Recent developments in charmed baryon spectroscopy

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Abstract. An overview of recent developments in charmed baryon spectroscopy is given. The classification of charmed baryons is presented, a quark model for ground states is briefly described, and the energy levels of excited states are analyzed.

1 Introduction

The spectroscopy of charmed baryons is beautiful and intricate. With three quarks there are numerous degrees of freedom, giving rise to many more states than in the charmed meson sector. At the same time, the large difference in mass between the charm quark and the light quarks provides a natural way to classify and understand these states: Heavy Quark Effective Theory (HQET). The spectrum of known singly charmed states can be thought of in three broad regimes: the ground states, which are a vindication of the constituent quark model; the low-lying excited states, which are described well by HQET; and higher excited states, where the situation is murkier.

2 Quark Model for Ground States

In the constituent quark model [1], baryons composed of $u,d,s,c$ quarks can be classified into $SU(4)$ multiplets according to the symmetry of their flavor, spin, and spatial wavefunctions. All states in a given $SU(4)$ multiplet have the same angular momentum $J$, and parity $P$, but can have different quark flavors. For excited states with multiple units of orbital angular momentum the number of possible multiplets becomes large, but for the ground states the picture is much simpler. This framework is not exact — different states with the same conserved quantum numbers will mix, and baryons are not pure three-quark objects — but it works remarkably well for the ground states.

Quarks are fermions, so the baryon wavefunction must be overall antisymmetric under quark interchange$^1$. Baryons are color singlets, and so have an antisymmetric color wavefunction. In the ground state, the orbital angular momentum $L$ is zero ($S$-wave) and the spatial wavefunction is symmetric. Therefore, the product of the spin and flavor wavefunctions

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$^1_{Strictly, it only needs to be antisymmetric under interchange of equal-mass quarks, but we assume SU(4) is a good symmetry.}$
must also be symmetric for ground-state baryons. There are two ways this can be accomplished: both wavefunctions can be fully symmetric, or both can have mixed symmetry with the product being symmetric.

In concrete terms, we can consider a singly charmed baryon to consist of a heavy $c$ quark and a light diquark with spin-parity $j^p$. Assuming isospin symmetry and letting $q$ denote a $u$ or $d$ quark, there are four possibilities for the flavor content of the diquark:

- $qq$ with isospin 0 (flavor antisymmetric);
- $qq$ with isospin 1 (flavor symmetric);
- $sq$ with isospin $1/2$ (either);
- $ss$ with isospin 0 (flavor symmetric).

These correspond to the $\Lambda_c$, $\Sigma_c$, $\Xi_c$, and $\Omega_c$ states, respectively. The diquark wavefunction must be antisymmetric under quark interchange. Its color wavefunction is antisymmetric and in the ground state its spatial wavefunction is symmetric, so it may be either flavor-symmetric and spin-symmetric ($j^p = 1^+$) or flavor-antisymmetric and spin-antisymmetric ($j^p = 0^+$). Combining the diquark with the charm quark gives rise to the possible states illustrated in figure 1, where the multiplets of the full $SU(3)$ symmetry (formed by the $u$-, $d$-, and $s$-quarks) are shown. Those with $J^P = 1/2^+$ are all members of the same multiplet as the proton, and those with $J^P = 3/2^+$ are all members of the same multiplet as the $\Delta$ and $\Omega$ (figure 2). Note that there is a second isospin doublet of $\Xi_c$ states with $J^P = 1/2^+$, denoted $\Xi_c'$.

The constituent quark model predicts relations between the masses of states as well as their existence and quantum numbers.

The quark model also predicts baryons with two charm quarks and one lighter quark, as shown in figure 2. Because two quark flavors are identical, fewer distinct configurations are possible than for the $C = 1$ baryons. Three weakly-decaying ground states with $J^P = \frac{1}{2}^+$ ($\Xi_{cc}^+, \Xi_{cc}'^+, \Omega_{cc}^+$) and three further states with $J^P = \frac{3}{2}^+$ ($\Xi_{cc}^{++}, \Xi_{cc}'^{++}, \Omega_{cc}^{++}$) are expected.

