SAID analysis of meson photoproduction: Determination of neutron and proton EM couplings

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Abstract. We present an overview of the GW SAID group effort to analyze on new pion photoproduction on both proton- and neutron-targets. The main database contribution came from the recent CLAS and MAMI unpolarized and polarized measurements. The differential cross section for the processes $\gamma n \to \pi^- p$ was extracted from new measurements accounting for Fermi motion effects in the impulse approximation (IA) as well as NN- and π N effects beyond the IA. The electromagnetic coupling results are compared to other recent studies.

1. SAID for baryon spectroscopy

The properties of the resonances for the non-strange sector have been determined almost entirely from the results of πN elastic scattering analyses [1]. Meson photoproduction reactions have mainly served to fix electromagnetic (EM) couplings. With the refinement of multichannel fits and the availability of highprecision photoproduction data for both single- and double-meson production, identifications of some new states have emerged mainly due to evidence from reactions not involving single-pion-nucleon initial or final states [1]. The GW SAID N^* program consists of $\pi N \to \pi N$, $\gamma N \to \pi N$, and $\gamma^* p \to \pi N$ components as was established by Dick Arndt on 1997. Assuming dominance of two hadronic channels $[\pi N]$ elastic and $\pi N \to \eta N$, we parametrize $\gamma^* p \to \pi N$ in terms of $\pi N \to \pi N$ amplitudes ([2] and references therein). Most of the pion photoproduction analyses use SAID πN partial-wave analysis (PWA) outcome [3] or its modification as input for the constraint as well. However, beyond πN elastic scattering, single-pion photoproduction remains the most studied source of resonance information. Much of the effort aimed at providing complete or nearly complete information for meson-nucleon photoproduction reactions has been directed to measuring double-polarization observables. However, often overlooked is that the data coverage for several single-polarization observables, also vital in determining the properties of the nucleon resonance spectrum, still remains incomplete.

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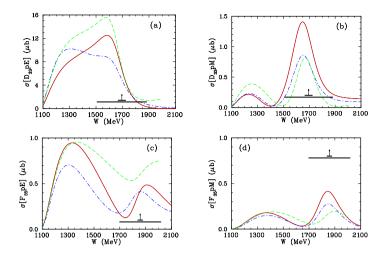


Figure 1. Partial cross sections for multipoles with the largest change was found after including the new CLAS data in the fit, $\Delta(1700)3/2^-$ and $\Delta(1905)5/2^+$. Solid (dash-dotted) lines correspond to the SAID DU13 [8] (CM12 [2]) solution. Dashed lines give MAID07 [9], Vertical arrows indicate resonance energies W_R and horizontal bars show full $\Gamma_{\pi N}$ widths associated with the SAID πN solution WI08 [3].

Here we focus on the single-pion production data and note that a complete solution requires couplings from both charged and neutral resonances [4, 5], the latter requiring $\pi^- p$ and $\pi^0 n$ photoproduction off a neutron target, typically a neutron bound in a deuteron target. Extraction of the two-body $(\gamma n \to \pi^- p)$ and $\gamma n \to \pi^0 n$ cross sections requires the use of a model-dependent nuclear correction, which mainly comes from final-state interactions (FSI) [6]. As a result, our knowledge of the neutral resonance couplings is less precise than that of the charged values for well-known low-laying baryons. The uncertainties for such kind of neutral states with $J^P = \frac{1}{2}$, for instance, $N(1440)1/2^+$, $N(1535)1/2^-$, and $N(1650)1/2^-$ vary from 25% to 140% [1]. Some of the N* baryons [$N(1675)5/2^-$, for instance] have stronger EM couplings to the neutron than to the proton, but parameters are very uncertain ($N^* \to \gamma p$: $+0.019 \pm 0.008 \, \text{GeV}^{-1/2}$ while $N^* \to \gamma n$: $-0.043 \pm 0.012 \, \text{GeV}^{-1/2}$ [1]). Then, PDG12 estimates for the $A_{1/2}$ and $A_{3/2}$ proton decay amplitudes of the $N(1720)3/2^+$ state are consistent with zero, while the recent SAID determination [2] gives small but non-vanishing values. Other unresolved issues relate to the second P_{11} , $N(1710)1/2^+$, that we do not seen in the recent SAID πN PWA [3] contrary to the findings of other PWAs referenced by PDG12 [1].

