

## Search for $Z'$ , vacuum (in)stability and hints of high-energy structures

Elena Accomando<sup>1,\*</sup>, Claudio Corianò<sup>2,\*\*</sup>, Luigi Delle Rose<sup>1,3,\*\*\*</sup>, Juri Fiaschi<sup>1,\*\*\*\*</sup>, Carlo Marzo<sup>2,†</sup>, and Stefano Moretti<sup>1,‡</sup>

<sup>1</sup>*School of Physics and Astronomy, University of Southampton, Highfield, Southampton SO17 1BJ, UK*

<sup>2</sup>*Dipartimento di Matematica e Fisica Ennio De Giorgi, Università del Salento and INFN-Lecce, Via Arnesano, 73100 Lecce, IT*

<sup>3</sup>*Dept. of Particle Physics, Rutherford Appleton Laboratory, Chilton, Didcot, OX11 0QX, UK*

**Abstract.** We study the high-energy behaviour of a class of anomaly-free abelian extensions of the Standard Model. We focus on the interplay among the phenomenological characterisation of the model and the use of precise renormalisation group methods. Using as boundary conditions regions of the parameter space at the verge of current LHC probe, interesting unification patterns emerge linked to thresholds belonging to a  $SO(10)$  grand unification theory (GUT). We stress how the evolution of the mixing between the two abelian factors may provide a valuable tool to address the candidate high-energy embedding. The emerging unification scenarios are then challenged to be perturbative and to allow for a stable vacuum.

### 1 Introduction

An extra  $U(1)'$  gauge symmetry is a common presence in many attempts to go beyond the Standard Model (SM). It represents, from a low-energy perspective, the simplest extension that can be attached to the SM gauge group, at the same time, from the opposite high-energy point of view, an extra abelian factor is almost an unavoidable leftover from the breaking of many GUT scenarios [1].

If we adopt a (grand) unification paradigm, it is therefore feasible that a regime ruled by the gauge structure  $SU(3) \otimes SU(2) \otimes U(1)_Y \otimes U(1)'$  could populate the sequence of effective descriptions scaling from the GUT energy, before breaking into the SM one. The last step may be triggered by the non-trivial vacuum expectation of a scalar field  $\chi$ , that is, consequently, required to be SM-singlet. If such  $U(1)'$  breaking is realised at the TeV scale, then there are realistic prospects of an interesting interplay with the current LHC probe, the precise traits of such phenomenological characterisation being dictated by the extended matter content ([2–6]). Beyond the scalar sector, where a SM-singlet accounts for the extra  $U(1)'$  breaking, and the neutral vector  $Z'$ , to accomplish gauge invariance, one

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\*e-mail: e.accomando@soton.ac.uk

\*\*e-mail: claudio.coriano@le.infn.it

\*\*\*e-mail: l.delle-rose@soton.ac.uk

\*\*\*\*e-mail: juri.fiaschi@soton.ac.uk

†Speaker. e-mail: carlo.marzo@le.infn.it

‡e-mail: s.moretti@soton.ac.uk

extra fermion per generation is needed to cancel gauge and gravitational anomalies in a minimal way. This scenario has been the subject of a recent up-to-date investigation [7] where we exploited the bounds and the discovery potential of current and forthcoming collider searches. The more promising regions of the allowed parameter space have supplied the boundary conditions for a Next-to-Leading-Order (NLO) vacuum stability analysis, that we performed extrapolating the model to higher energies with two-loop  $\beta$  functions. As a result, the explored regions have been labeled with the maximal energy scale up to which they would provide a coherent (stable and perturbative) extrapolation of the model.

The role of the Renormalisation Group (RG) extrapolation does not exhaust its insight power with the stability analysis. As we will illustrate, for the particular case of our minimal  $SM \otimes U(1)'$  regime, the RG may draw clear indications also about the high-energy regime that is expected to take place. In a combined effort, all the phenomenological and formal aspects of this analysis will contribute to unveil a consistent link between the low-energy model characterisation, and a stable, perturbative, ultraviolet (UV) completion.