3 Excited States

Baryons can be given orbital ($l$) or radial ($k$) excitations. Since they are three-body systems there are two degrees of freedom in each case (denoted $\rho, \lambda$). For baryons with one heavy
These correspond to the (figure 2). Note that there is a second isospin doublet of \( \Omega \) possible than for the shown in figure 2. Because two quark flavors are identical, fewer distinct configurations are their existence and quantum numbers.

Figure 1. The quark model also predicts baryons with two charm quarks and one lighter quark, as 

\[ \Xi^+ \] (\( \Xi^- \)) or radial (\( \Xi^{*+} \)) and in the ground state its spatial wavefunction is symmetric, so it may be either flavor-

\[ \sum_{\text{p}} \] and a light diquark with spin-parity \( j_{\text{p}} \). A double ring indicates that two states have the same \( J^P, I_3, S, \) and \( C \) quantum numbers.

\[ E = \sqrt{\frac{K}{m}(3 + 2l_\rho + 4k_\rho)} + \sqrt{\frac{K}{\mu}(3 + 2l_A + 4k_A)}, \]

where \( K \) is a constant describing the potential and \( \mu = (2/3M + 1/3m)^{-1} \approx 3m \) in the heavy quark limit. Thus, the \( \rho \) excitations (within the diquark) require roughly three times as much energy as the corresponding \( \lambda \) excitations (between quark and diquark). Therefore the lowest-lying excitations are those with \( l_\lambda = 1 \) and the other quantum numbers zero, i.e. \( L = 1 \). (Within this band there will be further splitting, e.g. due to spin-spin and spin-orbit couplings.) The second band will consist of two groups of states that have comparable energy: those with \( l_\lambda = 2 \) (\( L = 2 \)) and those with \( k_\lambda = 1 \) (\( L = 0 \)), with the other quantum numbers being zero. Beyond the second band the degeneracy grows further, but we lack useful experimental data in this region in any case.

All this said, it is important to bear in mind that states which share all conserved, external quantum numbers (\( J, P, I, C, S \)) can mix. Therefore we should be careful when interpreting observed resonances as specific expected states, particularly for higher excitations.

4 \( \Xi_c \) Family

Since all three quark flavors are different for the \( \Xi_c \), there are many allowed configurations. These may be divided into states for which the light diquark wavefunction is flavor-antisymmetric (analogous to \( \Lambda_c \)) or flavor-symmetric (analogous to \( \Sigma_c \)).

The two ground states are the only members of the group that decay weakly, and their masses, lifetimes, and many of their decay modes have been measured [3]. The \( \Xi_c \) states also exist in many angular momentum configurations of the constituent quarks, each as an isospin pair (table 1).
Table 1. Summary of excited $\Xi_c$ baryons [3, 13].

