

## Future projects of light kaonic atom X-ray spectroscopy

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**Abstract.** X-ray spectroscopy of light kaonic atoms is a unique tool to provide precise information on the fundamental  $\bar{K}N$  interaction at the low-energy limit and the in-medium nuclear interaction of  $K^-$ . The future experiments of kaonic deuterium strong-interaction shift and width (SIDDHARTA-2 and J-PARC E57) can extract the isospin dependent  $K^-N$  interaction at threshold. The high-resolution X-ray spectroscopy of kaonic helium with microcalorimeters (J-PARC E62) has the possibility to solve the long-standing potential-strength problem of the attractive  $K^-$ -nucleus interaction. Here, the recent experimental results and the future projects of X-ray spectroscopy of light kaonic atoms are presented.

## 1 Introduction

The kaon is one of the pseudo-scalar mesons, the mass (495 MeV) lies between that of pion (140 MeV) and eta (510 MeV) mesons, and the anti-kaon  $\bar{K}$  ( $\bar{K}^0$  and  $K^-$ ) includes a strange quark ( $\bar{d}$ s and  $\bar{u}$ s). Therefore the anti-kaon is a unique and suitable particle to study the role of explicit chiral

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symmetry breaking due to the relatively heavier strange quark and the dynamics of low-energy QCD in the strangeness sector. The in-medium nuclear interaction of the  $K^-$  is also important to understand the structure of exotic nuclear states such as the  $\bar{K}N$  sub-threshold resonance  $\Lambda(1405)$ , the nuclear bound state of  $K^-$ , as well as the high density of matter in the universe (neutron stars).

The precise study of the  $\bar{K}N$  strong interaction has started from X-ray spectroscopy of kaonic atoms. The kaonic atom is a Coulomb-bound system of a  $K^-$ , electrons, and a nucleus. The transition X-ray energy is typically several keV for light kaonic atoms due to the  $K^-$ /electron mass ratio of  $\sim 1000$ . The  $\bar{K}N$  interaction is attractive at short range, thus the strong interaction effects appear on the atomic states as the perturbation; an energy shift from the QCD calculation and a life-time broadening due to nuclear absorption of  $K^-$ . The  $1s$ -state strong-interaction shifts and widths of kaonic hydrogen ( $K^-p$ ) and kaonic deuterium ( $K^-d$ ) can be used to directly extract the isospin dependent  $K^-N$  interaction at threshold by the Deser-Trueman type formula [1]. They are necessary for precise calculations of chiral SU(3) meson-baryon effective-field theory in low-energy QCD. Furthermore, the  $K^-N$  threshold information provides the basic constraint on the structure of the  $\Lambda(1405)$  [2, 3]. The X-ray spectroscopy of other kaonic atoms (helium to uranium) enables the study of the strong interaction of the  $K^-$  in dense nuclei. The bound state of a  $K^-$  in a nucleus has been predicted using the strongly attractive interaction [4], and recently the  $K^-$  multi-nucleon cluster system like  $K^-pp$  is one of the hot topics in this field.

Currently, the strong-interaction shifts and widths of kaonic atoms from hydrogen to uranium have been measured. The  $K^-p$  scattering length has been determined, and also the  $K^-$ -nucleus interaction is qualitatively understood. A systematic analysis with a phenomenological density-dependent optical potential can accurately describe the trend of shift and width of kaonic atoms and predict the deep potential depth ( $\text{Re}(V_0) \sim -180$  MeV) [5, 6]. In addition to that, a chiral SU(3) calculation which is based on the experimental data of the  $\bar{K}N$  interaction can also describe the experimental data of shifts and widths and predict the relatively shallow potential depth ( $\text{Re}(V_0) \sim -50$  MeV) [7]. This quantitative disagreement, so-called ‘deep-or-shallow problem’ is fundamentally correlated to the characteristic and structure of the  $K^-$  multi-nucleon cluster states. Hence, a more precise and decisive experimental measurement has been awaited.