## 2 Structure of the model and constraints from current collider probe

The class of models encompassed in [7] adds, to the SM field content, a massive neutral gauge boson plus a scalar and three extra fermions, all transforming trivially under the SM gauge group. This extended spectrum is naturally introduced to minimally account for gauge invariance, anomaly freedom and the requirement of a massive  $Z'$ . We notice, as a valuable consequence of the previous setting, that the presence of a new abelian factor has forced the introduction of states that complete the 16-dimensional representation of  $SO(10)$  which is a further motivation to explore the possible UV fate of such model. Anomaly cancellation also rules the possible  $U(1)'$  charges, leaving to the ratio of just two parameters the definition of the allowed charge assignments. In a low-energy investigation the common choice is to highlight the Hypercharge operator  $Y$ , so that the generator of the extra  $U(1)'$  is constrained to the form  $Y' = (B - L) + (\tilde{g}/g'_1)Y$ , where  $B$  and  $L$  are, respectively, the Baryon and the Lepton number of the fields. The overall gauge strength  $g'_1$  and the *mixing*  $\tilde{g}$  rule, therefore, the content of the  $B - L$  and the Hypercharge operators in  $Y'$ .

The renormalisable interactions that arise from the extended field content can promptly realise a Type-I seesaw mechanism to account for neutrino masses. The SM Yukawa sector is in fact supplemented by the new contribution

$$\mathcal{L}' = -Y_\nu \bar{L} \tilde{H} \nu_R - Y_N \overline{(\nu_R)^c} \nu_R \chi \quad (1)$$

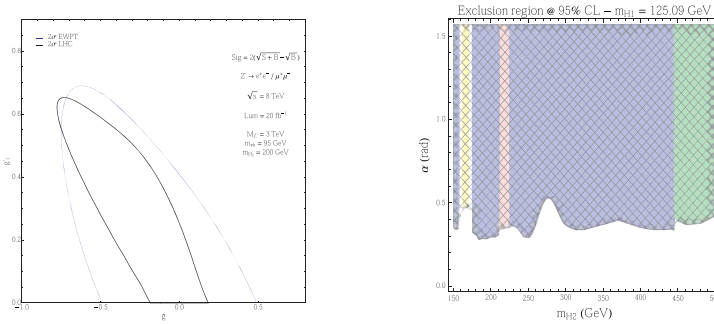
that, after the sequential breaking of the  $U(1)'$  and of the Electro-Weak (EW) symmetry itself, provides the wanted massive state with the typical seesaw hierarchy. The scalar sector, instead, is extended to the form

$$V(H, \chi) = m_1^2 H^\dagger H + m_2^2 \chi^\dagger \chi + \lambda_1 (H^\dagger H)^2 + \lambda_2 (\chi^\dagger \chi)^2 + \lambda_3 (H^\dagger H)(\chi^\dagger \chi) \quad (2)$$

where  $H$  is the Higgs doublet state.

It comes therefore with no surprise that, when the vacuum expectation value of  $\chi$  is at the TeV scale, the model has to deal with the exclusion limits from the more recent collider quest. In particular, the past investigations of the  $Z'$  have been strongly affected by bounds coming from EW Precision Tests (EWPTs) from LEP2. The first Run of LHC at 8 TeV and  $\mathcal{L} = 20 \text{ fb}^{-1}$  has generated even more stringent bounds at the TeV scale. These can be extracted using a signal-to-background analysis for the Drell-Yan channel. When translated in constraints in the extended  $(g'_1, \tilde{g})$  plane, the range of the allowed values is visible, for the exemplar case of  $M_{Z'} = 3 \text{ TeV}$ , from fig. 1(a). Also the extended

scalar sector creates numerous chances to reveal and characterise the class of models under study. We have limited the related new parameter space, that we parameterised with the new scalar mass  $m_{H_2}$  and the mixing angle  $\alpha$ , considering the bounds from the direct detection probes, and comparing the signal produced with the one measured of the discovered Higgs at 125.09 GeV. This analysis has been performed using, respectively, HiggsBounds [8] and HiggsSignals [9] tools, and has constrained the  $(m_{H_2}, \alpha)$  space to the regions of fig. 1(b).



