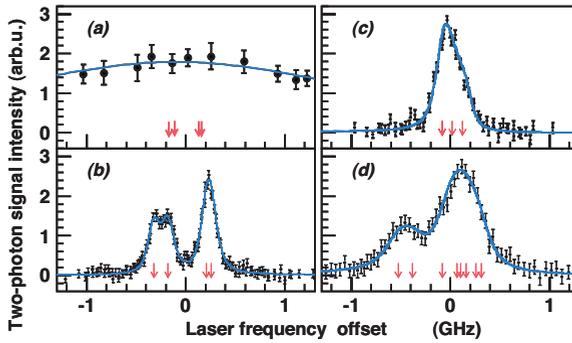
Figure 2. Single-photon resonance $(36, 34) \rightarrow (35, 33)$ of $\overline{p}^4\mathrm{He}^+$ (a). Sub-Doppler two-photon profiles of $(36, 34) \rightarrow (34, 32)$ (b) and $(33, 32) \rightarrow (31, 30)$ (c) of $\overline{p}^4\mathrm{He}^+$, and $(35, 33) \rightarrow (33, 31)$ of $\overline{p}^3\mathrm{He}^+$ (d). Solid lines indicate best fit of theoretical line profiles (see text) and partly overlapping arrows the positions of the hyperfine lines. From Ref. [4].
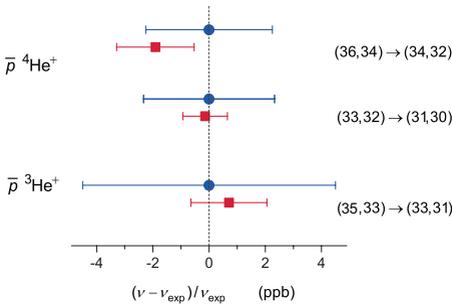

Figure 3. Fractional deviation between theoretical (squares) and experimental (circles) transition frequencies of $\overline{p}\mathrm{He}^+$ isotopes measured by two-photon laser spectroscopy. From Ref. [4].
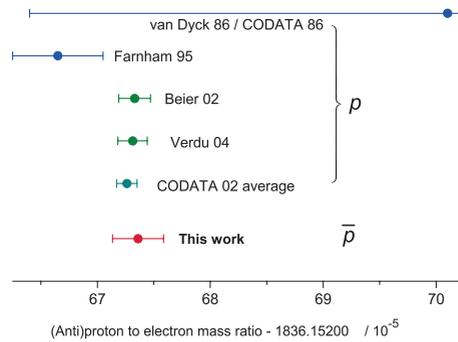

Figure 4. Mass ratio $M_{\overline{p}}/m_e$ determined in this work, compared with M_p/m_e measured previously [21–24] and the CODATA 2002 value obtained by averaging them. From Ref. [4].

The linewidth (~ 200 MHz) of this two-photon resonance is more than an order of magnitude smaller than the Doppler- and power-broadened profile of the single-photon resonance $(36, 34) \rightarrow (35, 33)$ [Fig. 2(a)]. The two-peak fine structure arises due to the interaction between the electron spin and the orbital angular momentum of the antiproton. We also detected the $(33, 32) \rightarrow (31, 30)$ and $(35, 33) \rightarrow (33, 31)$ resonances of $\overline{p}^4\mathrm{He}^+$ and $\overline{p}^3\mathrm{He}^+$, respectively [Fig. 2(c)–(d)]. The latter resonance profile contains eight partially-overlapping hyperfine lines, which arose from the spin-spin interactions of the three constituent particles. The spin-independent transition frequencies ν_{exp} were obtained by fitting these measured profiles with a theoretical lineshape (solid lines in Fig. 2) which was determined by numerically solving the rate equations of the two-photon process [10]. The positions of the hyperfine lines were fixed to the theoretical values [19], which have a precision of < 0.5 MHz.

The experimental transition frequencies ν_{exp} (filled circles with error bars in Fig. 3) agree with the theoretical frequencies ν_{th} (squares) within a fractional precision of $(2.3 - 5) \times 10^{-9}$. The calculation

uses the fundamental constants compiled in CODATA2002 [20], such as the ^{3}He- and ^{4}He-to-electron mass ratios, the Bohr radius, and Rydberg constant. The charge radii of the ^{3}He and ^{4}He nuclei give relatively small corrections to ν_{th} of $4 - 7$ MHz [5]. The correction from the antiproton radius is less than 1 MHz. The theoretical precision of ν_{th} is now mainly limited by the uncalculated radiative corrections of order $m_e c^2 \alpha^8 / h$ [5]. When the antiproton-to-electron mass ratio $M_{\bar{p}}/m_e$ in these calculations was increased by a relative amount of 10^{-9}, the ν_{th}-value changed by 2.3–2.8 MHz. By minimizing the difference between ν_{th} and ν_{exp} and considering the systematic errors, we obtained the above antiproton-to-electron mass ratio which yielded the best agreement between theoretical and experimental frequencies. The uncertainty includes the statistical and systematic experimental, and theoretical contributions of 18×10^{-7}, 12×10^{-7}, and 10×10^{-7}. This is in good agreement with previous measurements[21–24] of the proton-to-electron mass ratio (Fig. 4). Under the assumption that CPT invariance is valid (i.e, $M_{\bar{p}} = M_p = 1.00727646677(10)$ u), we derived a value for the electron mass, $m_e = 0.0005485799091(7)$ u [4].

Acknowledgements

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