Abstract. \(\omega\) Centauri (NGC 5139) contains many variable stars of different types, including the pulsating type II Cepheids, RR Lyrae and SX Phoenicis stars. We carried out a deep, wide-field, near-infrared (IR) variability survey of \(\omega\) Cen, using the VISTA telescope. We assembled an unprecedented homogeneous and complete \(J\) and \(K_S\) near-IR catalog of variable stars in the field of \(\omega\) Cen. In this paper we compare optical and near-IR light curves of RR Lyrae stars, emphasizing the main differences. Moreover, we discuss the ability of near-IR observations to detect SX Phoenicis stars given the fact that the amplitudes are much smaller in these bands compared to the optical. Finally, we consider the case in which all the pulsating stars in the three different variability types follow a single period-luminosity relation in the near-IR bands.

1 Introduction

In the near-infrared (IR) bands, the study of variable stars has some advantages compared to the optical: i) the period-luminosity (PL) relations have lower internal dispersions ([3, 10]), leading to more precise distance determinations; ii) the interstellar extinction is lower (for the \(K_S\) band, the extinction is one tenth of the extinction in the \(V\) band); and iii) pulsating stars tend to have smaller amplitudes, leading to better constrained mean magnitudes with a smaller number of epochs.

Despite these advantages, only a handful of wide-field time-series surveys are devoted to near-IR bands. Two ongoing near-IR variability surveys are the Vista Variables in the Vía Láctea (VVV) ESO Public Survey, which acquired time-resolved data (in the \(K_S\) band) in highly extinct regions of
the Galaxy, at low Galactic latitudes (see, e.g., [4, 15]), and the VISTA survey of the Magellanic Cloud system (VMC; e.g., [6, 19, 20]). A detailed review of the time-series surveys in the near-IR is presented by [14] in these proceedings.

In this present scenario, $\omega$ Centauri (NGC 5139) is an excellent laboratory to study pulsation properties in the near-IR bands since it hosts a large and rich variable star content, previously well studied using optical observations. In particular, the cluster has at least 180 RR Lyrae (RRL) stars ([16]); 74 SX Phoenicis (SX Phe), the greatest number found in a globular cluster ([18, 26]); and seven type II Cepheids (T2Cs), among others variability types.

2 Observations

Near-IR images of $\omega$ Cen were taken using the VISTA 4.1m telescope, at ESO Paranal Observatory [8]. 42 and 100 images in $J$ and $K_S$, respectively, were collected. The details of the observations and data reduction have been previously explained in [16]. Point-spread function (PSF) photometry was derived using the DAOPHOT II/ALLFRAME package ([24, 25]) for the innermost ten arcminutes region of the cluster, while the DoPhot package ([1, 22]) was preferred to derive PSF photometry in the outer regions.

From the observations, the intensity-average mean magnitudes for 278 previously known pulsating stars were recovered. Of them, the variability (i.e., sinusoidal light curve for the given period) was recovered for 209 pulsating stars. The 69 stars previously known to be variables ([11, 26]), but without signs of variability in the near-IR, include a subsample of low-amplitude, c-type RRL (RRc) stars, in addition to most of the SX Phe stars that are known to be present in the cluster field.

3 Near-IR and visible light curves of $\omega$ Cen RR Lyrae stars

Considering the extensive optical study of variable stars in the cluster by [11], the amplitudes and light curve shapes in $V$ and the near-IR bands $J$ and $K_S$ can be directly compared. Figure 1 shows the light curves in $V$ (top), $J$ (middle) and $K_S$ (bottom) for one ab-type RRL (RRab, left) and one RRc star (right). The light curves in $V$ are from the study of [11]. Each panel shows, at the top right, the number of epochs in each light curve. From the figure, some striking differences can be noticed. First of all, the Blazhko effect that is evident in the $V$-band light curve of the RRab variable (V5, upper left panel) is not distinguishable in the near-IR light curves. This is the case for all the known Blazhko RRab stars in the cluster ([16]). Even though the resulting amplitude modulation is too small to be recovered in our near-IR light curves, [23] reported increased scatter in their near-IR light curves of RR Lyr, which they attributed to the Blazhko effect. Second, the amplitudes in $J$ and $K_S$ are smaller than in the $V$ band. [16] provide relations to convert between $V$, $J$ and $K_S$ magnitudes for RRL stars, and the decrease in the amplitudes from the visual to the IR is evident in their Figure 3. Finally, the light curve shape of RRab stars tends to be more sinusoidal as the light curve is observed with redder filters. The same effect is seen for RRc stars but the difference is less prominent, given their already nearly sinusoidal $V$-band light curves. The different light curve shapes, as one moves from the visual regime to the near-IR, can be understood largely in terms of the reduced dependence of the emerging flux on the star’s temperature variations, as compared to the radius ([5], and references therein). The lack of distinctive features in the light curves is one of the difficulties facing the automated classification of variable stars in the near-IR (see, e.g., [2, 7]).

4 Variability amplitudes of SX Phoenicis stars

SX Phe stars typically have smaller variability amplitudes than RRL and T2Cs, and are thus more difficult to detect. $\omega$ Cen hosts 74 SX Phe, of which more than 45 have $V$-band amplitudes $\leq 0.1$ mag.
Using the $J$ and $K_S$ time series, the variability of only 12 of these SX Phe could be recovered. These 12 stars have the highest $V$-amplitudes among all the SX Phe in the cluster, from 0.13 up to 0.31 mag (based on the minimum and maximum magnitudes reported by [11]). For the remaining SX Phe stars, the variability amplitudes are too small and, therefore, the light curves look indistinguishable from those of non-variable stars.

