

Ultra-relativistic heavy-ion collisions - a hot cocktail of hydrodynamics, resonances and jets

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Abstract. Ultra-relativistic heavy-ion collisions at energies of RHIC and LHC are considered. For comparison with data the HYDJET++ model, which contains the treatment of both soft and hard processes, is employed. The study focuses mainly on the interplay of ideal hydrodynamics, final state interactions and jets, and its influence on the development of harmonics of the anisotropic flow. It is shown that jets are responsible for violation of the number-of-constituent-quark (NCQ) scaling at LHC energies. The interplay between elliptic and triangular flows and their contribution to higher flow harmonics and dihadron angular correlations, including ridge, is also discussed.

1 Introduction

Heavy-ion collisions at ultra-relativistic energies, accessible for modern colliders such as Relativistic Heavy Ion Collider (RHIC) at BNL and Large Hadron Collider (LHC) at CERN, revealed several signals which favored the creation of a new state of matter - quark-gluon plasma (QGP) - during the earlier phase of the collision. Among these signals are strong collective flow of secondary hadrons, particularly *elliptic* flow [1], and the phenomenon of jet quenching [2]. Recall, that the flow analysis in the azimuthal plane is performed in terms of Fourier series [3, 4]

$$E \frac{d^3N}{d^3p} = \frac{1}{\pi} \frac{d^2N}{dp_T^2 dy} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n \cos [n(\phi - \Psi_n)] \right\}, \quad (1)$$

where Ψ_n is the azimuth of the participant plane of n -th order, ϕ is the azimuthal angle between the particle transverse momentum p_T and the participant plane, and y is the particle rapidity. The flow harmonic coefficients are

$$v_n = \langle \cos [n(\phi - \Psi_n)] \rangle, \quad (2)$$

where one has to average over all particles in a single event and then over all events, respectively. Harmonics are called directed, v_1 , elliptic, v_2 , triangular, v_3 , quadrangular (sometimes, hexadecapole),

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v_4 , pentagonal, v_5 , hexagonal, v_6 , flow and so on. The first two flow components have been studied in heavy-ion collisions at different energies for more than 15 years, whereas systematic investigation of triangular flow and higher harmonics started about 5 years ago. Although elliptic flow is the strongest among the flow harmonics, v_3 and higher order coefficients can carry valuable information about the properties of hot and dense medium at the very early stages of the fireball expansion. At energies of RHIC and LHC hydrodynamic models usually provide a good description of the $v_2(p_T)$ distribution at $p_T \leq 2 \text{ GeV}/c$. At higher transverse momenta the signal is overpredicted in hydrodynamics [5] in contrast to microscopic transport models, which underpredict the elliptic flow at high p_T [6–8]. This gives rise to appearance of hybrid models, e.g. VISHNU [9] and MUSIC [10], where the hydrodynamic description of the early stage is coupled to hadronic cascade as afterburner after the chemical freeze-out.

Hard processes are usually not included in hydrodynamic models. In the flow sector it is just assumed that jets contribute to the p_T -distributions of the flow harmonics at high transverse momenta because of the jet quenching. Also, many hydrodynamic models rely on rather short tables of hadron resonances. Our aim is to show that resonances and jets are quite important for the description of not only the particle yields and p_T -spectra, but also collective effects such as anisotropic flow. The HYDJET++ model (HYDroynamics with JETs) is employed for our study. Basic features of the model are listed in Sec. 2.

2 Basic features of HYDJET++ model

Monte Carlo event generator HYDJET++ [11] is the first model designed for the simulation of relativistic heavy-ion collisions which contains a hydrodynamics coupled to a hard multiparton state. Both soft and hard states are treated independently. The predecessors of the HYDJET++ in soft and hard sectors are FASTMC [12, 13] and PYQUEN [14] event generators, respectively. The soft part of the model represents a relativistic hydrodynamical parametrization of the chemical (single freeze-out scenario) or thermal (double freeze-out scenario) freeze-out hypersurfaces with given freeze-out conditions. The simulation of an individual event starts with calculation of effective volume V_{eff} of the fireball. This volume depends on the mean number of participating nucleons at given centrality, i.e. impact parameter b , of the collision. The latter is determined from the Glauber model of multiple scattering. For the most appropriate scheme with separated chemical and thermal freeze-out, the particle composition in the system is frozen at the stage of chemical freeze-out. The fireball continues to expand and cools down until the thermal freeze-out stage, where the contact between hadrons is lost. The final state interactions (FSI) take into account the two- and three-body decays of the resonances. The model benefits from the extremely rich table of resonances with ca. 350 particles taken from the SHARE thermal model [15]. Note, that HYDJET++ employs its own original routine for treatment of resonance decays.

In hard sector the model propagates the hard partons through the expanding quark-gluon plasma and takes into account both gluon radiation loss and collisional loss because of the parton rescattering. For each hard nucleon-nucleon (NN) collision the PYQUEN routine starts with generation of initial parton spectra and production vertexes at a given impact parameter. In recent version of the model [16, 17] the tune Pro-Q20 of PYTHIA is utilized, whereas earlier modifications [14, 18] relied on standard PYTHIA_6.4 [19]. After the rescattering stage accompanied by radiative and collisional energy loss the partons and in-medium emitted gluons are hadronized according to the Lund string model. The hard event includes also jets. Their number is proportional to the product of number of binary NN collisions in an event at given impact parameter and the integral cross section of the hard processes in NN collision with the minimal transverse momentum transfer, p_T^{min} .

