

Numerical modelling of suffusion by discrete element method: a new internal stability criterion based on mechanical behaviour of eroded soil

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Abstract. Non-cohesive soils subjected to a flow may have a behavior in which fine particles migrate through the interstices of the solid skeleton formed by the large particles. This phenomenon is termed internal instability, internal erosion or suffusion, and can occur both in natural soil deposits and also in geotechnical structures such as dams, dikes or barrages. Internal instability of a granular material is its inability to prevent the loss of its fine particles under flow effect. It is geometrically possible if the fine particles can migrate through the pores of the coarse soil matrix and results in a change in its mechanical properties. In this work, we use the three-dimensional Particle Flow Code (PFC3D/DEM) to study the stability/instability of granular materials and their mechanical behavior. Kenney and Lau criterion sets a safe boundary for engineering design. However, it tends to identify stable soils as unstable ones. The effects of instability and erosion, simulated by clipping fine particles from the grading distribution, on the mechanical behaviour of glass ball samples were analysed. The mechanical properties of eroded samples, in which erosion is simulated and gives a new approach for internal stability. A proposal for a new internal stability criterion is established, it is deduced from the analysis of relations between the mechanical behaviour and internal stability, including material contractance.

1 Introduction

The construction of earth structures such as dams, levees and road embankments often requires the use of granular soils. These cohesionless granular media are often composed of two parts: a solid (coarse) skeleton that can support and transmit the external stresses, and fine particles that can move through the constrictions.

These granular soils can be internally stable or unstable, and more or less resistant to the phenomena of internal erosion and suffusion. These phenomena caused by seepage of water through the material affect its mechanical behaviour and may lead to its collapse.

In granular soils, suffusion may occur only when these three following conditions are satisfied: the fine particles are smaller than the size of constrictions formed by the coarse particles; fine particles do not fill the constrictions and are free to move; the hydraulic gradient is high enough. Kenney and Lau [1-2] proposed a criterion to assess the internal stability of granular media. This criterion is based on the assumption that each class of grain, characterized by its diameter d must be prevented to move by the grains whose diameter is comprised between d and $4d$.

This criterion consists in plotting the PSD curve of a soil in a diagram with the mass fraction F of particles whose

diameter is smaller than d on the X-axis and the mass fraction H of the particles whose diameter is comprised between d and $4d$ on the Y-axis. The soil is considered as stable if, for $F < 20$ or 30% , the curve obtained is located below the line $H = F$. Otherwise, if some portion of this curve passes above the line $H = F$, the soil is considered as unstable. According to Kenney and Lau [1-2], F values of 20% apply to the soils with widely graded primary fabric ($C_u > 3$) and the value of 30% to the soils with narrowly graded primary fabric ($C_u < 3$).

The mechanism of internal stability has also been widely studied by other authors [3-9], mainly in order to define criteria for soils likely to develop internal erosion.

Kézdi [4] proposed a criterion to assess the internal stability of soil based on the division of the grain size distribution curve into its coarser and finer components. Each component must satisfy the criterion $D'_{15} / D''_{85} = 4$ [5], where D'_{15} is the particle diameter of the filter corresponding to 15% of passing and D''_{85} is the particle diameter of the soil to be protected, corresponding to 85% of passing.

A unified approach combining the methods of Kézdi [4] and Kenney and Lau [1-2] was established by Li and Fannin [6]. The common feature of both methods is the examination of the slope of the gradation curve over a

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discrete interval of its length. This approach yielded a more reliable estimation of soil stability [7].

Internal instability has also been assessed by Andrianatrehina et al. [8]. The stability of nine samples with different grain size distribution curves, derived from direct grain size measurements carried out after triaxial and vibration tests was studied. The results were compared with the predictions of several methods [1, 4, 5, 9,10].

In the literature, many works have focused on the evaluation of the internal stability of materials, but few of them studied the change in the mechanical behaviour resulting from grain size distribution changes after flow.

