Three-dimensional Monte Carlo calculation of some nuclear parameters

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Abstract. In this study, a fusion-fission hybrid reactor system was designed by using 9Cr2WVTa Ferritic steel structural material and the molten salt-heavy metal mixtures 99–95% Li$_2$OSn$_8$O + 1-5% RG-Pu, 99–95% Li$_2$OSn$_8$O + 1-5% RG-PuF$_4$, and 99–95% Li$_2$OSn$_8$O + 1-5% RG-PuO$_2$, as fluids. The fluids were used in the liquid first wall, blanket and shield zones of a fusion–fission hybrid reactor system. Beryllium (Be) zone with the width of 3 cm was used for the neutron multiplication between the liquid first wall and blanket. This study analyzes the nuclear parameters such as tritium breeding ratio ($TBR$), energy multiplication factor ($M$), heat deposition rate, fission reaction rate in liquid first wall, blanket and shield zones and investigates effects of reactor grade Pu content in the designed system on these nuclear parameters. Three-dimensional analyses were performed by using the Monte Carlo code MCNPX-2.7.0 and nuclear data library ENDF/B-VII.0.

1 Introduction

The fuels used in hybrid reactor systems are generally deuterium–tritium (D-T) or deuterium–deuterium (D-D) fuels. When D-T fuel enters the fusion reaction, 14.1 MeV fusion neutrons and 3.5 MeV alpha particles are released. The plasma is surrounded by a wall made of fertile material, which cannot undergo the fusion reaction with thermal neutrons, but can undergo conversion with high energy neutrons, such as the 14.1 MeV neutrons produced by the fusion reaction. Thus, the high energy fusion neutrons convert fertile materials to fissile fuel, fission neutrons, and produce energy. The hybrid reactor produces 30 times more nuclear fuel per nuclear energy quantity than fast reactors [1-6].

In this study, a hybrid reactor system was designed. The hybrid reactor system can generate secure energy in large quantities with D-T fuel usage and subcritical study. Furthermore, it enables the production of a self-sufficient fuel for the reactor through the reaction of the neutrons released by the plasma. Reactor-grade (RG) plutonium is found in spent nuclear fuel. Isotopic distribution of RG-Pu has composition 1% $^{238}$Pu, 62% $^{239}$Pu, 24% $^{240}$Pu, 8% $^{241}$Pu and 5% $^{242}$Pu [7]. The reactor-grade Pu in present nuclear power stations as fuel can use to reduce the trans-uranium content of spent nuclear fuel. In this study, radioactive materials with a plutonium additive were used in the hybrid reactor system to reduce the amount of reactor grade Pu used.

2 Method

2.1 Numerical Calculations

Hybrid reactor system used in the study is in the shape of a torus. The radial structure of designed the hybrid reactor system is shown in Table 1. Calculation of all the parameters of the fission and fusion reactors and other areas of nuclear technology depend on the cross-section data. The data of the ENDF/B-VII libraries are very important for theoretical calculations [8-10]. Analysis was performed for neutron wall loading 10 MW/m$^2$ and fusion power 4000 MW.

Table 1. The radial build of the hybrid reactor system design

<table>
<thead>
<tr>
<th>Inboard side</th>
<th>Outboard side</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zone</td>
<td>r (cm)</td>
</tr>
<tr>
<td>SS316LN</td>
<td>276</td>
</tr>
<tr>
<td>Vacuum vessel$^*$</td>
<td>278</td>
</tr>
<tr>
<td>SS316LN</td>
<td>294</td>
</tr>
<tr>
<td>GAP</td>
<td>296</td>
</tr>
<tr>
<td>Shield$^b$</td>
<td>301</td>
</tr>
<tr>
<td>Ferritic Steel$^c$</td>
<td>350</td>
</tr>
<tr>
<td>Blanket$^d$</td>
<td>354</td>
</tr>
<tr>
<td>Be$^e$</td>
<td>404</td>
</tr>
<tr>
<td>Liquid First Wall$^a$</td>
<td>407</td>
</tr>
<tr>
<td>SOL</td>
<td>409</td>
</tr>
<tr>
<td>Plasma</td>
<td>437</td>
</tr>
</tbody>
</table>