2. Pion photoproduction off the proton

The overall SAID χ^2 has remained stable (χ^2 /data = 2.1) against the growing database, which has increased by a factor of 2 since 1995 (13.4 k up to 27.3 k data points) [7]. Most of this increase coming from photon-tagging facilities. More complete data sets for double- and single-polarization observables for pion photoproduction can offer important constraints on analyses of the photoproduction reaction.

Using linearly polarized photons and an unpolarized target, CLAS provides a large set of beam asymmetry Σ measurements for $\gamma p \to \pi^0 p$ and $\gamma p \to \pi^+ n$ from $E_{\gamma} = 1.100$ and up to 1.860 GeV in laboratory photon energy, corresponding to a CM energy W range of 1.7–2.1 GeV ($\theta = 30 - 150^{\circ}$ of pion production angle in CM) [8]. Its contribution to the world database is more than doubled [7]. In Fig. 1, we show the effect of new CLAS Σ measurements in terms of partial cross sections from SAID (CM12 [2] and recent DU13 [8] included new CLAS data) and MAID [9]. While the CM12 and DU13 solutions differ over the energy range of the recent CLAS experiment, the resonance couplings are fairly

Table 1. Proton helicity amplitudess $pA_{1/2}$ and $pA_{3/2}$ (in [(GeV)^{-1/2} × 10⁻³] units).

Resonance	$pA_{1/2}$	$pA_{3/2}$	Ref.	
$\Delta(1700)3/2^{-}$	132 ± 5	108 ± 5	SAID DU13 [8]	
	105 ± 5	92 ± 4	SAID CM12 [2]	
	160 ± 20	165 ± 25	BnGa12 [10]	
	58 ± 10	97 ± 8	Kent12 [11]	
	226	210	MAID [9]	
	104 ± 15	85 ± 22	PDG12 [1]	
$\Delta(1905)5/2^{+}$	20 ± 2	-49 ± 5	SAID DU13 [8]	
	19 ± 2	-38 ± 4	SAID CM12 [2]	
	25 ± 5	-49 ± 4	BnGa12 [10]	
	66 ± 18	-223 ± 29	Kent12 [11]	
	18	-28	MAID [9]	
	26 ± 11	-45 ± 20	PDG12 [1]	

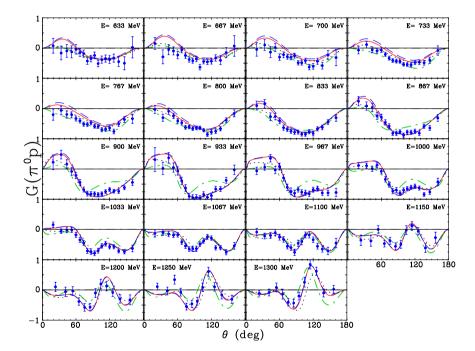


Figure 2. The double-polarization observable G as a function of pion production angle in CM. Dashed (solid) lines correspond to the SAID (DU13 [8] and preliminary solution included new CB-ELSA G measuremenents. Dotted (dash-dotted) lines give BnGa12 [10] (MAID07 [9]).

stable. The largest change is found for the $\Delta(1700)3/2^-$ and $\Delta(1905)5/2^+$ states, for which the various analyses disagree significantly in terms of photo-decay amplitudes (Table 1).

With the inclusion of new high-precision data, our fits are becoming more stable and predictive. Plots of recent double polarized G data, covered $E_{\gamma}=630-1300\,\text{MeV}$ and $\theta=20-160^{\circ}$, in Fig. 2 from CB-ELSA [12] show that the SAID CM12 fit gives a good prediction of this quantity. We have recently analyzed $C_{x'}$ ($E_{\gamma}=460-1340\,\text{MeV}$ and $\theta=75-140^{\circ}$) [13] and preliminary F and T data ($E_{\gamma}=440-1430\,\text{MeV}$ and $\theta=30-160^{\circ}$) [14] from Mainz, finding a similarly quantitative level of agreement.