The flow components are implemented in the HYDJET++ as follows. For noncentral collisions the transverse radius of the overlap region is a function of impact parameter b , azimuthal angle ϕ and spatial eccentricity $\epsilon(b) = (R_y^2 - R_x^2)/(R_y^2 + R_x^2)$ [13],

$$R_{ell}(b, \phi) = R_{fr.-out}(b) \sqrt{\frac{1 - \epsilon^2(b)}{1 + \epsilon(b) \cos 2\phi}} \quad (3)$$

with

$$R_{fr.-out}(b) = R_0 \sqrt{1 - \epsilon(b)} \quad (4)$$

In the last formula $R_0 \equiv R_{fr.-out}(0)$ is the freeze-out radius of the fireball in a central collision. The momentum anisotropy arises from the pressure gradients, which are stronger in the direction of short axis of the ellipsoid. Then, the azimuthal angle ϕ_{fl} in HYDJET++ does not coincide with the azimuthal angle ϕ as in the case of transverse isotropic parametrization. Instead, both angles are linked via the nonzero flow anisotropy parameter $\delta(b)$ as [13]

$$\tan \phi_{fl} = \sqrt{\frac{1 - \delta(b)}{1 + \delta(b)}} \tan \phi \quad (5)$$

Parameters $\epsilon(b)$ and $\delta(b)$ are proportional to the initial spatial anisotropy $\epsilon_0 = b/(2R_A)$.

Triangular flow in the model is obtained by further modification of the transverse radius [16]

$$R_{triang}(b, \phi) = R_{ell}(b, \phi) \{1 + \epsilon_3(b) \cos [3(\phi - \Psi_3)]\}. \quad (6)$$

Experimental data indicate no correlations between the reaction planes Ψ_2 and Ψ_3 , therefore position of the plane Ψ_3 in the generated events is isotropically distributed w.r.t. the plane Ψ_2 . $\epsilon_3(b)$ is a new free parameter responsible for appearance of triangularity in the system. It can be treated independently or expressed via the initial ellipticity $\epsilon_0(b)$. It is worth mentioning that introduction of triangular modulation in the system does not change the elliptic flow v_2 . Further details of the model can be found elsewhere [11–14]. Here we would like to stress that the model extension to triangular flow appears very fruitful. It enables one to study the cross-talk of elliptic and triangular harmonics and their contributions to higher flow harmonics in ideal conditions, because all other eccentricities, such as ϵ_4 , ϵ_5 , etc., are absent. Several important consequences of the interplay between v_2 and v_3 are discussed below.

3 Elliptic flow. Interplay of hydrodynamics and jets

Elliptic flow of hadrons in Au+Au collisions at RHIC and in Pb+Pb collisions at LHC was among the first collective effects considered within the HYDJET++ model. First of all, it appeared that the differential flow $v_2(p_T)$ had a characteristic hump structure around 2.5–3.5 GeV/c, see Fig. 1, where the elliptic flow reached its maximum value and then rapidly dropped. In experimental data such a hump profile became pronounced when the methods based on particle cumulants and Lee-Yang zeroes (LYZ) were extended to the range of intermediate transverse momenta $2 \text{ GeV}/c \leq p_T \leq 5 \text{ GeV}/c$. Standard two-particle correlation method gives almost flat distribution of $v_2(p_T)$ at $p_T \geq 2.5 \text{ GeV}/c$. Then, the model demonstrated crossing of meson and baryon branches, as shown in Fig. 1. Here the elliptic flows of identified charged hadrons are compared to those measured by PHENIX and STAR collaborations in Au+Au collisions at full RHIC energy $\sqrt{s} = 200 \text{ AGeV}$. Note, that in ideal hydrodynamics the $v_2(p_T)$ distributions of hadrons grow without crossing up to unity. Both effects, i.e.

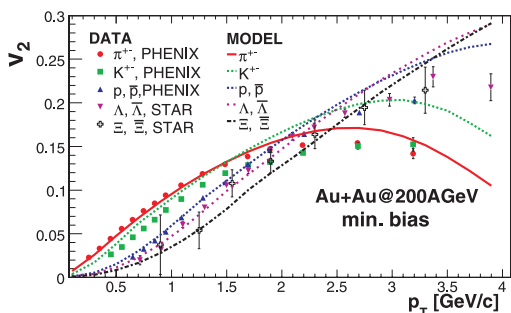


Figure 1. The $v_2(p_T)$ distributions in the HYDJET++ model for different hadron species (lines) and comparison with RHIC data (symbols) (from [21]).