<table>
<thead>
<tr>
<th>State</th>
<th>Decay mode</th>
<th>Mass, MeV/c^2</th>
<th>Width, MeV</th>
<th>J', P'</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Xi_c^{+}$</td>
<td>$\Xi_c^{+}\gamma$</td>
<td>2577.4 ± 1.2</td>
<td>2792</td>
<td>$\frac{1}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c^{0}$</td>
<td>$\Xi_c^{0}\gamma$</td>
<td>2578.8 ± 0.5</td>
<td>2820</td>
<td>$\frac{3}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2645)^+$</td>
<td>$\Xi_c^{+}\pi^+$</td>
<td>2645.53 ± 0.31</td>
<td>3077</td>
<td>$\frac{1}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2645)^0$</td>
<td>$\Xi_c^{0}\pi^+$</td>
<td>2646.32 ± 0.31</td>
<td>3095</td>
<td>$\frac{3}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2790)^+$</td>
<td>$\Xi_c^{+}\pi^0$</td>
<td>2792.0 ± 0.5</td>
<td>2816</td>
<td>$\frac{1}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2790)^0$</td>
<td>$\Xi_c^{0}\pi^0$</td>
<td>2792.8 ± 1.2</td>
<td>2820</td>
<td>$\frac{3}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2815)^+$</td>
<td>$\Xi_c^{+}\pi^+\pi^-$, $\Xi_c(2645)^0\pi^+, \Xi_c^{0}\pi^+$</td>
<td>2816.67 ± 0.31</td>
<td>3077</td>
<td>$\frac{1}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2815)^0$</td>
<td>$\Xi_c^{0}\pi^+\pi^-$, $\Xi_c(2645)^0\pi^+, \Xi_c^{0}\pi^+$</td>
<td>2820.22 ± 0.32</td>
<td>3077</td>
<td>$\frac{3}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2930)^0$</td>
<td>$\Lambda_c^+ K^-$</td>
<td>2931 ± 6</td>
<td>2930</td>
<td>$\frac{1}{2}$+</td>
</tr>
<tr>
<td>$\Xi_c(2930)^+$</td>
<td>$\Lambda_c^+ K^+\pi^-, \Sigma_c^+ K^-, \Xi_c(2645)^0\pi^+, \Xi_c^{0}\pi^0$</td>
<td>2969.4 ± 0.8</td>
<td>2967.8 ± 0.8</td>
<td>28.1±0.4</td>
</tr>
<tr>
<td>$\Xi_c(2970)^0$</td>
<td>$\Sigma_c^+ K^-, \Lambda D^+$</td>
<td>3055.9 ± 0.4</td>
<td>3059.0 ± 0.8</td>
<td>6.4 ± 2.4</td>
</tr>
<tr>
<td>$\Xi_c(2970)^+$</td>
<td>$\Sigma_c^+ K^-, \Lambda D^+$</td>
<td>3077.2 ± 0.4</td>
<td>3079.9 ± 1.4</td>
<td>5.6 ± 2.2</td>
</tr>
</tbody>
</table>

The $\Xi_c^+$ and $\Xi_c(2645)$ states form a doublet analogous to the $\Sigma_c(2455)$ and $\Sigma_c(2520)$ with expected ($J^P, J'P'$) of $(1^+, 1/2^+)$ and $(1^+, 3/2^+)$, respectively. The former is too light to decay strongly, but the electromagnetic transition $\Xi_c^+ \rightarrow \Xi_c \gamma$ is allowed. BaBar performed an angular analysis of $\Xi_c^0 \rightarrow \Xi_c (\Xi_c^+ \pi^-) \gamma$ in the helicity formalism and found the data to be consistent with $J = 1/2$ [4]. However, due to the inclusive production environment higher spins could not be ruled out.

The low-lying excited states $\Xi_c(2790)$ and $\Xi_c(2815)$ are analogous to the $\Lambda_c(2595)$ and $\Lambda_c(2625)$, and their decays follow a corresponding pattern: $\Xi_c(2790) \rightarrow \Xi_c^0 \pi$, $\Xi_c(2815) \rightarrow \Xi_c(2645)\pi$. They were therefore identified as the $1/2^-, 3/2^-$ doublet with $J' = 1^-$ and the diquark in a flavor-antisymmetric configuration [5].

Recently Belle collaboration significantly improved measured mass differences (between excited and ground states) and widths (where applicable) for $\Xi_c^+$, $\Xi_c(2645)$, $\Xi_c(2790)$, $\Xi_c(2815)$, and $\Xi_c(2970)$ states [6].

The $\Xi_c(2930)^0$ was seen in $B^+ \rightarrow \Lambda_c^+ \Lambda_c^- \pi^+ K^- \Xi_c$ decays [7]. The Dalitz plot was clearly not flat and the $\Lambda_c^+ K^-$ projection was consistent with a single resonance with the parameters given in table 1. However, given the small sample size, it was impossible to rule out other explanations (such as two overlapping $\Xi_c$ resonances or a complicated interference pattern between $\Xi_c$ and charmonium resonances). Recently this analysis was repeated by the Belle collaboration [8], using 1.5 larger statistics, which allowed to observe $\Xi_c(2930)^0$ signal with greater significance and improve measurement precision.

