Mechanical behaviour of graphdiyne film: experimental and molecular dynamics simulation

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Abstract. AFM experiments and molecular dynamics simulation of rectangular graphdiyne films are performed in this paper. The force-deflection curves are obtained, and the elastic modulus is calculated as 218.5 GPa and 482.615 GPa, respectively. The simulated maximum stress and pre-tension of graphdiyne film are 33.088 GPa and 0.551 GPa, respectively. It is observed that the graphdiyne film fractured in the central point once the indentation depth over the critical depth. Also, the obviously elastic behaviour has found during the loading-unloading-reloading process. The deformation mechanisms and fractured behaviour of the graphdiyne film are discussed in detail during the loading process. Moreover, the effects of various factors including loading speed and indenter radii of the graphdiyne film by the MD simulation are discussed.

1 Introduction

The two-dimensional materials have attracted great attention once graphene is discovered. Their superlative properties and potential applications such as electronic, chemical, thermal, mechanical stability and nanostructures have been a subject of extensive research recently [1-2]. Carbon’s three hybridization states (sp\textsuperscript{3}, sp\textsuperscript{2}, sp), can be combinations to produce numerous carbon allotropes; such as diamond (sp\textsuperscript{3}), graphite (sp\textsuperscript{2}), fullerene (sp\textsuperscript{2}), carbon nanotubes (sp\textsuperscript{2}) and graphene (sp\textsuperscript{2}). Most of these materials have remarkable mechanical strength [3] and electronic properties [4]. Here, we pay attention to graphdiyne [5], one of the carbon allotropes with the satisfactory candidates of novel graphene-like materials in future. Graphdiyne, which is sp\textsuperscript{2}-sp-hybridized carbon atoms and can be considered as one-third of the carbon-carbon bonds of graphene’s crystal structure are replaced by one acetylene unit.

The structure of graphdiyne has diacetylene (\(-\text{C≡C-C≡C-}\)) linkages between benzene rings, which makes the more flexible than graphene because of graphdiyne’s smaller density of atoms, indicating that the ductility of graphdiyne is better than graphene. Lee et al. [6] measured the intrinsic strength and in-plane stiffness of graphene are 130 ± 10 GPa and 1 ± 0.1 TPa at room temperature. Kang et al. [7] using the density functional theory (DFT) method calculated that the in-plane stiffness of graphene is 170.4 N/m and the strength is 45 GPa in zigzag direction and 29 GPa in armchair direction using molecular dynamics (MD). The study by Ahangari at al. [11] indicated that the in-plane stiffness and Young’s modulus of graphyne decrease from 164.4 N/m and 513.8 GPa at room temperature to 128.9 N/m and 402.8 GPa at 1500 K, respectively, using ab initio MD simulation. It’s shown that the ductility of graphyne and graphdiyne is better than graphene but the in-plane strength of graphene is superior to. However, the deformation mechanism of graphyne is not clear up to now.

In this paper, the mechanical behaviour of graphdiyne sheet transferred to copper network with rectangular wells is investigated by AFM and MD simulation. The van der Waals interaction between copper network and graphdiyne can make the graphdiyne binding strongly with copper network. It shows excellent mechanical performance such as high strength, more flexible and stretchable when compared to graphene. Also, a detailed fracture behaviour of graphdiyne is investigated with MD simulation, which clear show that the fracture of graphdiyne’s bonds leads to great ductility of graphdiyne.

2. METHODS
2.1 Materials

The graphdiyne is fabricated with the same method as Li et al. [5]. The monomer of hexaethynylbenzene was synthesized in good yield (62%) by adding tetrabutylammonium fluoride (TBAF) to the THF solution of hexakis[(trimethylsilyl)ethynyl]benzene for 10 minutes at 8 °C. The graphdiyne grow on the surface of copper foil in the pyridine by a cross-coupling reaction of the monomer structure of hexaethynylbenzene for 72 h at 60 °C under nitrogen atmosphere. In the procedure of forming graphdiyne, the copper foil is not only the catalyst for the cross-coupling reaction but also the substrate for growing graphdiyne film, as shown in Fig. 1. After successfully synthesized the graphdiyne membrane, the film is transferred to a copper network with rectangular wells for preparing atomic force microscope (AFM) tests. The van der Waals interaction between copper network and graphdiyne can make the graphdiyne binding strongly with copper network. The length and width of the wells are both 6.1 µm. In AFM experiments, a diamond AFM tip was chosen. Electron micrographs of the tip are shown in Figure 3, the length of the indenter is 6.4 ± 1 µm and the radius of curvature is 20 nm. The thermal noise method was used to calibrate the force constant of tip to be 25.47 N/m by measuring the sensitivity of optical leverage system. The GDY membranes were scanned in the noncontact mode and a slightly withdraw were executed.