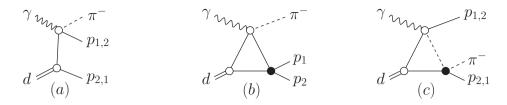


Figure 3. Feynman diagrams for the leading terms of the $\gamma d \to \pi^- pp$ amplitude. (a) IA, (b) pp-FSI, and (c) πN -FSI. Filled black circles show FSI vertices. Wavy, dashed, solid, and double lines correspond to the photons, pions, nucleons, and deuterons, respectively.

3. Pion photoproduction off the neutron

In addition to being less precise, experimental data for neutron-target photoreactions are much less abundant than those utilizing a proton target, constituting only about 15% of the present SAID database [7]. At low to intermediate energies, this lack of neutron-target data is partially compensated by experiments using pionic beams, e.g., $\pi^-p \to \gamma n$, as has been measured, for example, by the Crystal Ball Collaboration at BNL [15] for the inverse photon energy $E_{\gamma}=285$ –690 MeV and $\theta=40$ –150°, where θ is the inverse production angle of pion in the CM frame. This process is free from complications associated with the deuteron target. However, the disadvantage of using the reaction $\pi^-p \to \gamma n$ for the pion photoproduction study is the 5 to 500 times larger cross sections for $\pi^-p \to \pi^0 n \to \gamma \gamma n$, depending on E_{γ} and θ .

We extract the $\gamma n \to \pi^- p$ cross section on free nucleon from the deuteron data in the quasi-free (QF) kinematic region of the $\gamma d \to \pi^- pp$ reaction with fast knocked-out proton and slow proton-spectator assumed not to be involved in the pion production process. In this, so-called impulse approximation (IA) [16], the reaction mechanism corresponds to the diagram in Fig. 3a. There are 2 critical factors to be taken into account when using this approach: (i) the neutron is bound and (ii) there are NN- and πN -FSI effects.

Item (i) means that the effective mass of the neutron is not equal to the mass of the free neutron. In our former analyses [17, 18], the $\gamma n \to \pi^- p$ amplitude for a given E_γ and CM pion production angle θ is assumed to be the same as on a free neutron at rest. That is why the cross section obtained should be considered as an average over energies around E_γ . The size of the averaging region is determined by a smearing of the energy owing to the Fermi-motion in the deuteron. The typical scale here is 20 MeV in energy.

Item (ii) corresponds to the inclusion of the FSI corrections. Their leading terms correspond to Feynman diagrams shown on Fig. 3(b,c). Determinations of the $\gamma d \to \pi^- pp$ differential cross section, with the FSI taken into account (all the diagrams on Fig. 3, were included) were done recently for the CLAS [17] and MAMI-B [18] $\gamma d \to \pi^- pp$ data. The SAID phenomenological amplitudes for $\gamma N \to \pi N$ [19], NN-elastic [20], and πN -elastic [3] were used as inputs to calculate the diagrams in Fig. 3. The Bonn potential [21] was used for the deuteron description.

Recently, we applied our FSI corrections [22] to CLAS $\gamma d \to \pi^- pp$ data ($E_\gamma = 1050-2700\,\text{MeV}$ and $\theta = 30-160^\circ$) [23] to get elementary cross sections for $\gamma n \to \pi^- p$ [17]. New CLAS differential cross sections are quadrupling the world database for $\gamma n \to \pi^- p$ above 1 GeV. The FSI correction factor for the CLAS kinematics was found to be small, $\Delta \sigma / \sigma < 10\%$. However, these new cross sections departed significantly from our predictions at the higher energies, and greatly modified the fit result, which allows to determine new neutron couplings (Table 2).

In our recent study [18], we addressed to the differential cross section measurements for $\gamma n \to \pi^- p$ in the Δ -isobar region. The data came from MAMI-B (E_{γ} = 300–455 MeV and θ = 60–140°) [24]. At energies dominated by the Δ -resonance, the isospin I = 3/2 multipoles are constrained by extensive

