

# Hadronic transitions in bottomonia at Belle

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**Abstract.** Recent Belle results on various hadronic transitions among bottomonia are presented. We observe transitions with the  $\eta$  and  $\eta'$  meson at the  $\Upsilon(4S)$ . Bottomonium production together with the  $\eta$  meson is also reported at the  $\Upsilon(10860)$ . We study  $\pi^+\pi^-\pi^0$  transitions at the  $\Upsilon(10860)$  and  $\Upsilon(11020)$ .

## 1 Introduction

Spectroscopy of heavy quarkonia provides crucial information for understanding strong interactions since QCD calculations become possible. Measurements of hadronic transitions ( $\pi^+\pi^-$ ,  $\eta$ ,  $\omega$ , ...) between bottomonia yield important input for QCD.  $\eta$  transitions are believed to be suppressed compared to  $\pi^+\pi^-$  because of the spin flip.  $\pi^+\pi^-$  transitions and their peculiarities were studied by both BaBar and Belle. Large integrated luminosity collected by Belle above the  $\Upsilon(4S)$  opened unique possibilities resulting in exciting observations of  $h_b(1P)$ ,  $h_b(2P)$ ,  $\eta_b(2S)$ ,  $Z_b(10610)$  and  $Z_b(10650)$ . In this work we discuss recent results on hadronic transitions in bottomonia.

## 2 Study of $\eta$ and $\pi^+\pi^-$ transitions in $\Upsilon(4S)$ decays to lower $b\bar{b}$

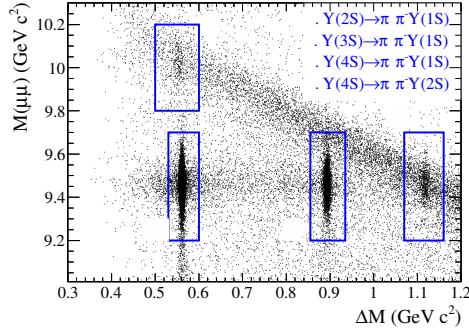
Here we study the transitions  $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(nS)$  ( $n = 1, 2$ ) and  $\Upsilon(4S) \rightarrow \eta\Upsilon(1S)$ , by reconstructing  $\Upsilon(nS) \rightarrow \mu^+\mu^-$ ,  $\eta \rightarrow \pi^+\pi^-\pi^0$  using  $(538 \pm 7) \times 10^6$   $\Upsilon(4S)$  mesons [1].

For the dipion transitions, the two-dimensional distribution of the invariant dimuon mass  $M(\mu\mu)$  vs.  $\Delta M$  for the selected events is shown in Fig. 1, where  $\Delta M = M(\pi\pi\mu\mu) - M(\mu\mu)$ . The signal yields are determined from the fit to the  $\Delta M$  distribution in  $6 \times 4$  ( $4 \times 4$ ) bins of  $M(\pi^+\pi^-)$  and  $\cos\theta_{\text{hel}}(\pi^+)$  in the regions (a) and (b) due to the initial-state radiation processes  $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$  and  $\Upsilon(3S) \rightarrow \pi^+\pi^-\Upsilon(1S)$ , respectively (in (c) and (d) due to the decays of interest  $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S)$  and  $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(2S)$ , respectively). The results are listed in Table 1 and the  $\Delta M$  distributions integrated over the bins are shown in Fig. 2.

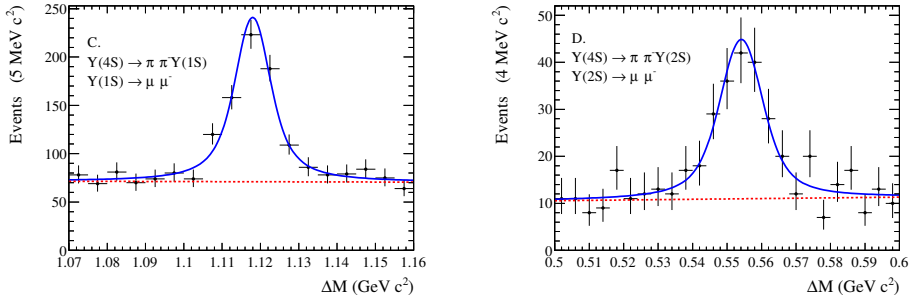
For the  $\eta$  transitions, the distributions of  $\Delta M_\eta = M(\pi\pi\gamma\mu\mu) - M(\mu\mu) - M(\pi\pi\gamma\gamma)$  are shown in Fig. 3 for the  $\Upsilon(4S) \rightarrow \eta\Upsilon(1S)$  (left) and  $\Upsilon(1^3D_{1,2}) \rightarrow \eta\Upsilon(1S)$  (right).