We present here the key experiments and the future projects of light kaonic atom X-ray spectroscopy:

1. past and recent results of kaonic hydrogen  $2p \rightarrow 1s$  X-ray measurement by KEK-PS E228 [8], DEAR [9], and SIDDHARTA [10],
2. first measurement of kaonic deuterium  $2p \rightarrow 1s$  X-rays planned by the SIDDHARTA-2 [11] and the J-PARC E57 [12] groups,
3. high-resolution x-ray spectroscopy of kaonic helium-3 and helium-4 with superconducting transition-edge-sensors (TESs) by the HEATES and J-PARC E62 groups [13], which can solve the deep-or-shallow problem on the  $K^-$ -nucleus potential depth.

## 2 Kaonic hydrogen

The primary study of the  $\bar{K}N$  interaction based on the  $K^-p$  scattering experiments in the 1960s-1980s. The threshold information was extrapolated with the cross section data with large uncertainties. At that time, the precise measurement technique of kaonic hydrogen X-rays was not yet established; therefore even the sign of the  $\bar{K}N$  interaction (attractive or repulsive) was not determined. Later, the

kaonic hydrogen X-ray measurement with new background suppression technique and with new X-ray detectors was performed by three experimental groups. The details of experiments are shown in Table 1.

The reliable  $\bar{K}N$  threshold information was first provided in the 1990s. The KEK-PS E228 group measured the strong-interaction shift and width of  $K^-p$   $1s$  state at KEK-PS in Tsukuba, Japan [8]. The  $2p \rightarrow 1s$  X-ray energy is about 6.2 keV, and the strong interaction shift is  $\sim -300$  eV (repulsive) and the width is  $\sim 400$  eV. The  $K^-$  beam extracted through the K3 secondary beam line was slowed down with carbon degraders and stopped on the hydrogen gaseous target. They measured the X-rays with Si(Li) detectors installed inside of the target chamber and also tracked the coincident secondary charged particles generated from the reaction of  $K^-$  and nucleus with a cylindrical drift chamber system. The event selection of specific reaction modes and the timing selection of stopped  $K^-$  successfully reduced the synchronous background, and they clearly observed the clear peaks of  $K^-p$  X-rays. Though the background was small, the statistical uncertainties of the shift and width were large (see Table 1), because the energy resolution of the Si(Li) detectors was 360 eV full-width-at-half-maximum (FWHM) at 6 keV (this is relatively worse than recent silicon detectors of 150 eV FWHM). However, it was enough to determine the sign of the  $\bar{K}N$  interaction (attractive) and laid the basis of theory. The attractive  $\bar{K}N$  interaction led to the prediction of the deeply-bound  $K^-$  nuclear states [4]. The established event selection technique at the high intensity hadron beam line has been transitioned to other kaonic atom measurements at KEK and J-PARC in Tokai, Japan [12, 14].

In 2005, the DEAR group measured the strong-interaction shift and width of kaonic hydrogen at the DAΦNE positron-electron collider in Frascati, Italy [9]. DAΦNE produced almost at rest  $\phi(1020)$  mesons with 510 MeV  $e^+$  and  $e^-$  beams. The low kinetic energy  $K^-$ s from  $\phi \rightarrow K^+K^-$  decay were easily stopped in the gaseous target. They measured the  $K^-p$  X-rays with the CCD detectors with 180 eV FWHM energy resolution at 6 keV. Although the accumulated number of events was high, the background was also large due to no timing information of the CCDs. The background level of a lepton collider is usually lower than that of a hadron beam line. However, the signal-to-background ratio depends on the yield of the interesting event, and in the DEAR case, the  $K^-p$  X-ray yield is  $\sim 1\%$  per stopped kaon in the  $24 \rho_{\text{STP}}$  density hydrogen target ( $\rho_{\text{STP}}$  is the density at the standard temperature and pressure). They subtracted the large background and characteristic X-ray peaks of ion and manganese which were overlaid with the  $K^-p$  X-rays, and then determined the shift and width. After the DEAR result was published, the KEK-PS E228 and DEAR results suffered from theoretical ambiguities even with considering their experimental uncertainties [15].