The objective of this work is to establish a relationship between the internal stability parameters and the mechanical behaviour of materials. To achieve this, a Discrete Elements Method (DEM) is used to model soil sample submitted to a triaxial paths. A new criterion of internal stability taking into account the mechanical behaviour of soils is proposed.

2 Numerical modelling

This numerical study was performed with PFC 3D that uses the discrete element method (DEM) originally developed by Cundall and Strack [11, 12]. The DEM method is very suitable for numerical modelling of granular systems behaviour (granular soils; rocks...).

Materials are discretized in elements of simple shape (spheres) that interact with neighbouring contact elements.

A material is generated with a target granular distribution and porosity and then subjected to a triaxial test. Three stages were employed for the numerical specimen tests: (1) specimen preparation; (2) consolidation and (3) specimen shearing.

2.1 Numerical sample generation

The generation procedure of granular sample with a given grain size distribution curve and a given porosity developed by Abdoulaye Hama et al [13,14] is used.

2.2 Triaxial modelling

The triaxial test in PFC3D is performed by confining a cylindrical sample within three walls. The top and the bottom walls simulate loading platens and the lateral one simulates the confining pressure experienced by the sample sides. The void volume can be calculated using the total volume of the sample minus the total volume of the solid particles.

The axial strain can be calculated by the following equation (which can be obtained by a combination of the Eulerian and Lagrangian strains):

$$\varepsilon = \frac{H_1 - H_0}{\frac{1}{2}(H_1 + H_0)} \quad [1]$$

Where H_0 is the initial height of the sample and H_1 is the current height during the test.

The tridimensional particle flow determines the wall stress and adjusts the wall velocity to reduce the difference between the current wall stress and the target wall stress σ^w , σ^t . The wall velocity \dot{u}^w must satisfy:

$$\dot{u}^w = G(\sigma^w - \sigma^t) = G\Delta\sigma \quad [2]$$

Where G is the “gain” parameter that is estimated by:

$$G = \frac{\alpha A}{k_n^w \Delta t} \quad [3]$$

3 Results and discussion

When it occurs in a soil sample the phenomenon of suffusion, its PSD changes and this affects its internal stability. To study the impacts of suffusion on the mechanical behaviour of granular soils, five PSD identified by S1; S2; S3; S4 and S5 were defined from an alluvial deposit from the Rhône River in France [14]. Table 1 summarises the Characteristics of these samples.

Table 1: Characteristics of different samples

Material	S1	S2	S3	S4	S5
D10 (mm)	0.56	1.01	1.26	1.29	7.61
D30 (mm)	1.62	2.31	3.52	2.50	6.5
D50 (mm)	2.70	8.00	5.87	7.61	8.00
D60 (mm)	3.25	6.15	5.85	6.20	6.3
CU= d60/d10	5.8	6.08	4.64	4.80	0.82
CC= d30/d60*d10	0.89	0.37	0.47	0.31	0.13
Porosity n (%)	40	40	40	40	40
Minimum ratio of stability $(H/F)_{\min}$	1.85	2.47	3.87	3.38	0
Maximum coefficient of retention $(D_{15}/d_{85})_{\max}$.	15.5	1.95	2.20	2.31	3.24

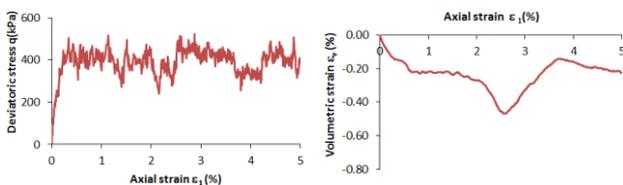
Table 1 shows that the only differences between samples are geometric. Samples PSD are all widely graded ($C_u > 3$) with slight curvature. They have different minimum stability index and different maximum retention coefficient. We interpret this as a consequence of the phenomenon of suffusion. If it occurs, it causes loss or gain of particles. From the internal stability parameters ($(H/F)_{\min}$; $(D_{15}/d_{85})_{\max}$.) the samples are classified according to the Kenney and Lau and Kezdi criteria. Samples internal stability state is presented on Table 2. One can note that the two criteria diverge on samples S1 and S5.