All the results are compatible with the previous measurements with the slightly improved precision. We confirm the enhancement of the  $\Upsilon(4S) \rightarrow \Upsilon(1S)$  transition via the spin-flip exchange of the  $\eta$  meson with respect to the dipion one.

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**Figure 1.** Distribution of  $M(\mu\mu)$  vs.  $\Delta M$  for the selected events. Fit regions are enclosed in boxes.



**Figure 2.** Fits to the  $\Delta M$  distributions for: (left)  $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S)$  and (right)  $\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(2S)$ .

**Table 1.** The signal yields and branching fractions compared to PDG [2] for the decay modes studied.

Decay	Events	$\mathcal{B}, 10^{-5}$	$\mathcal{B}_{\text{PDG}}, 10^{-5}$
$\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(1S)$	$1095 \pm 74$	$8.2 \pm 0.5 \pm 0.4$	$8.1 \pm 0.6$
$\Upsilon(4S) \rightarrow \pi^+\pi^-\Upsilon(2S)$	$821 \pm 107$	$7.9 \pm 1.0 \pm 0.4$	$8.6 \pm 1.3$
$\Upsilon(4S) \rightarrow \eta\Upsilon(1S)$	$49 \pm 7$	$1.70 \pm 0.23 \pm 0.08$	$1.96 \pm 0.28$
$\Upsilon(1^3D_{1,2}) \rightarrow \eta\Upsilon(1S)$	$2.1 \pm 3.0$	$< 0.23$	–

### 3 Observation of $\Upsilon(4S) \rightarrow \eta'\Upsilon(1S)$

This observation is based on the same data sample of  $(538 \pm 7) \times 10^6$   $\Upsilon(4S)$  mesons as in Sect. 2. We reconstruct  $\Upsilon(1S) \rightarrow \mu^+\mu^-$  and  $\eta' \rightarrow \rho\gamma$ ,  $\eta\pi^+\pi^-$ ,  $\eta \rightarrow 2\gamma$  [3].

Signal events are identified by the variable  $\Delta M_{\eta'} = M(\Upsilon(4S)) - M(\Upsilon(1S)) - M(\eta')$ , where  $M(\Upsilon(1S)) = M(\mu\mu)$ ,  $M(\Upsilon(4S)) = M(\mu\mu\pi\pi\gamma)[M(\mu\mu\pi\pi\gamma\gamma)]$  and  $M(\eta') = M(\pi\pi\gamma)[M(\pi\pi\gamma\gamma)]$ . The signal and background yields are obtained by the fit to the  $\Delta M_{\eta'}$  distributions shown in Fig. 4 and are also listed in Table 2.

The combined branching fraction is  $\mathcal{B}(\Upsilon(4S) \rightarrow \eta'\Upsilon(1S)) = (3.43 \pm 0.88 \pm 0.21) \times 10^{-5}$  and corresponds to the  $5.7\sigma$  statistical significance.

We also determine the ratios of branching fractions:

$$R_{\eta'/h} = \frac{\mathcal{B}(\Upsilon(4S) \rightarrow \eta'\Upsilon(1S))}{\mathcal{B}(\Upsilon(4S) \rightarrow h\Upsilon(1S))}$$

**Table 2.** The signal and background yields as well as significances for two  $\eta'$  decay modes.

$\eta'$ decay mode	$N_{\text{sig}}$	$N_{\text{bkg}}$	Sign., $\sigma$
$2\pi 1\gamma$	$22 \pm 7$	$96 \pm 11$	4.2
$2\pi 2\gamma$	$5.0 \pm 2.3$	$2.0 \pm 1.6$	4.1

where the decay is mediated by  $h = \eta$  or  $h = \pi^+\pi^-$  and using the values from our work [1] obtain  $R_{\eta'/\eta} = 0.20 \pm 0.06$  and  $R_{\eta'/\pi^+\pi^-} = 0.42 \pm 0.11$ . The former ratio agrees with the predicted 0.2 [4].