The most precise and new results were provided by the SIDDHARTA group in 2011 at DAΦNE. They used newly developed silicon drift detectors (SDDs) with 150 eV FWHM energy resolution at 6 keV. They detected the decay charged kaons and created the hardware ‘kaon’ trigger. The trigger system and the sub-micro second timing resolution of SDDs successfully worked to reduce the background, and the significantly clear  $K^-p$  X-ray peaks were observed. One of the most remarkable things was the global analysis with  $K^-p$  and  $K^-d$  X-ray spectra. The measured X-ray spectrum with the deuterium target was useful to confirm the background shape and X-ray peaks of other kaonic atoms ( $K^-C$ ,  $K^-N$ ,  $K^-O$ , and  $K^-Al$ ), because the  $K^-d$  X-ray yield was under the background level. The precise  $K^-p$  scattering length of the SIDDHARTA results provided new basic constrains for the  $\bar{K}N$  interaction of chiral approach calculations (e.g., [3]).

### 3 Kaonic deuterium

The SIDDHARTA results of kaonic hydrogen give the strong constraint for the  $K^-p$  scattering length at the threshold. On the other hand, the calculation of  $K^-n$  scattering length (pure isospin=1 term) is

**Table 1.** Experimental details of kaonic hydrogen X-ray spectroscopy [8–10, 16], where  $\rho_{\text{STP}}$  is the density at the standard temperature and pressure,  $\Delta E_{\text{FWHM}}$  is the full-width-at-half-maximum energy resolution, and  $\Delta t_{\text{FWHM}}$  is the time resolution. The first error of shift and width is statistical and second one is systematic.

	KEK-PS E228 (1997)	DEAR (2005)	SIDDHARTA (2011)
Place	KEK-PS K3 (Japan)	DAΦNE (Italy)	DAΦNE (Italy)
H <sub>2</sub> gas density	10 $\rho_{\text{STP}}$	24 $\rho_{\text{STP}}$	15 $\rho_{\text{STP}}$
X-ray detector	Si(Li) 120 cm <sup>2</sup>	CCD 116 cm <sup>2</sup>	SDD 114 cm <sup>2</sup>
$\Delta E_{\text{FWHM}}$ at 6 keV	360 eV (beam off)	180 eV	150 eV
$\Delta t_{\text{FWHM}}$	290 ns	–	800 ns
1s shift (eV)	$-323 \pm 63 \pm 11$	$-193 \pm 37 \pm 6$	$-283 \pm 36 \pm 6$
1s width (eV)	$407 \pm 208 \pm 100$	$249 \pm 111 \pm 30$	$541 \pm 89 \pm 22$
$2p \rightarrow 1s$ X-ray yield	$1.5 \pm 0.5$ % / stopped $K^-$	–	$1.2_{-0.3}^{+0.4}$ % / stopped $K^-$

totally varied for theories [3]. To determine the isospin=1 term of the scattering length, the essential measurement of kaonic deuterium 1s-state strong-interaction shift and width has been awaited for a long time. There is no evidence of the  $K^-$ -d X-rays so far due to the low X-ray yield ( $\sim 10$  % of kaonic hydrogen) and the broad width (650–1000 eV predicted by theory) [17, 18]. In order to measure such a low-yield and broad X-ray peaks, a high-efficient and low-background measurement is required. Aimed at the first observation of the  $K^-$ -d X-rays, two experiments are planned at DAΦNE and J-PARC. Table 2 shows the expected parameters of the future experiments.

The SIDDHARTA-2 group plans to measure the  $K^-$ -d X-rays from a gaseous deuterium target at DAΦNE [11]. They improve the event selection efficiency and the background suppression. The efficiency of event selection is improved by a  $K^+$ -tag counter to identify the  $K^-$  from  $\phi \rightarrow K^+K^-$  decay. The synchronous background is suppressed by VETO counters to catch the coincident secondary charged particles generated from the  $K^-$ -nucleus reactions. They are also developing new SDDs (total 200 cm<sup>2</sup>) with 130 eV FWHM energy resolution at 6 keV and 400 ns timing resolution. Finally, these updates will achieve a 10-times higher signal-to-background ratio than the SIDDHARTA measurement.