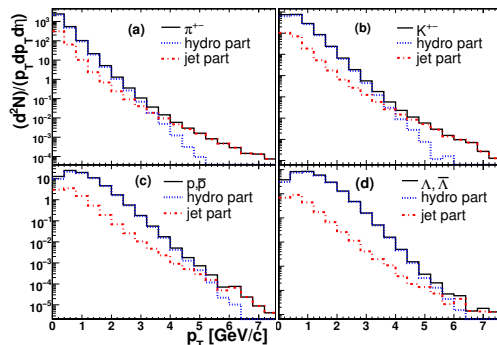


Figure 2. The p_T distribution for charged pions, kaons, protons and antiprotons, and Lambdas in HYDJET++ calculations of Pb+Pb collisions with centrality $c \approx 40\%$ at LHC (from [20]).

(1) the saturation and the subsequent drop of hadron elliptic flow with rising transverse momentum, and (2) the crossing of meson and baryon branches demonstrate clearly the influence of jets. Figure 2 presents the p_T spectra of most abundant particle species in comparison to their hydrodynamic (soft) and jet (hard) parts. Lighter hadrons have softer p_T -spectra, thus the slopes of their hydrodynamically generated distributions are steeper. Therefore, the change from hydro-dominated to jet-dominated regime occurs for mesons at lower p_T compared to that for baryons, as was pointed out in [20, 21]. Hadrons emerging from the jet fragmentation develop very weak elliptic flow due to well-known jet quenching process, and the combined $v_2(p_T)$ drops at certain p_T threshold. At higher transverse momenta heavier hadrons possess larger v_2 .

Another interesting feature of elliptic flow which was considered as a “smoking gun” revealing the QGP formation is the number-of-constituent-quark (NCQ) scaling, first observed in gold-gold collisions at RHIC in [22, 23]. If the elliptic flow v_2 and the transverse kinetic energy $KE_T = m_T - m_0$ are divided by a number of constituent quarks n_q , 2 for mesons and 3 for baryons, then the distributions $v_2/n_q(KE_T/n_q)$ for all hadrons coincide with good accuracy up to $KE_T/n_q \approx 1$ GeV. This circumstance was taken as a strong evidence of the predominant production of elliptic flow from the quark coalescence at the partonic, i.e. plasma, stage. However, in Pb+Pb collisions at LHC energy $\sqrt{s} = 2.76$ ATeV the NCQ scaling was found to be violated [24], whereas recent results of beam energy scan (BES) at RHIC confirm the scaling fulfillment in a broad energy range 7.7 AGeV $\leq \sqrt{s} \leq 62$ AGeV [25]. At the first sight the results look puzzling, although the violation of NCQ scaling at LHC energies was *predicted* in [20]. Jet phenomena are again the processes which should be responsible for worsening of the scaling. Figure 3 displays the reduced functions $v_2(KE_T/n_q)$ calculated within the HYDJET++ model for 20%-30% central Pb+Pb collisions at 2.76 ATeV. The panels show the elliptic flow of only directly produced hadrons, the flow modified by decays of resonances (jet contribution is excluded), and the final v_2 of hadrons, where both hard and soft processes are taken into account. One can see in Fig. 3 that resonances are extremely important, because they drive the particle elliptic flow towards the NCQ scaling. To see the degree of the scaling fulfillment explicitly all particle flows in the bottom row are normalized to the flow of protons, $v_2^h/n_q : v_2^p/n_q$. The feed-down from heavy resonances makes the elliptic flow of light hadrons harder, whereas, for instance, flow of ϕ mesons is unchanged due to the absence of the resonance boost. But then jets come into

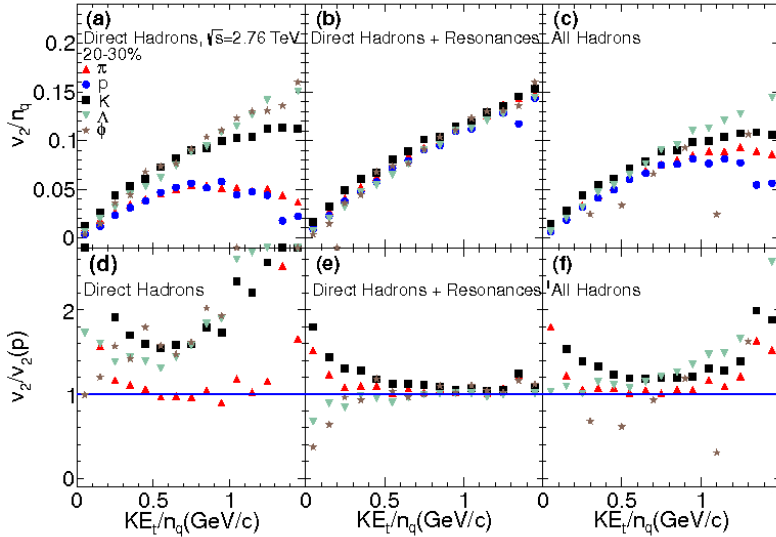


Figure 3. Upper row: The KE_T/n_q dependence of elliptic flow for (a) direct hadrons, (b) hadrons produced both directly and from resonance decays, and (c) all hadrons produced in the HYDJET++ model for Au + Au collisions at $\sqrt{s} = 200A$ GeV with centrality 20–30%. Bottom row: The KE_T/n_q dependence of the ratios $(v_2/n_q)/(v_2^p/3)$ for (d) direct hadrons, (e) direct hadrons plus hadrons from the decays, and (f) all hadrons (from [26]).

play and spoil the result completely. In heavy-ion collisions jets are more abundant at LHC energies than at RHIC ones, therefore, the NCQ scaling at LHC holds only approximately despite the fact that in pure hydrodynamic sector with final state interactions the scaling performance is very good.