Resonance	$nA_{1/2}$	Resonance	$nA_{1/2}$	$nA_{3/2}$	Ref.
$N(1535)1/2^-$	-58 ± 6	$N(1520)3/2^-$	-46 ± 6	-115 ± 5	SAID GB12 [17]
	-60 ± 3		-47 ± 2	-125 ± 2	SAID SN11 [25]
	-93 ± 11		-49 ± 8	-113 ± 12	BnGa13 [26]
	-49 ± 3		-38 ± 3	-101 ± 4	Kent12 [11]
	-46 ± 27		-59 ± 9	-139 ± 11	PDG12 [1]
$N(1650)1/2^-$	-40 ± 10	$N(1675)5/2^-$	-58 ± 2	-80 ± 5	SAID GB12 [17]
	-26 ± 8		-42 ± 2	-60 ± 2	SAID SN11 [25]
	25 ± 20		-60 ± 7	-88 ± 10	BnGa13 [26]
	11 ± 2		-40 ± 4	-68 ± 4	Kent12 [11]
	-15 ± 21		-43 ± 12	-58 ± 13	PDG12 [1]
$N(1440)1/2^+$	48 ± 4	$N(1680)5/2^+$	26 ± 4	-29 ± 2	SAID GB12 [17]
	45 ± 15		50 ± 4	-47 ± 2	SAID SN11 [25]
	43 ± 12		34 ± 6	-44 ± 9	BnGa13 [26]
	40 ± 5		29 ± 2	-59 ± 2	Kent12 [11]
	40 ± 10		29 ± 10	-33 ± 9	PDG12 [1]

Table 2. Neutron helicity amplitudes $nA_{1/2}$ and $nA_{3/2}$ (in [(GeV)^{-1/2} × 10⁻³] units).

studies performed using proton targets. The forward peaking structure is due largely to the Born contribution, which is well known. As a result, one would expect models to give predictions within a tight range.

We have included the new neutron cross sections from the CLAS and MAMI-B experiments in a number of multipole analyses covering incident photon energies up to 2.7 GeV, using the full SAID database [7], in order to gauge the influence of these measurements, as well as their compatibility with previous experiments. The solution, GB12 [17], uses the same fitting form as our recent SN11 solution [25]. A second fit, GZ12, instead used the recently proposed form based on a unified Chew-Mandelstam parametrization of the GW DAC fits to both πN elastic scattering and photoproduction [21].

Table 2 shows that the new SAID GB12 $nA_{1/2}$ and $nA_{3/2}$ helicities sometimes have a significant deviation from the previous SAID SN11 [25] determination and PDG12 [1] values, e.g., for $N(1650)1/2^-$, $N(1675)5/2^-$, and $N(1680)5/2^+$. While BnGa13 group [26] used the same (almost) data to fit them as we are while BnGa13 has several new ad hoc resonances. Meanwhile, BnGa13 determination is different for $N(1535)1/2^-$, $N(1650)1/2^-$, and $N(1680)5/2^+$.

4. Summary

Future progress in the database development is expecting from tagged-photon fasilities as JLab, MAMI-C, SPring-8, CB-ELSA, and ELPH. Partial-wave analyses will clearly benefit from the constraints provided by these new data, which highlight the importance of new polarization observables in providing a stringent test of PWA, even in kinematic regions where a large number of cross section and polarization observables are already present in the world database. An accurate PWA must ultimately describe a complete set of observables. The current data and future experiments exploiting these polarimetry developments at large acceptance detectors will be a key part to achieving this complete measurement.

In this regard, future experiments to measure unpolarized and the spin polarization of neutrons are already planned at MAMI-C. Measurements of such observables with large acceptance are crucial to the world program aiming to determine the excitation spectrum of the nucleon.

We proposed to perform a precision measurement of $d\sigma/d\Omega$ in the reactions $\gamma d \to \pi^- pp$ and $\gamma d \to \pi^0 np$ in the tagged-photon energy region from threshold to 800 MeV [27] and then to 1500 MeV [28]. The $d\sigma/d\Omega$ for the processes $\gamma p \to \pi^- p$ and $\gamma p \to \pi^0 n$ will be extracted from these CB@MAMI-C measurements accounting for Fermi motion effects in IA [16] as well as NN- and π N-FSI effects beyond the IA. Data below 800 MeV were taken in March of 2013 and analysis is in progress.

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Consequential calculations of the FSI corrections, as developed by our GW-ITEP Collaboration, will be applied. We will extend our FSI code [22] to extract $\gamma n \to \pi^0 n$ data from $\gamma d \to \pi^0 n p$ measurements as well. Polarized measurements will help to bring more physics in. FSI corrections need to apply.

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