The J-PARC E57 experiment will measure the  $K^-$ -d X-rays from a gaseous deuterium target at J-PARC [12]. They use the high-intensity  $K^-$  beam at the K1.8 BR beam line. The  $K^-$ -d X-rays are detected with new SDDs (total 246 cm<sup>2</sup>) with conjugation of a cylindrical drift chamber system. The background suppression by the event selections of stopped- $K^-$  and the  $K^-$ -d reaction modes will result in a comparable signal-to-background ratio of SIDDHARTA-2.

## 4 Kaonic helium

Helium is a nucleus and its nuclear density can be treated as a medium for the  $K^-$ . The kaonic helium ( $K^-$ -<sup>4</sup>He and  $K^-$ -<sup>3</sup>He) is one of the good probes to investigate the medium effect of the  $K^-$  and the exotic  $K^-$ -bound states in nuclei. While the direct information of the  $K^-$ -nucleus interaction could be extracted from the strong-interaction 1s-state shift and width of kaonic helium, the  $2p \rightarrow 1s$  X-ray has not been observed due to the low X-ray yield. This indicates that the  $K^-$  is most likely absorbed before the transition to the 1s state. Hence, the observable strong-interaction shift and width of kaonic helium are on the 2p state.

The kaonic helium 2p-state strong-interaction shift is predicted to be  $\sim 0$  eV, and the width to be a few eV by both the phenomenological ‘deep’ optical potential model [5, 6] and the chiral unitary ‘shallow’ potential model [7]. Recently, a possibility to solve the deep-or-shallow problem has been

**Table 2.** Expected experimental details of kaonic deuterium X-ray spectroscopy [11, 12].

	SIDDHARTA-2 (DAΦNE)	J-PARC E57 (K1.8 BR)
D <sub>2</sub> gas density	3 % of liquid D <sub>2</sub>	5 % of liquid D <sub>2</sub>
X-ray yield	0.1 % / stopped K <sup>-</sup>	0.1 % / stopped K <sup>-</sup>
X-ray detector	SDD 200 cm <sup>2</sup>	SDD 246 cm <sup>2</sup>
ΔE <sub>FWHM</sub> at 6 keV	130 eV	130 eV
Δt <sub>FWHM</sub>	400 ns	400 ns
Signal/BG	1/3	1/3
Precision 1s shift	±30 eV	±60 eV
Precision 1s width	±70 eV	±130 eV
Assumed 1s width	750 eV	800 eV
Feature	high geometrical efficiency, new trigger and VETO counters	high beam intensity, event selection with cylindrical drift chamber system

**Table 3.** Experimental results and details of kaonic helium X-ray spectroscopy [14, 19–22]. The first error of shift and width is statistical and second one is systematic.

	KEK-PS E570 (2007)	SIDDHARTA (2011)	J-PARC E62
Place	KEK-PS K5	DAΦNE	J-PARC K1.8 BR
Target	liquid <sup>4</sup> He	<sup>4</sup> He gas / <sup>3</sup> He gas	liquid <sup>4</sup> He / liquid <sup>3</sup> He
X-ray detector	SDD 8 cm <sup>2</sup>	SDD 144 cm <sup>2</sup>	240-pixel TES 23 mm <sup>2</sup>
ΔE <sub>FWHM</sub> at 6 keV	190 eV	150 eV	5 eV
Δt <sub>FWHM</sub>	380 ns	800 ns	1 μs
2p shift	+2 ± 2 ± 2 eV ( <sup>4</sup> He)	+5 ± 3 ± 4 eV ( <sup>4</sup> He) -2 ± 2 ± 4 eV ( <sup>3</sup> He)	goal ±0.2 eV ( <sup>4</sup> He- <sup>3</sup> He)
2p width	≤ 18 eV (90 % CL)	14 ± 8 ± 5 eV ( <sup>4</sup> He) 6 ± 6 ± 7 eV ( <sup>3</sup> He)	sensitive to determine

discussed with new theoretical calculations [23]. The *isotope shift* of K<sup>-</sup>-<sup>4</sup>He and K<sup>-</sup>-<sup>3</sup>He 2p states (the difference of two shifts) is calculated to be 0.6 eV for the deep potential [24] and 0.0 eV for the shallow one [25]. Therefore, the two models can be distinguished experimentally with the precision of 0.2 eV. On the other hand, the current best precision of the 2p-state shift is ±2 eV (stat.) ±2 eV (syst.) [14]. At least one order of magnitude higher precision is necessary to distinguish the predictions. In order to achieve such a high precision, new measurement technique and low noise X-ray detectors are needed.