Figure 4 demonstrates the importance of final state interactions for the development of hadron elliptic flow. Only v_2 of kaons seems to be unchanged, while the flows of charged pions, protons + antiprotons and Lambdas become stronger. Soft pions coming from the resonance decays possess lower momentum anisotropy. On the other hand, hard pions and heavier particles have larger elliptic flow attributed to massive resonances.

4 Triangular flow

Triangular flow v_3 was introduced in the HYDJET++ model relatively recently [16, 17]. Figure 5 shows the model generated v_3 of charged hadrons in Pb+Pb collisions at 2.76 ATeV compared to CMS data [27]. In order to estimate uncertainties in experimental determination of the v_3 signal, the event-plane (EP) method was applied to restore the triangular flow out of the generated particle spectra. The restored triangular flow is plotted in Fig. 5 also. One can see that overall agreement with the data is good. At transverse momenta below 3 GeV/c the “true” flow $v_3(\Psi_3^{\text{RP}})$ coincides with that restored by the event-plane method, $v_3\{\text{EP}\}$. At $3 \text{ GeV}/c \leq p_T \leq 4 \text{ GeV}/c$ $v_3\{\text{EP}\}$ exceeds slightly the original flow. Both restored and generated differential triangular flows show a falloff at $p_T \geq 3.5 \text{ GeV}/c$ in accord with the data. As in the case with elliptic flow, such a drop in the flow behavior is caused by hadrons originated from the fragmentation of jets. These hadrons, which carry very little collective

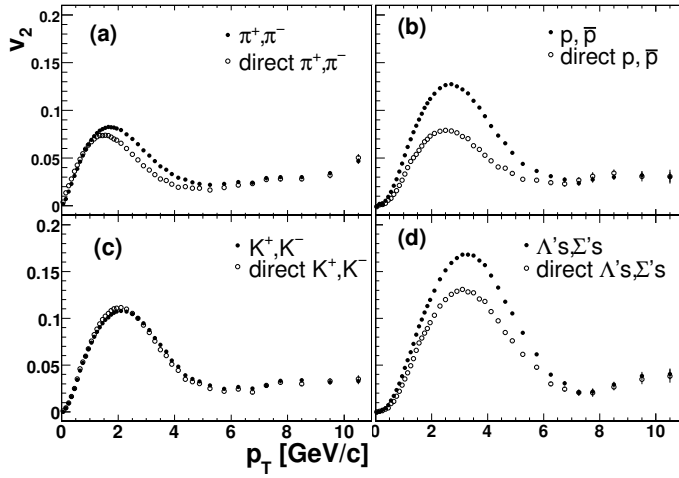


Figure 4. Transverse momentum dependence of elliptic flow of direct hadrons (open symbols) and of all hadrons (full symbols) produced in the HYDJET++ model for Pb+Pb collisions at LHC energy with centrality $c \approx 40\%$: (a) pions, (b) protons, (c) kaons, and (d) Lambdas plus Sigmas (from [20]).

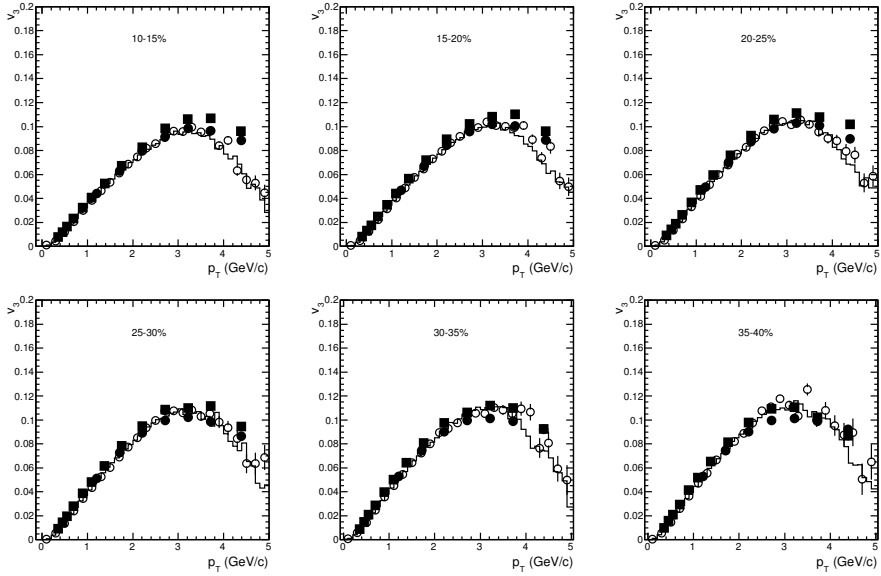


Figure 5. Transverse momentum dependence of triangular flow of charged hadrons in pseudorapidity interval $|\eta| < 0.8$ for six different centralities of Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV. The full symbols are CMS data [27] ($v_3\{2\}$ – circles, $v_3\{\text{EP}\}$ – squares), open circles and histograms represent $v_3\{\text{EP}\}$ and $v_3\{\Psi_3^{\text{RP}}\}$ for HYDJET++ events, respectively (from [16]).