2.2 MD model

We perform molecular dynamics (MD) simulations through large scale atom/molecular massively parallel simulation (LAMMPS) package [12] to simulate the nanoindentation of a suspended sheet of GDY membranes. The number of samples carbon atoms is 81468. There are three constituent bonds: aromatic (e.g. sp²), single and triple (e.g. sp³), we set the bond length of 1.44 Å for aromatic bonds, 1.40 Å for single bonds and 1.24 Å for triple bonds [13]. Fig. 2 shows the original model of our nanoindentation tests and the upper sphere configuration is the indenter. The indenter constructed by diamond, which is considered as a rigid object so that the indenter’s configuration of atoms had no changes during MD simulations. The radii of indenter were set as 20 Å so we can consider the contact area between indenter and membranes were point.

The boundary atoms are set clamped. The carbon-carbon interaction of the GDY membrane and indenter atoms was described by adaptive intermolecular reactive empirical bond order (AIREBO) potential [14]. The interaction between indenter and GDY membrane were described by Lennard-Jones (LJ) potential. All the MD simulations were performing by canonical ensemble (i.e. NVT) and the temperature were controlled by Nose-Hoover and the room temperature of 300 K were set to be equilibrium temperature. Before simulate the process of nanoindentation, the energy minimization and relaxation should be carried out to ensure the system stay in the equilibrium state with lowest energy.

Fig. 1. SEM images of GDY film (a) GDY films grown on the surface of copper foil; (b) the microstructure of GDY film; (c) cracked film on the edge of copper foil; (d) GDY film after transferred to the copper network with rectangular well.

Fig. 2. Atomic configuration of the original model.

3 RESULTS AND DISCUSSION

3.1 Mechanical model

According to the model of clamped circular elastic films under point load, the loading force F and deflection δ can be approximated with a polynomial function[15]. We considered two conditions getting the expression fitted to the force-displacement relationship:

\[ F = F_{\text{cap}}(\delta) + F_{\text{strain}}(\delta) \]  

(1)

The first term represents the membrane with a large initial pre-tension, and the second term is valid for stresses larger than the initial axial pre-tension. Based on our experiments condition, the first term can be written as

\[ F_{\text{cap}}(\delta) = \sigma_0^{2D} (\text{ah}) \beta^{3/2} \left( \frac{a}{a} \right)^{3/2} \left( \frac{\delta}{a} \right) \]  

(2)

where \( \sigma_0^{2D} \) is the pre-tension of membrane, \( \beta \) is the aspect ratio of the sample, and \( a \) represents the equivalent radius of the rectangular GDY membrane.

The second term can be written as

\[ F_{\text{strain}}(\delta) = E^{2D} (q' \text{ah}) \beta^{1/2} \left( \frac{a}{a} \right)^{1/2} \left( \frac{\delta}{a} \right) \]  

(3)

where \( E^{2D} \) is Young’s modulus of two-dimensional materials, and \( q' \) is an dimensionless constant, and \( b \) is Poisson’s ratio, \( b = 0.4 \).

According to Bhatia et al. [16], the maximum stress for a rectangular elastic film can be expressed as

\[ \sigma_n^{2D} = \left( \frac{FE^{2D}}{8\pi R} \right)^{1/2} \]  

(4)
where $\sigma_{\text{mem}}^{2D}$ is the maximum stress of the membrane under indenter, $R$ is the radii of indenter tip and $F$ is the breaking force under indentation.

### 3.2 The results of AFM experiments

Different thickness has been tests of the GDY film, so the dispersion of our data also proved the thickness has significantly effects to the elastic modulus. The measured relationship of load-deflection can be seen in Fig. 3. Because the thickness from 10 nm to 30 nm exists in our tests, the averaged elastic modulus is 218.5 GPa, which is almost one half of the MD results. This is due to the flaws in the synthesized film and the measured modulus is the defects materials. When the thickness increased, the elastic modulus also increased.