#### 4 Observation of $\Upsilon(4S) \rightarrow \eta h_b(1P)$

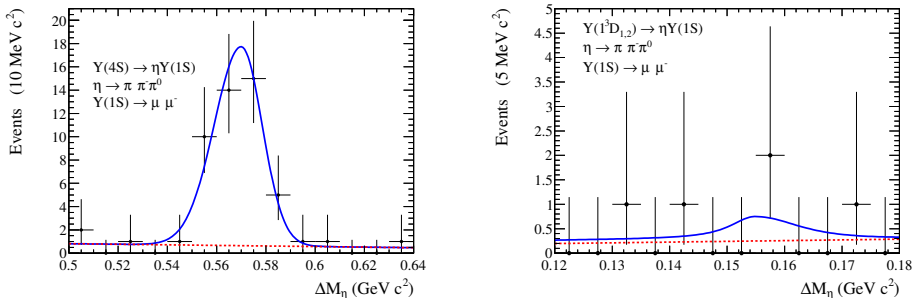
From a sample of  $771.6 \times 10^6$   $\Upsilon(4S)$  decays ( $711 \text{ fb}^{-1}$ ) Belle observed for the first time the decay  $\Upsilon(4S) \rightarrow \eta h_b(1P)$  using the  $\eta$  missing mass,  $M_{\text{miss}}(\eta) = \sqrt{(P_{e^+e^-} - P_\eta)^2}$  and  $\eta \rightarrow \gamma\gamma$  [5]. The  $M_{\text{miss}}(\eta)$  distribution is shown in Fig. 5 (left). The clear  $h_b(1P)$  signal is observed with the fit yield of  $112469 \pm 5537$  events ( $11\sigma$  significance).

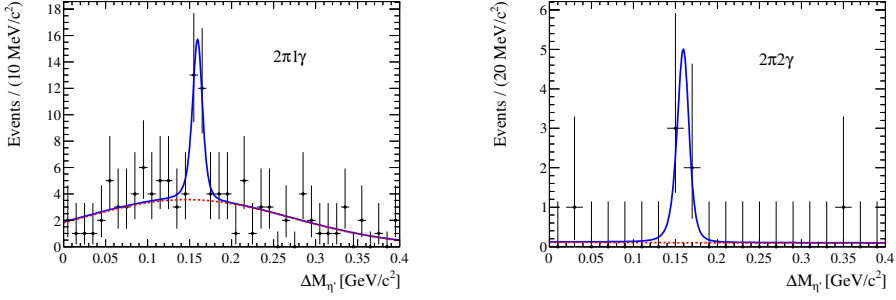
The obtained branching fraction  $\mathcal{B}(\Upsilon(4S) \rightarrow \eta h_b(1P)) = (2.18 \pm 0.11 \pm 0.18) \times 10^{-3}$  agrees with the theoretical prediction of Ref. [6].

We reconstruct the  $h_b(1P) \rightarrow \gamma \eta_b(1S)$  decay by measuring the number of events of  $\Upsilon(4S)$  decay as a function of the variable  $\Delta M_{\text{miss}} = M_{\text{miss}}(\eta\gamma) - M_{\text{miss}}(\eta)$ . Its distribution (Fig. 5 (right)) shows a clear excess at  $\Delta M_{\text{miss}} = M_{\eta_b(1S)} - M_{h_b(1P)}$ , with a yield of  $33116 \pm 4741$  events ( $9\sigma$  significance). The corresponding branching fraction  $\mathcal{B}(h_b(1P) \rightarrow \gamma \eta_b(1S)) = (56 \pm 8 \pm 4)\%$  agrees with predictions [7, 8]. The results are summarized in Table 3.

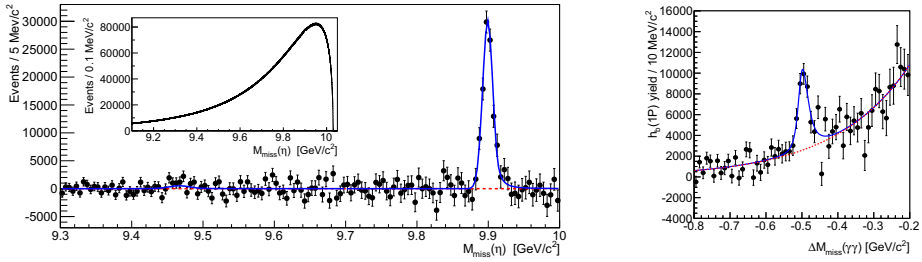
**Table 3.** Summary of the searches for  $\Upsilon(4S) \rightarrow \eta h_b(1P)$  and  $h_b(1P) \rightarrow \gamma \eta_b(1S)$ .