The HEATES group has attempted to apply the superconducting TES microcalorimeters to high-resolution hadronic atom X-ray spectroscopy. The TES is an ideal detector to measure a thin X-ray line like kaonic helium 3d → 2p X-ray and to determine the X-ray energy precisely. According to the results of feasibility test experiment [26], the 240-pixel TES array (23 mm<sup>2</sup> effective area) has achieved 5 eV FWHM energy resolution at 6 keV with 1 μs time resolution, and they successfully measured the pionic carbon 4f → 3d X-ray energy with precision of ≤ 0.2 eV [27].

The J-PARC E62 group plans the measurement of both the K<sup>-</sup>-<sup>4</sup>He and K<sup>-</sup>-<sup>3</sup>He X-rays with the TESs at the J-PARC K1.8 BR beam line [13]. The successive measurement can minimize the systematic uncertainty of *isotope shift*, and it is free from the theoretical uncertainty associated with the error of charged kaon mass. The recent results and the future experiment of kaonic helium X-ray spectroscopy are summarized in Table 3.

## 5 Summary

The experimental results and the future projects of light kaonic atom spectroscopy are presented with the details of experimental methods.

The precise measurement of kaonic hydrogen X-rays by the SIDDHARTA group provided a unique possibility to determine the  $K^-p$  scattering lengths. This is one of the most important observables to investigate the chiral SU(3) dynamics in low-energy QCD. For further study of the isospin dependence of the  $K^-N$  interaction, the SIDDHARTA-2 and the J-PARC E57 groups plan the kaonic deuterium X-ray measurement with new SDDs. These measurements will provide constraints on the structure of the  $\Lambda(1405)$  and the  $K^-$  multi-nucleon clusters.

The long-standing problem of the optical potential depth of the  $K^-$ -nucleus interaction could be solved by the high-resolution kaonic helium X-ray measurement with superconducting microcalorimeters. The J-PARC E62 group plans the measurement of both the  $K^-^4\text{He}$  and  $K^-^3\text{He}$  X-rays with a 240-pixel TES array. The difference of  $2p$ -state strong-interaction shifts of  $K^-^4\text{He}$  and  $K^-^3\text{He}$  will be determined with the precision of 0.2 eV. The precise result can give a decisive settlement of the deep-or-shallow problem. This will be an important complement of the experimental direct search for the  $K^-$ -bound states in nuclei.

**Acknowledgments** We thank C. Capocchia, G. Corradi, B. Dulach, and D. Tagnani from LNF-INFN; and H. Schneider, L. Stohwasser, and D. Stütkler from Stefan-Meyer-Institut, for their fundamental contribution in designing and building the SIDDHARTA setup. We thank as well the DAΦNE staff for the excellent working conditions and permanent support. Part of this work was supported by the European Community-Research Infrastructure Integrating Activity “Study of Strongly Interacting Matter” (Hadron-Physics2, Grant Agreement No. 227431, and Hadron-Physics3 (HP3) Contract No. 283286) under the Seventh Framework Programme of EU; Hadron-Physics I3 FP6 European Community program, Contract No. RII3-CT-2004-506078; Austrian Science Fund (FWF) (P24756-N20); Austrian Federal Ministry of Science and Research BMBWK 650962/0001 VI/2/2009; Romanian National Authority for Scientific Research, Contract No. 2-CeX 06-11-11/2006; the Grant-in-Aid for Specially Promoted Research (20002003), MEXT, Japan; and the Croatian Science Foundation, under project HRZZ 1680.

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