The remaining resonances were all seen in the $\Lambda_c^+ K^-\pi^+$ isodoublet of final states (and, in the case of the $\Xi_c(2970)$, in $\Xi_c(2645)\pi$). The $\Xi_c(2970)$ and $\Xi_c(3077)$ were discovered by Belle in $\Lambda_c^+ K^-\pi$ and confirmed by BaBar. Since this is a three-body decay it could proceed via an intermediate $\Sigma_c$. BaBar tested this by fitting a two-dimensional PDF in $M(\Lambda_c^+ \pi)$, $M(\Lambda_c^+ K\pi)$. It was found that approximately half of the $\Xi_c(2970)$ decays to this final state proceed through an intermediate $\Sigma_c(2455)$ with the rest non-resonant. By contrast, most if not all of the $\Xi_c(3077)$ decays to this final state proceed via $\Sigma_c(2455)$ or $\Sigma_c(2520)$ with approximately equal branching fractions to each. Because the $\Xi_c(2970)$ is close to threshold on the scale of its natural width, especially with an intermediate $\Sigma_c$, the available phase space changes sig-
Table 2. Summary table of excited $\Omega_c$ baryons [3]. For each parameter, the first uncertainty is statistical and the second systematic. The asymmetric uncertainty arising from the $\Xi_c^+$ mass is given separately.

<table>
<thead>
<tr>
<th>State</th>
<th>Decay mode</th>
<th>Mass, MeV/$c^2$</th>
<th>Width, MeV</th>
<th>$J^P$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Omega_c^{0}$</td>
<td>$\Omega_c^0\gamma$</td>
<td>2765.9 ± 2.0</td>
<td>4.5 ± 0.7</td>
<td>$3^+$/2</td>
</tr>
<tr>
<td>$\Omega_c(3000)^0$</td>
<td>$\Xi_c^+K^-$</td>
<td>3000.4 ± 0.4</td>
<td>&lt; 1.2 @ 95% CL</td>
<td></td>
</tr>
<tr>
<td>$\Omega_c(3050)^0$</td>
<td>$\Xi_c^+K^-$</td>
<td>3050.2 ± 0.33</td>
<td>&lt; 1.2 @ 95% CL</td>
<td></td>
</tr>
<tr>
<td>$\Omega_c(3065)^0$</td>
<td>$\Xi_c^+K^-$</td>
<td>3065.6 ± 0.4</td>
<td>3.5 ± 0.4</td>
<td></td>
</tr>
<tr>
<td>$\Omega_c(3090)^0$</td>
<td>$\Xi_c^+K^-$</td>
<td>3090.2 ± 0.3 ± 0.7</td>
<td>8.7 ± 1.3</td>
<td></td>
</tr>
<tr>
<td>$\Omega_c(3120)^0$</td>
<td>$\Xi_c^+K^-$</td>
<td>3119.1 ± 1.0</td>
<td>&lt; 2.6 @ 95% CL</td>
<td></td>
</tr>
</tbody>
</table>

significantly across the resonance. Different handling of this threshold behavior is the reason for the mild tension in the fitted $\Xi_c$ masses between [9] and [10]. The masses measured in the $\Xi_c(2645)\pi^+$ final state [11], which is far from threshold, are consistent with the BaBar treatment, although the widths are smaller than either experiment saw in $\Lambda_c^+\bar{K}\pi$. Requiring an intermediate $\Sigma_c$ reduces the background levels, and by doing this BaBar was able to identify two further candidate states, the $\Xi_c(3055)$ and $\Xi_c(3123)$. The latter had a limited statistical significance ($3\sigma$), and later was not confirmed by Belle with twice as much statistics [12].