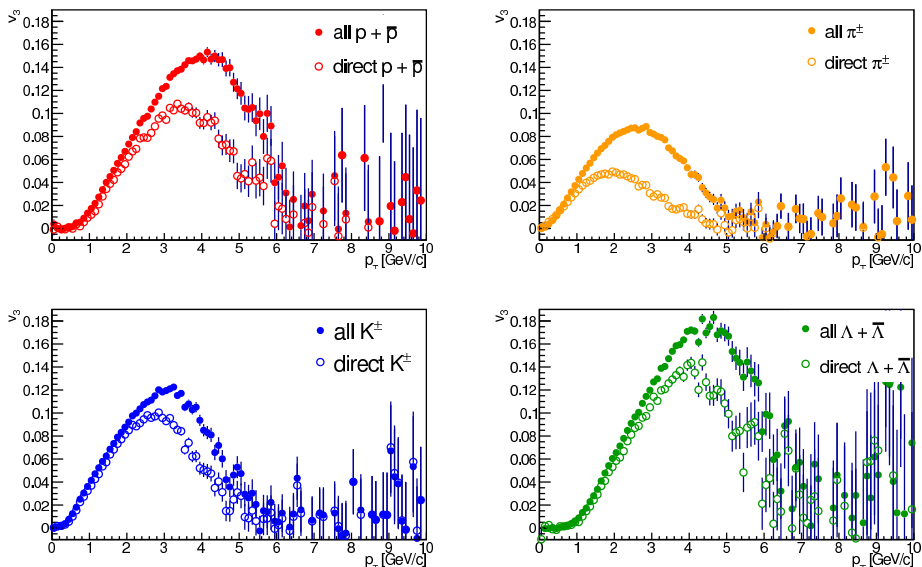


Figure 6. Triangular flow vs. p_T of direct hadrons (open symbols) and of all hadrons (full symbols) in HYDJET++ calculations of 20 - 30% central Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV.

flow, if any, dominate the particle spectrum at intermediate and high p_T . Generally speaking, there are many similarities between the role of jets and final state interactions, i.e. resonance decays, in the development of elliptic and triangular flows. For instance, $v_3(p_T)$ after the decays of resonances is increased and its maximum is shifted to higher transverse momenta, as seen in Fig. 6. The counterplay of jets and resonances also leads to violation of NCQ scaling conditions for triangular flow. Details can be found in J. Crkovska's talk [28] (this volume).

5 Higher flow harmonics

Systematic study of higher flow harmonics v_n , $n > 3$ started relatively recently. Important theoretical result was obtained in [29], where the authors demonstrated that the quadrangular flow v_4 is determined exclusively by the elliptic flow v_2

$$v_4 \simeq \frac{1}{2} v_2^2 \quad (7)$$

at high transverse momenta. Since triangular flow does not affect the v_4 , here we will consider pentagonal and hexagonal flows, respectively. Study of the fulfillment of Eq.(7) in the model and the role of jets in the increase of the ratio v_4/v_2^2 and rise of its high- p_T tail can be found in [26, 30, 31].

Pentagonal v_5 and hexagonal v_6 flow coefficients in non-central lead-lead collisions at $\sqrt{s} = 2.76$ TeV are shown as functions of p_T in Figs. 7 and 8, respectively. Here the HYDJET++ results are compared with CMS data, comparison with ATLAS data can be found in [16]. Because of absence of genuine eccentricity ϵ_5 and related to it reaction plane Ψ_5 in the present version of the model, the generated v_5 shown in Fig. 7 emerges only as a result cross-talk of v_2 and v_3 , namely $v_5 \sim v_2 \cdot v_3$ [32]. Direct check in HYDJET++ reveals that $v_5 = 0$ if either elliptic or triangular flow is absent. If,

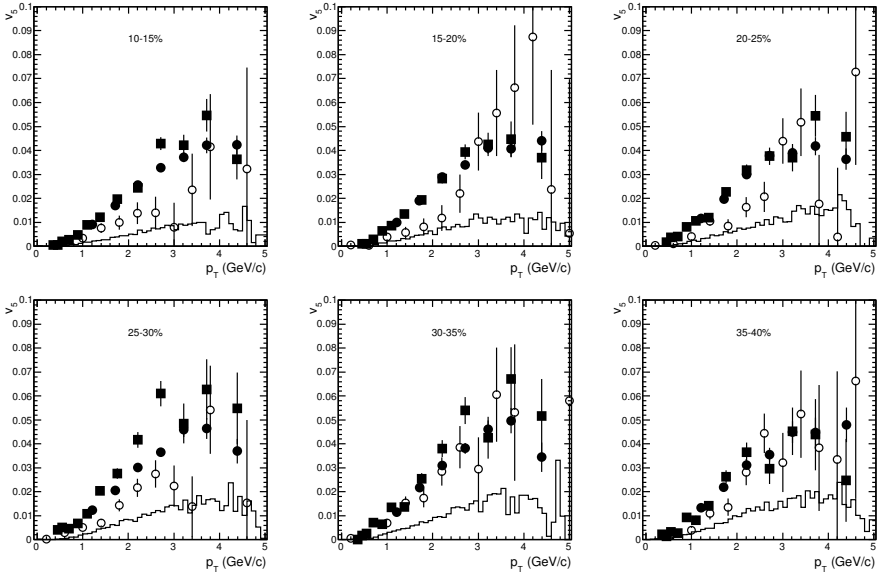


Figure 7. The same as 5 but for pentagonal flow of charged hadrons in Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV (from [16]).