Observable	Value, MeV
$M_{h_b(1P)}$	$9899.3 \pm 0.4 \pm 1.0$
$M_{\eta_b(1S)}$	$9400.7 \pm 1.7 \pm 1.6$
$\Gamma_{\eta_b(1S)}$	$8_{-5}^{+6} \pm 5$
$\Delta M_{\text{HF}}(1P) = M_{\chi_{bj}}^{\text{sa}}(1P) - M_{h_b(1P)}$	$+0.6 \pm 0.4 \pm 1.0$
$\Delta M_{\text{HF}}(1S) = M_{\Upsilon(1S)} - M_{\eta_b(1S)}$	$59.6 \pm 1.7 \pm 1.6$

**Figure 3.** Fits to the  $\Delta M_\eta$  distributions for: (left)  $\Upsilon(4S) \rightarrow \eta \Upsilon(1S)$  and (right)  $\Upsilon(1^3D_{1,2}) \rightarrow \eta \Upsilon(1S)$ .



**Figure 4.** Fit to the  $\Delta M_\eta$  distribution for  $\Upsilon(4S) \rightarrow \eta'\Upsilon(1S)$  candidates in the  $2\pi 1\gamma$  (left) and  $2\pi 2\gamma$  (right) modes.



**Figure 5.** Distributions of: (left)  $M_{\text{miss}}(\eta)$  after background subtraction, (right)  $\Delta M_{\text{miss}}$ .

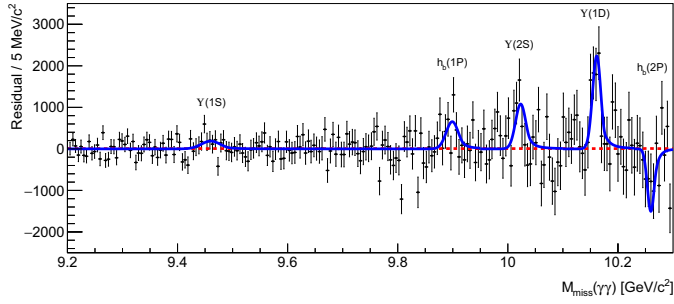
## 5 Production of $b\bar{b}$ and $\eta$ near $\Upsilon(5S)$

For this study we used a sample of  $121.4 \text{ fb}^{-1}$  collected near the  $\Upsilon(5S)$  energy [9]. The approach is based on the missing mass  $M_{\text{miss}}(\eta)$  similar to that in Sect. 4. The corresponding distribution is shown in Fig. 6 with the results listed in Table 4.

**Table 4.** Summary of the studies of  $e^+e^- \rightarrow \eta(b\bar{b})$  near  $\Upsilon(5S)$ .

Process	Sign., $\sigma$	$N, 10^3$	Process	Sign., $\sigma$	$N, 10^3$
$\eta\Upsilon(1S)$	$1.5\sigma$	$1.7 \pm 1.0$	$\eta\Upsilon(2S)$	$3.3\sigma$	$5.6 \pm 1.6$
$\eta h_b(1P)$	$2.7\sigma$	$3.9 \pm 1.5$	$\eta\Upsilon(1D)$	$5.3\sigma$	$9.3 \pm 1.8$

We observe for the first time the process  $e^+e^- \rightarrow \eta\Upsilon_J(1D)$  and find evidence for  $e^+e^- \rightarrow \eta\Upsilon(2S)$ . Assuming that the process proceeds entirely via the  $\Upsilon(5S)$  and taking  $\sigma(e^+e^- \rightarrow \Upsilon(5S)) = \sigma(e^+e^- \rightarrow b\bar{b}) = (0.340 \pm 0.016) \text{ nb}$  from our measurement [10], we obtain  $\mathcal{B}(\Upsilon(5S) \rightarrow \eta\Upsilon_J(1D)) = (4.82 \pm 0.92 \pm 0.67) \times 10^{-3}$ . This result agrees with theoretical estimates accounting for the effect of virtual  $B$ -meson loops [11]. We do not have significant evidence for  $e^+e^- \rightarrow \eta h_b(1P, 2P)$  nor  $e^+e^- \rightarrow \eta\Upsilon(1S)$ . We do not have direct evidence for the presence of the three states of the  $\Upsilon_J(1D)$  triplet and derive 90% CL upper limits on the fraction of  $J = 1$  and  $J = 3$  states with respect to the  $J = 2$  state.