Till recently all measurements of excited $\Xi_c$ baryons were performed using decay modes in which the charm quark is contained in the final state baryon. Belle reported studies of $\Xi_c$ baryons decaying to the $\Lambda D^+$ and $\Lambda D^0$ final states [13]. Significant signals were found for $\Xi_c(3055)^+$ and $\Xi_c(3080)^+$ decays into $\Lambda D^+$. In the $\Lambda D^0$ final state, observation of the $\Xi_c(3055)^0$ was reported.

As a final point it should be noted that no direct measurements of the $J^P$ of any of the excited $\Xi_c$ states are available. Mild constraints on the quantum numbers can be inferred from the decay pattern. For example, the observation of the $\Xi_c(3077)$ in $\Sigma_c(2455)\bar{K}$ and $\Sigma_c(2520)\bar{K}$ excludes states with diquark $j^P = 0^-$. However, many quantum numbers are still allowed for these states and there is a range of opinions on the best match to the data.

5 $\Omega_c$ Family

In contrast to the $\Lambda_c$, $\Sigma_c$, and $\Xi_c$ families available experimental data on the $\Omega_c$ ground state were limited before the B Factories. The weakly-decaying $\Omega_c^0$ ($J = 1/2^+$) had been seen in a number of different decay modes and production environments, but with only limited statistics (typically samples of $O(10)$ events in a given decay mode, and never more than 100); and the $J = 3/2^+$ $\Omega_c^0$ had not been observed. Belle carried out a precise measurement of the $\Omega_c^0$ mass using a sample of 725 decays to the $\Omega^-\pi^+$ final state [14], obtaining (2693.6 ± 0.3$^{+1.8}_{-1.5}$) MeV/$c^2$.

The short list of known doubly strange charm baryons is summarized in table 2. The $\Omega_c^0$ is too light to undergo strong decay and so decays purely to $\Omega_c^0\gamma$. It was discovered by BaBar [15] and confirmed by Belle [14]. Both measured the mass difference $m(\Omega_c^0) - m(\Omega_c^0)$, and the two results are in excellent agreement with each other as well as with most theoretical predictions [16].

Recently LHCb collaboration performed a study of the $\Xi_c^+K^-$ spectrum, observing five new narrow excited $\Omega_c^0$ states [17] and thus presenting first excited doubly strange charm baryons, that decay strongly. The observation of these states in an inclusive process through a two-body decay does not allow the determination of their quantum numbers. More information can be obtained from the study of possible three-body decays or when reconstructing
these states in decays of heavy baryons. Four of these states (\(\Omega_c(3000), \Omega_c(3050), \Omega_c(3065),\) and \(\Omega_c(3090)\)) were confirmed by Belle with very similar parameters, while no evidence for \(\Omega_c(3120)\) was found [18].

6 \(\Xi_{cc}\) Family

Up till recently, sightings of \(\Xi_{cc}\) states have been reported only at the SELEX experiment. SELEX claimed observation of \(\Xi_{cc}^+\) at a mass of 3519 MeV/c\(^2\) in the \(\Lambda_c^+ K^-\pi^+\) and \(pD^+K^-\) final states [19]. In each case the signature is a small, narrow signal on top of a smaller background: an excess of 15.9 events above an estimated background of 6.1\(\pm\)0.5 for \(\Lambda_c^+ K^-\pi^+\), and of 5.4 above 1.6\(\pm\)0.4 for \(pD^+K^-\). The observations were controversial, primarily because the lifetime and the production rate of \(\Xi_{cc}\) at SELEX were far from expectations. The theory expectation for the \(\Xi_{cc}^+\) lifetime is approximately 200–250 fs across a number of models [20], compared to a reported upper limit of 33 fs. Even more surprising, by comparing the relative yields of \(\Lambda_c^+\) and \(\Xi_{cc}^+\) and correcting for acceptance and additional decay modes, SELEX estimated that 20\% of its sample of 1,630 \(\Lambda_c^+\) came from \(\Xi_{cc}^+\) decays (presumably with a further contribution of similar order from \(\Xi_{cc}^{++}\)). This runs counter to expectations: it is much more difficult to produce a baryon with more than one unit of flavor because two heavy quark-antiquark pairs need to be created within a narrow enough kinematic window for them to coalesce into a baryon. SELEX also reported preliminary observations of several other peaks in the \(\Lambda_c^+ K^-\pi^+\) and \(\Lambda_c^+ K^-\pi^+\pi^+\) mass spectra, claiming a further \(\Xi_{cc}^+\) state at 3443 MeV/c\(^2\) and \(\Xi_{cc}^{++}\) states at 3460, 3540, and 3780 MeV/c\(^2\) [21], but did not publish these results.