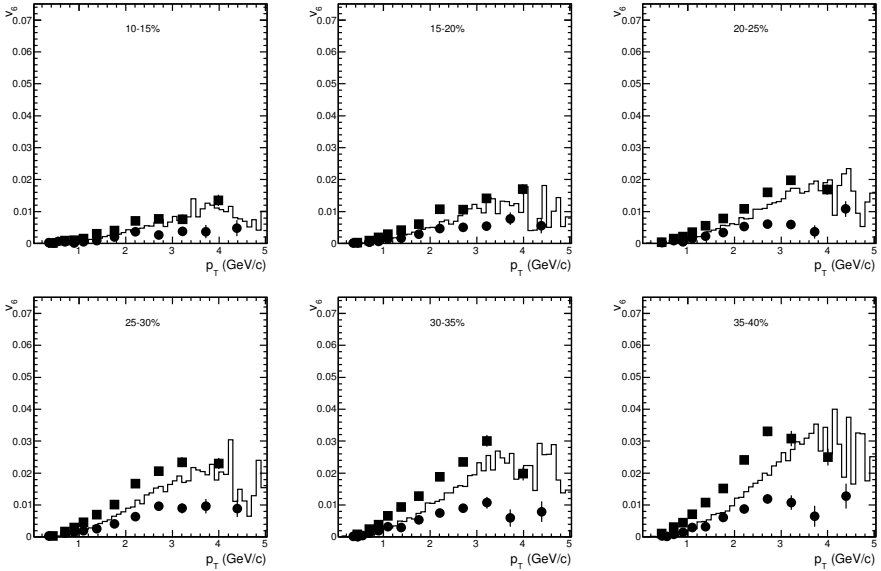


Figure 8. The same as 7 but for hexagonal flow of charged hadrons in Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV (from [16]).

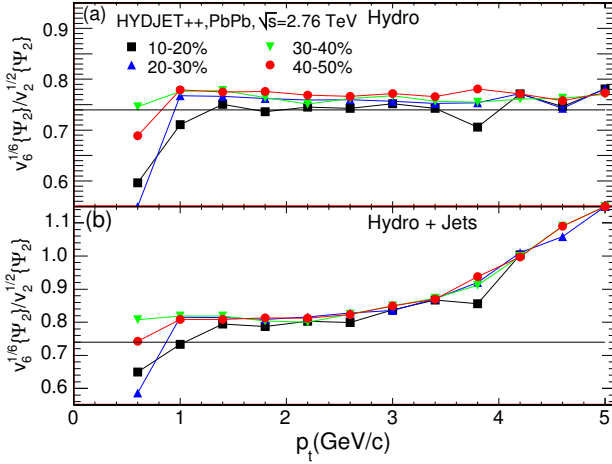


Figure 9. Ratio $v_6^{1/6}/v_2^{1/2}$ as a function of p_T in the Ψ_2 event plane for charged particles, originated from (a) soft processes only and (b) both soft and hard processes, in HYDJET++ simulations of Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV for four selected centralities. Solid lines in both plots show the prediction of ideal hydrodynamics for this ratio at high p_T , $v_6^{1/6}/v_2^{1/2} = (1/6)^{1/6} \approx 0.74$ (from [17]).

however, the event-plane method is applied to generated particle spectra, the reconstructed pentagonal flow in the model appears to be very close to the distributions extracted from the experimental data, especially for semi-peripheral events.

The situation with the hexagonal flow is even more curious, because the v_6 emerging in the model is not a product but rather a sum of independent contributions coming from v_2 and v_3 . Within the same approach as was used for derivation of Eq.(7), it was obtained that

$$v_6 \simeq \frac{1}{6}v_2^3 + \frac{1}{2}v_3^2 \quad (8)$$

in the high- p_T limit [17]. This leads to a non-trivial correlations between the (Ψ_2, Ψ_6) and (Ψ_3, Ψ_6) event planes. Triangular flow weakly increases with rising non-centrality of the collisions, whereas elliptic flow is almost zero for central 0-5% collisions and quickly rises up as the reactions become more peripheral. As a result, for central events hexagonal flow is mainly determined by the v_3 , and Ψ_6 plane should be closer to Ψ_3 plane. In semi-peripheral and peripheral collisions the situation is opposite. Here elliptic flow dominates over the triangular flow, thus Ψ_6 is elongated closer to Ψ_2 rather than to Ψ_3 [17]. Such a behavior was observed in plane correlators $\langle \cos 6(\Psi_2 - \Psi_6) \rangle$ and $\langle \cos 6(\Psi_3 - \Psi_6) \rangle$ in [33]. Another interesting feature is the prediction of the scaling for $v_6^{1/6}\{\Psi_2\}/v_2^{1/2}\{\Psi_2\}$ ratios, where the p_T -distributions for different centralities should sit on the top of each other [17], as displayed in Fig.9. In contrast, for the similar ratios $v_6^{1/6}\{\Psi_3\}/v_3^{1/3}\{\Psi_3\}$ the scaling is not observed. These predictions can be easily checked experimentally. Again, jets increase the ratio of about 10% and cause the rise of the high- p_T tail at $p_T \geq 3$ GeV/c. Other details concerning the peculiarities of the hexagonal flow development in HYDJET++ can be found in [16, 17, 31, 34].