**Figure 1.** (a) EWPTs and LHC bounds for the case  $M_{Z'} = 3$  TeV (b) Excluded region in the  $(m_{H_2}, \alpha)$  parameter space for  $m_{\nu_h} = 95$  GeV from HiggsBounds.

### 3 The kinetic mixing and the breaking of SO(10) thresholds

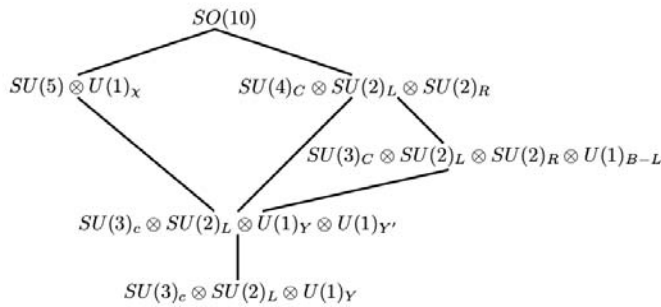
The presence of multiple abelian factors is a peculiar trait of this class of models. The induced kinetic mixing, absorbed in the contribution of the coupling  $\tilde{g}$  to the covariant derivative

$$\mathcal{D}_\mu = \partial_\mu + ig_1 Y B_\mu + i(\tilde{g} Y + g'_1 Y_{B-L})B'_\mu + \dots, \tag{3}$$

may shed light, supported by a precise RG inspection, on the UV embedding that precedes the  $U(1)'$  regime [10–12].

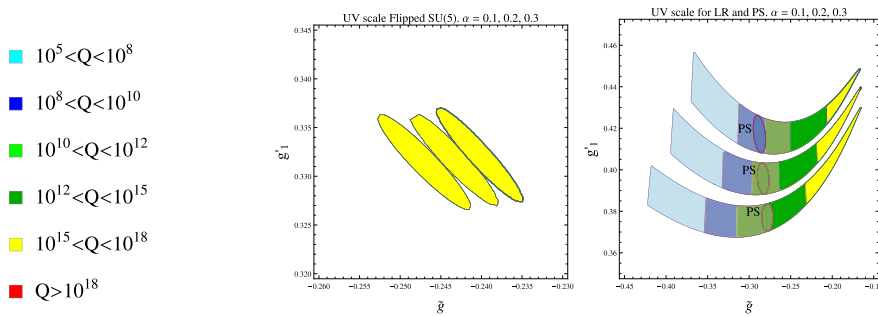
The key for this analysis is in the matching of the low and the high-energy generators basis, used to describe the abelian sector. In our phenomenological survey, adherence with the SM regime suggested the use of the Hypercharge for one of the two  $U(1)$ . In turn, within the constraints of anomaly cancellation, we chose B-L for the other. The mixing would then provide the component of the  $Y'$  generator in the Hypercharge direction. From a high-energy perspective is more appropriate to work with the basis that is naturally provided by the embedding of the abelian factors in the unifying group. For example, a Left-Right (LR) symmetric regime  $SU(2)_R \otimes U(1)_{B-L}$ , which includes  $U(1)_R \otimes U(1)_{B-L}$ , would select the corresponding  $Y_R$  and  $Y_{B-L}$  set of generators. Close to the energy scale of the Left-Right symmetry breaking, the mixing between the  $Y_R$  and  $Y_{B-L}$  is zero, being protected by the overall *non-abelian* gauge symmetry of  $SU(2)_R$ . It is possible, with the appropriate normalisation, to match our SM-oriented parameters  $(g_1, g'_1, \tilde{g})$  with the ones corresponding to the (candidate) high-energy basis  $(g_R, g_{B-L}, \tilde{g}_{R/B-L})$ . Therefore, following the RG evolution of  $\tilde{g}_{R/B-L}$  in terms of  $g_1, g'_1$  and  $\tilde{g}$ , we can recognise, by its zeroing at a given energy, the restoration of a Left-Right symmetry.