![Fig. 3. Load and indentation depth curves for the experiment and fitted by Eq.(4).](image)

### 3.3 The results of MD simulation

The indenter was placed over the center of the GDY membranes and moved perpendicular to the surface of the original GDY sheets with a constant velocity. The atoms on the edge of the GDY film kept in a static state because the edge atoms were fixed. After loading enough time and distance, some lattices of the GDY membranes were ultimately fractured and it shows the failure mode of the GDY membrane.

#### 3.3.1 Elastic modulus analysis

The simulated force-deflection curve is given in Fig. 4. The case of indenter radii as 2 nm and loading velocity as 0.2 Å/ps was considered to illustrate this behaviour. The fitted curve is according to the nonlinear least squares methods based on formula (1). The maximum value of the indentation depth is 42.08 Å corresponding to the 40.36 nN, which is the critical value of the GDY film broken.

The simulated elastic modulus, maximum stress and pre-tension of GDY are 482.615 GPa, 33.088 GPa and 0.551 GPa, respectively. The elastic modulus in our experiments is in good agreement with those published works [17], and the maximum stress is harmonious with the published work [10]. When the indentation depth is less than 4.22 Å, the slope of the curve is larger than the other range.

![Fig. 4. Load and indentation depth curves for the MD simulation results.](image)

### 3.3.2 The fracture behaviour of GDY under indentation

The loading-deflection curves can be obtained from the data of indenter load and indentation depth as shown in Fig. 5. It can see that the load suddenly dropped once the indentation depth over 42.08 Å corresponding to the load 40.36 nN when the loading velocity is 0.2 Å/ps. It can be understood by the different number of bonds in graphene and GDY. Each C atom is three-fold coordinated of graphene, whereas in GDY, the average coordination number of C atom is 2.5. This could be leading to the relatively smaller in-plane stiffness of GDY.

![Fig. 5. The force-deflection curve of loading process.](image)

The fracture behaviour happens when the load exceeded the ultimate force of GDY. Fig. 6 shows some detailed on the lattice fracture of the GDY film. The attractive pair potential exists in the indenter and film when the indenter close to the surface of GDY film, so that the distance small than 3.4 Å, the GDY film will be convex. The GDY film has a “snap-through” when the indenter contact with GDY film. With the increase of indentation depth, the force between indenter and GDY sheet changed from attractive interaction to repulsive interaction. Consequently, the force on the local atom which under indenter is non-uniform, the C-C bonds getting larger and the acetylenic bond broken firstly when the indentation depth over critical depth, the GDY film was expanded largely, as shown in Fig. 6(c). That is due to the energy...
of triple bond large than double bond and single bond, and the first fracture bond of triple bond is π bond. Then the C=C bonds broken subsequently, the fracture bond of double bond is also π bond, after that, some C=C bonds broken and that’s due to the σ bond is more stable than π bond. When the GDY film is broken, the force between indenter and film suddenly dropped to 0 and the bond-broken is irreversible. When the indenter fully penetrate the GDY film, some broken atoms separated from the GDY film and it can’t be recovery so that an irregular crack has occurred, as shown in Fig. 6(d). The broken C=C bonds and C≡C bond will re-combine to deform the circle structure, as shown in Fig. 6(e), the black circle part. Also, the quadrangular structure has appearance, as shown in Fig. 6(f), the blue circle part. The broken of C=C bond is partial to combine with the near atoms and form different shape as shown in Fig. 6(g), the circle part., the trilateral structure has shown in the red circle part. Be differ from the fracture of graphene [18], the GDY film deform a lathy crack through bond breaking and reforming as shown in Fig. 6(h). In near further the effects of indenter radii and loading speed on the mechanics properties of GDY film will be performed.

4 CONCLUSION

The mechanical behaviour of GDY film is studied by AFM tests and MD simulations in this paper. The microstructure of synthesized GDY film is obtained by scanning electron microscope (SEM) and then its elastic modulus is measured to be 218.5 GPa by AFM experiments. An atomic model of GDY is constructed and the nanoindentation process is carried out. The maximum value of the indentation depth is 42.08 Å corresponding to the 40.36 nN in the case of indenter radii as 2 nm and loading velocity as 0.2 Å/ps, the elastic modulus, maximum stress and pre-tension of GDY are 482.615 GPa, 33.088 GPa and 0.551 GPa, respectively. Once the indentation depth over the critical depth, the broken of the GDY film occur, and the failure behaviour of the GDY is analysed according to its micro-structures during continuous loading.

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