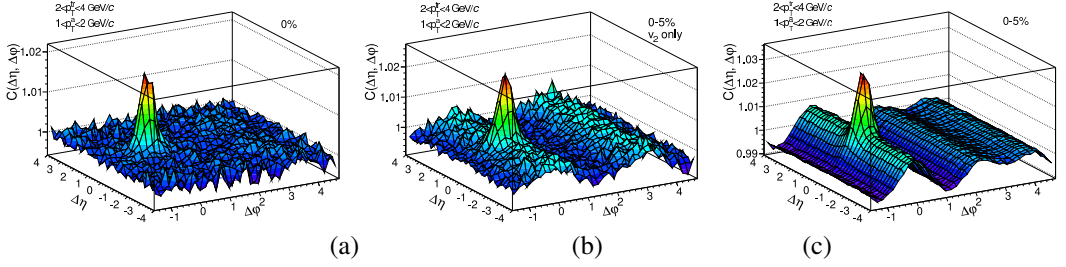


Figure 10. 2D correlation function in HYDJET++ in Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV for $2 < p_T^{\text{tr}} < 4$ GeV/c and $1 < p_T^{\text{a}} < 2$ GeV/c for (a) central collisions with impact parameter $b = 0$, (b) centrality 0-5% with only elliptic flow, and (c) centrality 0-5% with both elliptic and triangular flow present (from [38]).

6 Dihadron angular correlations: ridge

The two-particle correlations in the system may arise because of various interaction processes between particles and phase-space restrictions imposed by, e.g. energy-momentum conservation. The two-particle correlation function is typically defined as the ratio of pair distribution in the event to the combinatorial background of uncorrelated particles. In the flow dominated regime the pair angular distribution reads [cf. Eq.(1)]

$$\frac{dN^{\text{pairs}}}{d\Delta\varphi} \propto 1 + 2 \sum_{n=1}^{\infty} V_n(p_T^{\text{tr}}, p_T^{\text{a}}) \cos n(\Delta\varphi), \quad (9)$$

where $\Delta\varphi = \varphi^{\text{tr}} - \varphi^{\text{a}}$, and indices “tr” and “a” indicate the so-called “trigger” and “associated” particle, respectively. The study of angular dihadron correlations in relativistic heavy-ion collisions revealed the long-range correlations dubbed “ridge” [35]. Many interesting options have been proposed for the description of the ridge phenomenon, e.g. Cerenkov gluon radiation, Mach-cone of shock waves, etc. (see [36] and references herein). The authors of [37] suggested that the triangular flow should be important for understanding of ridge. HYDJET++ is ideally suited for such a check. - Although the model possesses many sources of particle correlations, for instance decays of resonances, femtoscopic correlations, jets, the long-range correlations in the model appear only because of the collective flow. The correlation function $C(\Delta\eta, \Delta\varphi)$ calculated in HYDJET++ for central lead-lead collisions at $\sqrt{s} = 2.76$ TeV is shown in Fig.10(a)-(c). In Fig.10(a) the centrality is 0% sharp, and both elliptic and triangular flows are absent. Just the distinct near-side ($\Delta\varphi \approx 0$) jet peak is seen, and no long range azimuthal correlations at the near-side or away-side ($\Delta\varphi \approx \pi$) are found. In Fig.10(b) the centrality is 0-5%, but the triangular flow is switched off. Here the long range correlations start to appear at both sides. However, only the presence of triangular flow in addition to the elliptic one [see Fig.10(c)] leads to development of ridge at near-side and, simultaneously, to formation of characteristic double-hump structure at the away-side, in full agreement with the experimental observations. Details of the study are presented in [38].

7 Conclusions

We show the importance of final state interactions and jets for the correct treatment of anisotropic flow harmonics in heavy-ion collisions at ultrarelativistic energies within the ideal hydrodynamic model. Jets account for (i) falloff of the flow harmonics in the range of intermediate transverse momenta, (ii)

changing of the mass ordering of the hadron elliptic flow, (iii) increase of the ratios $v_n^{1/n}(p_T)/v_2^{1/2}(p_T)$ of about 10-15% and formation of rising high- p_T tails in these ratios. Maybe, the most important result is that (iv) jets are responsible for the violation of the constituent quark scaling at energies of LHC and higher.