Table 2: Samples classification according to the Kenney and Lau and Kezdi criteria

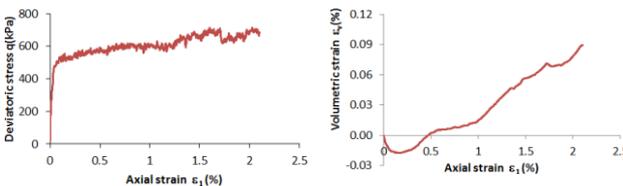
Material	S1	S2	S3	S4	S5
Kenney & Lau (1985-1986)	S	S	S	S	U
Kezdi (1979)	U	S	S	S	S
S stands for "Stable" and U for "Unstable"					

3.1. Triaxial results

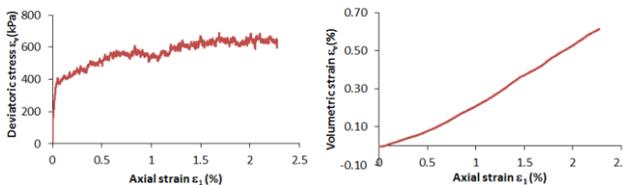
Each sample was subjected to a consolidated and drained triaxial test simulation, at same initial void ratio of $e=0.66$ and constant confining stress $\sigma_3=200$ kPa. Results are presented in the deviatoric (ϵ_1 ; q/p) and the volume change (ϵ_1 , ϵ_v) planes (Fig 1). They are used to calculate the stress ratio $(q/p)_{max}$ and the maximum contractancy (ϵ_{vmax}) corresponding at projection of the characteristic point in the (ϵ_1 ; q/p) plane.



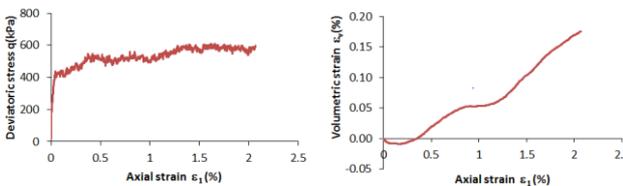
S1: $(H/F)_{min} = 1.85$; $(D_{15}/d_{85})_{max} = 15.5$



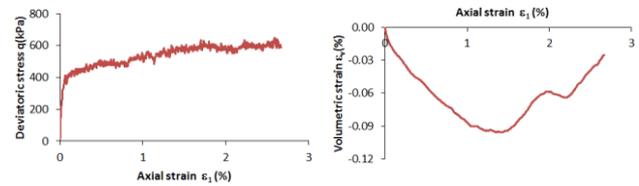
S2: $(H/F)_{min} = 2.47$; $(D_{15}/d_{85})_{max} = 1.95$



S3: $(H/F)_{min} = 3.87$; $(D_{15}/d_{85})_{max} = 2.20$



S4: $(H/F)_{min} = 3.38$; $(D_{15}/d_{85})_{max} = 2.31$



S5: $(H/F)_{min} = 0$; $(D_{15}/d_{85})_{max} = 3.24$

Fig 1: Triaxial results

Despite the identical test conditions, samples exhibit different maximum shear strength and different maximum contractancy (Fig 1). Table 3 showed a comparison between mechanical parameters $(q/p)_{max}$ and ϵ_{vmax} and internal stability ones $((H/F)_{min}; (D_{15}/d_{85})_{max})$.

Table 3: Comparison of mechanical and internal stability parameters

Material	S1	S2	S3	S4	S5
$(H/F)_{min}$	1.85	2.47	3.87	3.38	0
$(D_{15}/d_{85})_{max}$	15.5	1.95	2.20	2.31	3.24
$(q/p)_{max}$	1.42	1.6	1.6	1.51	1.4
$\epsilon_{vmax}(\%)$	0.5	0.02	0	0.01	0.9

It is noted that the parameters of internal stability influence the mechanical behaviour of soil samples (Table 3). Samples with higher deviatoric stress and lower contractancy present a minimum ratio of stability higher than their maximum coefficient of retention: $(H/F)_{min} > (D_{15}/d_{85})_{max}$.