This analysis can be promptly extended to include thresholds of SO(10) that represent a realistic UV embedding. These involve, in addition to the Left-Right case discussed, a direct breaking of a Pati-Salam (PS) group into our model, and the flipped SU(5) case (fig 2). Choosing as boundary



**Figure 2.** The  $SO(10)$  breaking chart illustrating the chains investigated in this work. The cases for the Flipped  $SU(5)$  and Pati-Salam required also additional unification conditions involving the non-abelian gauge sector.

conditions, for the RG extrapolation, benchmarks points inspired by our phenomenological analysis, the parameter space offers regions that, in case of discovery, would clearly reveal the presence of one of the previous embeddings (fig. 3).



**Figure 3.** (a) When we consider the stability and perturbativity analysis, the colours refer to the different regions defined by the maximum energy up to which the model is stable and perturbative. The same energy/colour relation is also used for the unification study, referring to regions that fulfil the given unification requirement. (b) Regions with Flipped  $SU(5)$  restoration. (c) Regions with LR and PS restoration.

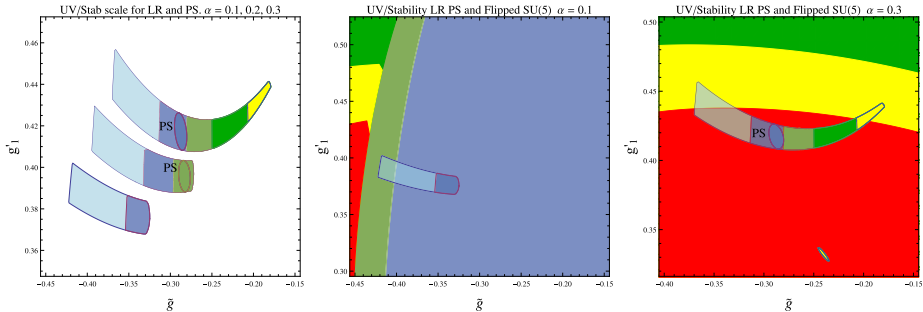
### 4 Vacuum stability and Unification patterns

The minimal character of this  $U(1)'$  extension of the SM makes particularly efficient the use of vacuum stability and perturbativity as constraining requirements to shape the viable parameter space [13–15]. The vacuum stability is addressed asking for the extended scalar potential to be bounded from below,

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad 4\lambda_1\lambda_2 - \lambda_3^2 > 0. \tag{4}$$

Together with the perturbativity requirement it is also challenges the viability of a given unification scenario. If we accept the minimal content of the model, then a coherent extrapolation asks for the maximum scale of stability and perturbativity to be greater than the one realising a succesful embedding. By relying on the analysis presented in [7], we may exploit this further constrains. Our

final results (fig. 4) give an illustration of how the interplay of the tools presented may enrich the forthcoming collider profiling of specific regions of the parameter space. Moreover, in a possible post-discovery phase, frictions with the measured scenarios would help in outlining the degrees of freedom necessary to recover stability, when a promising unification of the gauge sector is at hand.



**Figure 4.** (a) The effect of the stability requirement to the LR and PS restoration. The similar analysis for the Flipped  $SU(5)$  case would result trivially in the surviving only of the case with  $\alpha = 0.3$ . Explicit matching of the stability and perturbativity map with the unification regions. Case  $\alpha = 0.1$  (b) and  $\alpha = 0.3$  (c).

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