FOCUS photoproduction experiment, BaBar, Belle, and later LHCb carried out searches for \(\Xi_{cc}\) in an attempt to reproduce the published SELEX observation [22]. All three examined \(\Lambda_c^+ K^-\pi^+\) along with a variety of other final states. None found any signal. In each case, the samples of \(\Lambda_c^+\) events used were much larger than that of SELEX: yields of 19k for FOCUS, 600k for BaBar, 840k for Belle, and 820k for LHCb. However, because the production environments differ from that of SELEX it cannot be excluded that the doubly charmed baryon cross section is dramatically higher with a hyperon in the initial state for reasons that are not understood theoretically.

There is one further twist: several of the excited \(\Xi_c\) states discussed in Section 4, notably the \(\Xi_c(2970)\) and \(\Xi_c(3077)\), were discovered in the \(\Lambda_c^+ K^-\pi^+\) final state. None of these states were reported by SELEX (although they were not specifically excluded either). This poses a further challenge: if the production cross section at SELEX for these excited \(\Xi_c\) states were not lower than for \(\Xi_{cc}\) they should have been seen clearly, so their non-observation raises questions about the \(\Xi_{cc}\) signals; conversely, if the cross section for the excited \(\Xi_c\) is smaller than for \(\Xi_{cc}\) the mechanism must be highly exotic since the \(\Xi_c\) states are not only lighter than \(\Xi_{cc}\) but also closer in flavor content to the initial-state \(\Sigma^-\).

Recently LHCb collaboration performed a study of the \(\Lambda_c^+ K^-\pi^+\pi^+\) spectrum, observing a structure consistent with originating from a weakly decaying particle, identified as the doubly charmed baryon \(\Xi_{cc}^{++}\) [23]. The mass of the structure was measured to be \((3621.40 \pm 0.72 \pm 0.27 \pm 0.14)\) MeV/c\(^2\), where the last uncertainty is due to the limited knowledge of the \(\Lambda_c^+\) mass, and its width is consistent with experimental resolution. The \(\Xi_{cc}^{++}\) lifetime was measured by LHCb in a separate study and was found to be \((256^{+34}_{-22} \pm 14)\) fs [24]. While the reported state is consistent with most theoretical expectations for the \(\Xi_{cc}^{++}\) baryon, it is inconsistent with being an isospin partner to the \(\Xi_{cc}^+\) state reported by the SELEX collaboration.
7 Summary

Recently observed excited \( \Omega_c \) and \( \Xi^{++}_c \) states present a unique opportunity to test and further improve theoretical models, that predict properties of heavy hadrons. More accurate \( \Xi_c \) mass values is of both practical and theoretical interest, and knowing their widths (where applicable) can then lead to measurements of the matrix elements of their decays. These matrix elements are also applicable to other excited charmed and bottom baryons.

Interesting feature of the charmed baryons spectrum is that highly excited charmed baryons can decay to a charmed meson and a non-charmed baryon.

It should be noted that no direct measurements of the \( J^P \) of any of the excited strange charmed baryons are available. Constraints on the quantum numbers can be inferred only from the decay pattern.

Acknowledgements

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