The amplitude distribution in $V$, $J$, and $K_S$ for the SX Phe stars with recovered variability in the near-IR is shown in Figure 2. In this figure, and also in Figure 3, we include only those 7 stars for which we were able to retrieve the corresponding $V$-band data (from [11]). For these 7 stars, we re-derived the $V$-band amplitudes in a manner consistent with the technique that was used to obtain the near-IR amplitudes. As can be seen, most of the amplitudes in $J$ tend to be $\lesssim 0.22$ mag, while their respective $K_S$ amplitudes are $\lesssim 0.15$ mag. These small amplitude values make the detection of SX Phe stars on the basis solely of near-IR observations harder. Only high-amplitude pulsators are likely to be found, at least at the magnitude level of $K_S \sim 16$ mag. This group of SX Phe pulsators corresponds to a small fraction of the distribution of amplitudes found for this variability type (see, e.g., [21]). Efforts have been made to collect near-IR light curves for SX Phe stars in the field as well as in some clusters (see, e.g., [2]), again recovering only high-amplitude pulsators.

A comparison between the resulting $A_V$, $A_J$, $A_{K_S}$ values is shown in Figure 3. The lines overplotted on this diagram correspond to best-fit relations of the following forms:

$$A_J = (0.29 \pm 0.08) \left[ 1 - \exp^{(-1.95\pm0.81)A_V} \right],$$  \hspace{1cm} (1a)

$$A_{K_S} = (0.20 \pm 0.06) \left[ 1 - \exp^{(-1.74\pm0.76)A_V} \right],$$  \hspace{1cm} (1b)

which are valid for visual amplitudes in the range $A_V < 0.75$ mag.
Figure 2. Distribution of amplitudes for those SX Phe stars for which the variability was recovered in the near-IR observations and for which we were able to retrieve $V$-band light curves (from [11]) and thus measure amplitudes following the same procedure as for the near-IR light curves. From left to right, the amplitudes in $V$, $J$ and $K_S$ bands are presented. The decrease in amplitude is evident when observing in IR bands.

Figure 3. Relationship between visual and near-IR amplitudes for SX Phe stars in $\omega$ Cen. The sample is the same as used in Figure 2. $J$-band values are shown as blue circles, whereas those in the $K_S$ band are displayed as red squares. The corresponding best-fitting relations (Eqs. 1a and 1b) are shown as dotted and dashed lines, respectively.

5 Near-IR period-luminosity relations

It has been suggested that the PL relations for T2Cs and RRL can be seen as a single relation, with nearly the same slope and zero points, at least in the near-IR, extending from periods shorter than 1 day up to $\sim 30$ days (see, e.g., [9, 13, 17]). At least to first order, this may plausibly also extend to the SX Phe regime (e.g., [5, 12], and references therein). Here we revisit this possibility, using our sample of T2Cs, RRab and (candidate) fundamental-mode SX Phe stars from [17].

The left panels of Figure 4 show the log ($P$) (in days) and extinction-corrected $J$ (top) and $K_S$ (bottom) magnitudes and the least-squares fit recovered from the data (dashed lines). Despite the fact that the data largely conform to a straight line, resembling a single PL relation for all the aforementioned variability types, small differences are found, mostly in the longest- and shortest-period regimes. In the right panels of the figure, the difference between the observed $J$ and $K_S$ magnitudes (top and bottom panels, respectively) and the best fit to the data is presented. It is clear that the SX Phe stars tend to deviate the most from the relation, suggesting a non-negligible difference in slope between their PL relation and the one for RRL stars. The same is found for the longest-period T2Cs (W Virginis and RV Tauri sub-types). RRab stars present very small deviations from the fit ($\lesssim 0.1$ mag), in spite of the fact that its well-known metallicity dependence ([17]) was not corrected for when producing this plot.
Table 1. PL relations in different bandpasses.\(^1\)

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<th>(b_J)</th>
<th>(c_J)</th>
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<td>(-0.86 \pm 0.06)</td>
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<td>RRL</td>
<td>(-1.77 \pm 0.06)</td>
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<td>(-0.63 \pm 0.08)</td>
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<td>(-0.77 \pm 0.01)</td>
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<td>0</td>
<td>(-1.12 \pm 0.01)</td>
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</table>

\(^1\) In the form \(m_X = a_X \log (P) + b_X [\text{Fe/H}] + c_X\), where \(X\) corresponds to the bandpass.
\(^2\) Adopting \((m - M)_0 = 13.708\) mag for \(\omega\) Cen (from [17]).

Figure 4. Left: Extinction-corrected magnitudes in \(J\) (top) and \(K_S\) (bottom) versus \(\log (P)\), in days, for T2Cs, RRab and (candidate) fundamental-mode SX Phe stars. The dashed lines correspond to the linear least-squares fit to the data. The three variability types seem to follow, roughly, a single PL relation. Right: Difference between the observed extinction-corrected magnitudes and the derived fits, as a function of the logarithm of the period (in days). The horizontal dashed lines mark a zero-magnitude difference.

The slopes of the fits can be compared with the recently derived PL and PL−\(Z\) relations for SX Phe and RRL stars, respectively, as obtained by [17] using the same data. For T2Cs, no such relations were derived, since the cluster hosts only seven such stars. Table 1 shows the coefficients of the PL relations for the different variability types (from [13] and [17]), as well as the slopes derived in this paper simultaneously using the three variability types and when only T2Cs and RRL are considered. There is much better agreement among the different slope values when SX Phe stars are excluded from the fits. This was already evident from Figure 4 in which SX Phe stars are those with the highest deviations from the fit. Reassuringly, the slope values are closer when the \(K_S\) band is considered, suggesting that in fact T2Cs and RRL could indeed share a common PL relation, at least in this bandpass.
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References

[12] Majaess, D. J., JAAVSO, 38, 100