3.2 Proposition of a new stability criterion

Internal instability of a granular material is its inability to prevent the loss of its fine particles under flow effect. It is geometrically possible if the fine particles can migrate through the pores of the coarse soil matrix and results in a change in its mechanical properties.

From relationship $(H/F)_{min} > (D_{15}/d_{85})_{max}$, we propose a new criterion for assessing soil internal stability. It takes account mechanical behaviour and classifies stable sample with $H/F > D_{15}/d_{85}$. Fig 2 shows the classification of our samples according the proposed criterion. Samples S2, S3 and S4 are stable and S1 and S5 are unstable.

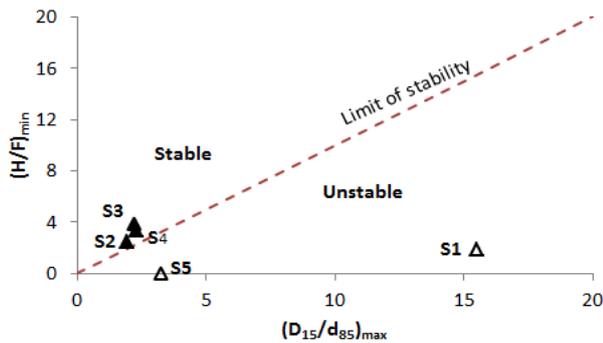


Fig 2: Proposed criterion

4 Validation of proposed criterion

To validate our criterion, 16 samples were taken from literature results: 4 from Kenney and Lau [3], 8 from Andrianatrehina et al [8], and 4 from Indraratna et al [10]. The choice of these samples is motivated by the diversity of their density and that of the analysis method of the authors. These 16 samples are classified using the proposed criterion. Fig 3 presents this classification and compares it with experimental result.

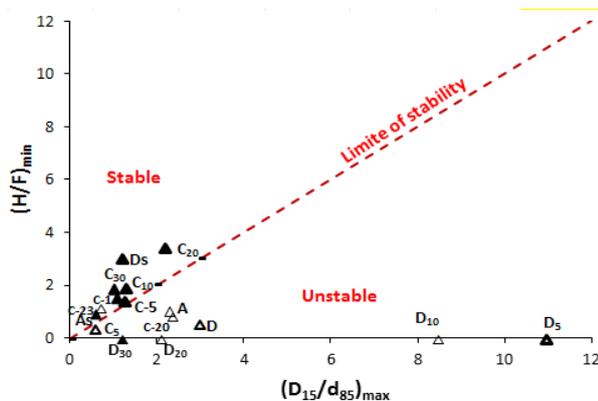


Fig 3: Validation of proposed criterion with literature results. ‘Hollow triangle’ means experimentally unstable
‘Full triangle’ means experimentally stable

5 Conclusions

Discrete elements method is used to model sand samples and to simulate their mechanical behaviour on triaxial paths. Consolidated and drained triaxial test simulation carried out at same initial void ratio and confinement stress. The maximum values of contractancy in $(\varepsilon_1; \varepsilon_v)$ plane and the maximum deviatoric stress in the $(\varepsilon_1; q/p)$ plane have been determined for each sample. Results showed that mechanical behaviour of granular material is influenced by the stability parameters $(H/F)_{\min}$ and $(D_{15}/d_{85})_{\max}$. Effects of suffusion on soil mechanical behaviour was analysed and a new internal stability criterion was proposed. Contrary to classical criteria, it takes into account the mechanical behaviour of the soil. It classifies as stable particle sizes distribution with $\frac{H}{F} \geq \frac{D_{15}}{d_{85}}$, corresponding to the better mechanical behaviour.

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