Decays of resonances (i) significantly enhance the elliptic and triangular flows of hadrons, (ii) make the $v_n(p_T)$ -distributions harder and (iii) push the particle spectra towards the NCQ-scaling fulfillment. Also, the interplay of v_2 and v_3 is studied in almost ideal conditions. We demonstrate that significant part of higher flow harmonics v_4, v_5, v_6 , etc. comes from the elliptic and triangular flows. Therefore, in order to investigate the genuine higher harmonics related to higher-order eccentricities one has to study more central events, where at least the elliptic flow is weak. Finally, the interplay between v_2 and v_3 is able to describe both qualitatively and quantitatively the long-range correlations, i.e. ridge at near-side and double-hump structure at the away-side. These phenomena deserve further investigations.

Acknowledgments

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References

- [1] J.-Y. Ollitrault, Phys. Rev. D **46**, 229 (1992)
- [2] X.-N. Wang and M. Gyulassy, Phys. Rev. Lett. **68**, 1480 (1992)
- [3] S. A. Voloshin and Y. Zhang, Z. Phys. C **70**, 665 (1996)
- [4] A. M. Poskanzer and S. A. Voloshin, Phys. Rev. C **58**, 1671 (1998)
- [5] S. A. Voloshin, A. M. Poskanzer, and R. Snellings, in *Relativistic Heavy Ion Physics*, Landolt-Börnstein Database Vol. 23, edited by R. Stock (Springer, Berlin, 2010), p.5–54.
- [6] M. Bleicher and H. Stöcker, Phys. Lett. B **526**, 309 (2002).
- [7] E. E. Zabrodin, C. Fuchs, L. V. Bravina, and Amand Faessler, Phys. Lett. B **508**, 184 (2001).
- [8] G. Bureau *et al.*, Phys. Rev. C **71**, 054905 (2005).
- [9] H. Song, S. A. Bass, and U. Heinz, Phys. Rev. C **83**, 024912 (2011).
- [10] B. Schenke, S. Jeon, and C. Gale, Phys. Rev. C **82**, 014903 (2010).
- [11] I. P. Lokhtin *et al.*, Comput. Phys. Commun. **180**, 779 (2009)
- [12] N. S. Amelin *et al.*, Phys. Rev. C **74**, 064901 (2006)
- [13] N. S. Amelin *et al.*, Phys. Rev. C **77**, 014903 (2008)
- [14] I. P. Lokhtin and A. M. Snigirev, Eur. Phys. J. C **46**, 211 (2006)
- [15] G. Torrieri *et al.*, Comput. Phys. Commun. **167**, 229 (2005)
- [16] L. V. Bravina *et al.*, Eur. Phys. J. C **74**, 2807 (2014)
- [17] L. V. Bravina *et al.*, Phys. Rev. C **89**, 024909 (2014)
- [18] I. P. Lokhtin *et al.*, Eur. Phys. J. C **72**, 2045 (2012)
- [19] T. Sjostrand, S. Mrenna, and P. Skands, JHEP **0605**, 026 (2006)
- [20] G. Eyyubova *et al.*, Phys. Rev. C **80**, 064907 (2009)
- [21] E. Zabrodin *et al.*, J. Phys. G. **37**, 094060 (2010)

- [22] J. Adams *et al.* (STAR Collaboration), Phys. Rev. Lett. **92**, 052302 (2004).
- [23] S. S. Adler *et al.* (PHENIX Collaboration), Phys. Rev. Lett. **91**, 182301 (2003).
- [24] F. Noferini *et al.* (ALICE Collaboration), Nucl. Phys. A **904-905**, 438c (2013)
- [25] L. Adamczyk *et al.* (STAR Collaboration), Phys. Rev. C **88**, 014902 (2013)
- [26] L. Bravina, B. H. Brushheim Johansson, G. Eyyubova, and E. Zabrodin, Phys. Rev. C **87**, 034901 (2013)
- [27] S. Chatrchyan, *et al.* (CMS Collaboration), Phys. Rev. C **87**, 014902 (2013)
- [28] J. Crkovska *et al.*, (these Proceedings)
- [29] N. Borghini and J.-Y. Ollitrault, Phys. Lett. B **642**, 227 (2006)
- [30] E. Zabrodin, G. Eyyubova, L. Malinina, and L. Bravina, Acta Phys. Polon. B **5**, 349 (2012)
- [31] B. H. Brushheim Johansson *et al.*, (these Proceedings)
- [32] D. Teaney and L. Yan, Phys. Rev. C **86**, 044908 (2012)
- [33] J. Jia *et al.* (ATLAS Collaboration), Nucl. Phys. A **910-911**, 276 (2013)
- [34] E. Zabrodin *et al.*, EPJ Web Confer. **71**, 00142 (2014)
- [35] A. Adare *et al.* (PHENIX Collaboration), Phys. Rev. C **78**, 014901 (2008);
M.M. Aggarwal *et al.* (STAR Collaboration), Phys. Rev. C **82**, 024912 (2010);
K. Aamodt *et al.* (ALICE Collaboration), Phys. Rev. Lett. **107**, 032301 (2011)
- [36] Proceedings of *Quark Matter 2008*, J. Phys. G **35**, 104001-104167 (2008)
- [37] B. Alver and G. Roland, Phys. Rev. C **81**, 054905 (2010) [Erratum-ibid. C **82**, 039903 (2010)]
- [38] G. Eyyubova *et al.*, arXiv:1411.4487 [hep-ph]