$^*$ 80% SS316LN, 20% H$_2$O
$^a$ 80% SS316LN, 20% H$_2$O
$^b$ 60% 9Cr2WVTa, 40% (99–95% Li$_2$OSn$_8$O-1-5% RG-Pu, 99-95% Li$_2$OSn$_8$O-1-5% RG-PuF$_4$, 99-95% Li$_2$OSn$_8$O-1-5% RG-PuO$_2$)
$^c$ 100% 9Cr2WVTa
$^d$ 99-95% Li$_2$OSn$_8$O-1-5% RG-Pu, 99-95% Li$_2$OSn$_8$O-1-5% RG-PuF$_4$, 99-95% Li$_2$OSn$_8$O-1-5% RG-PuO$_2$
$^e$ 100% Be

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breed the tritium it requires [11,12]. Tritium is bred through the reaction of lithium with neutrons. The $^{6}\text{Li}(n,\alpha)^{T}$ reaction is produced with thermal neutrons, and the $^{7}\text{Li}(n,\alpha)n$/$^{T}$ reaction with fast neutrons. In the hybrid reactor system, the working liquid must be a lithium-containing medium to provide adequate tritium so that the plasma is self-sustaining and the fusion is a renewable energy source. The required TBR for a fission reactor conceptual design must be 1.1 [11-15].

The TBR can be given as follows:

$$TBR = T_6 + T_7$$

$$T_6 = \int \int F \cdot \Sigma (n,\alpha)^T dE dV, \text{for } ^{6}\text{Li}$$

$$T_7 = \int \int F \cdot \Sigma (n,n'\alpha)^T dE dV, \text{for } ^{7}\text{Li}.$$  

In this study, Li$_{20}$Sn$_{80}$ molten salt was used, which has low melting temperatures and low vapor pressure, to acquire sufficient tritium breeding.

### 2.3 Energy Multiplication Factor, Heat Deposition Rate and Fission Reaction Rate

The energy multiplication factor $M$ is the ratio of nuclear heating and source neutron energy incident on the first wall [16]. The energy produced must exceed the energy produced by the plasma. To obtain high thermal power, the $M$ value should be as large as possible. It is desirable that $M$ is greater than 1.2 in a D-T fueled reactor [17]. $M$ can be defined as follows:

$$M = [(200\times(\Phi \cdot \Sigma_f)+4.784\times T_6-2.467\times T_7)/14.1]+1$$

$$\Phi \cdot \Sigma_f = \int \int \Phi \cdot \Sigma_f dE dV, \text{total fission rate}.$$  

The contributions of the neutron flux, fission, and other reactions to the integrated $M$ and heat deposition rate are very important. The main contributions to the integrated $M$ and heat deposition rate are from the neutron flux, the fission reaction of plutonium isotopes, and the exothermic $^{6}\text{Li}(n,\alpha)^{T}$ reaction of Li$_{20}$Sn$_{80}$ molten salt.

### 3 Numerical Results

In this study, the fluids were composed of molten salt Li$_{20}$Sn$_{80}$ as the main constituent with increased mole fractions of heavy metals, 1-5% RG-Pu, RG-PuF$_4$, RG-PuO$_2$. The fluids used in order to decrease amount of reactor grade Pu were used in the liquid first wall, blanket and shield zones of hybrid reactor system.

Fig. 1 shows the TBR in the liquid first wall, blanket and shield regions per fusion source neutron for the various mixture compositions of molten salt and heavy metals. The increasing heavy metals contents means decreasing the Li that produces tritium. In Fig. 1, the TBR decreases due to decreasing the Li that produces tritium with an increase in the heavy metals contents.

Fig. 2 and Fig. 3 shows the energy multiplication factor $M$ and the heat deposition rate in the liquid first wall, blanket and shield regions per fusion source neutron for the various mixture compositions of molten salt and heavy metals. In Fig. 2 and Fig. 3, it was found...
that M and the heat deposition rate increases linearly for 
increase of fission reaction rate with increasing of RG-
Pu, RG-PuF₄, RG-PuO₂ heavy metals contents. The M 
value was obtained to be between 2.56 and 2.87 values. 
This value is greater than 1.2 value desirable of 

Fig. 4 shows the variation of the fission reaction rate 
versus the mixture components of Li₂₀Sn₈₀, RG-Pu, RG-
PuF₄, RG-PuO₂ in the liquid first wall, blanket and 
shield regions. Fig. 4 shows that the fission reaction rate 
increases linearly in the liquid first wall, blanket and 
shield regions with increasing of the heavy metals 
contents in mole percent.

4 Conclusions

In conclusion, it was found that reactor grade Pu 
amount decrease and neutronic calculations yield 
desirable values when one uses fluids of 95% Li₂₀Sn₈₀-
5% RG-Pu, RG-PuF₄, RG-PuO₂, in comparison to the 
other ratios and types of fluids in the liquid first wall, 
blanket and shield zones.

Acknowledgements

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References

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