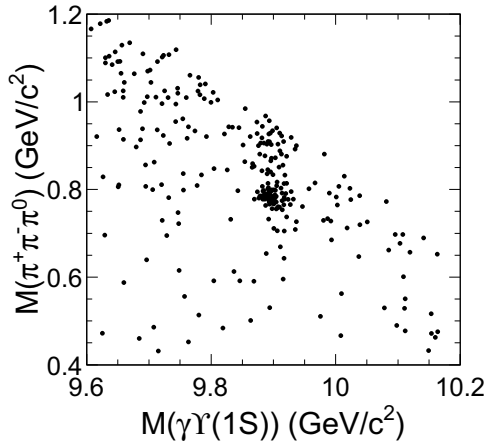
**Figure 6.**  $M_{\text{miss}}(\eta)$  distribution after subtraction of the fitted background.

## 6 Observation of $e^+e^- \rightarrow \pi^+\pi^-\pi^0\chi_{bJ}$ at 10.867 GeV

A data sample of  $118 \text{ fb}^{-1}$  collected at 10.867 GeV has been used to study  $\pi^+\pi^-\pi^0$  transitions between the  $\Upsilon(5S)$  and  $\chi_{bJ}$ ,  $J = 0, 1, 2$ , with subsequent  $\chi_{bJ} \rightarrow \gamma\Upsilon(1S)$ ,  $\Upsilon(1S) \rightarrow l^+l^-$ ,  $l = e, \mu$  decays [12].

Figure 7 shows the scatter plot of  $M(\pi^+\pi^-\pi^0)$  vs.  $M(\gamma\Upsilon(1S))$ . In addition to the clear  $\omega$  signal in the  $\chi_{bJ}$  mass region, there is an obvious accumulation of  $(\pi^+\pi^-\pi^0)_{\text{non-}\omega}$  events above the  $\omega$  mass. A two-dimensional fit gives the  $\omega\chi_{bJ}$  and  $(\pi^+\pi^-\pi^0)_{\text{non-}\omega\chi_{bJ}}$  yields. Figure 8 shows the  $\pi^+\pi^-\pi^0$  mass projection (left) with the obvious  $\omega$  signal and evidence for non- $\omega$  events, and the  $\gamma\Upsilon(1S)$  mass projection within (center) and outside (right) the  $\omega$  region with clear  $\chi_{b1}$  and  $\chi_{b2}$  signals. The fit results are summarized in Table 5. No excess of  $\chi_{b0}$  events above expected backgrounds is observed. The branching fractions of the three-pion transitions are large and of the same order as two-pion processes.

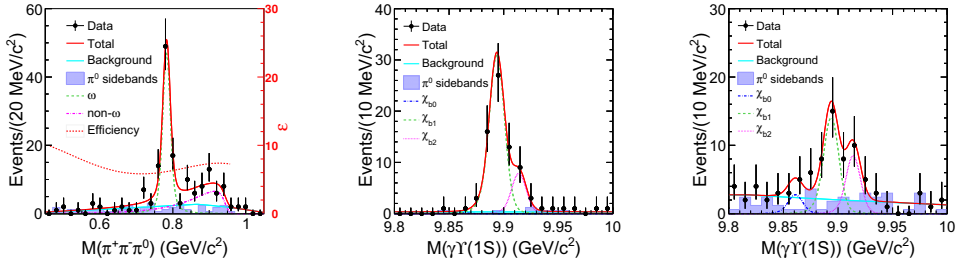
We also search for the  $X(3872)$ -like state  $X_b$  in the process  $e^+e^- \rightarrow \gamma X_b$ ,  $X_b \rightarrow \omega\Upsilon(1S)$  and observe no excess of events over the expectation from the  $\omega\chi_{bJ}$  final states. The upper limit is  $\mathcal{B}(\Upsilon(5S) \rightarrow \gamma X_b) \mathcal{B}(X_b \rightarrow \omega\Upsilon(1S)) < 2.9 \times 10^{-5}$  at 90% CL.



**Figure 7.** Scatter plot of  $M(\pi^+\pi^-\pi^0)$  vs.  $M(\gamma\Upsilon(1S))$  for selected  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma\Upsilon(1S)$  events.

**Table 5.** Results of the fits

Mode	Yield	Sign., ( $\sigma$ )	$\mathcal{B}$ , $10^{-3}$
$3\pi\chi_{b1}$	$80.1 \pm 9.9$	12	$1.85 \pm 0.23 \pm 0.23$
$3\pi\chi_{b2}$	$28.6 \pm 6.5$	5.9	$1.17 \pm 0.27 \pm 0.14$
$\omega\chi_{b1}$	$59.9 \pm 8.3$	12	$1.57 \pm 0.22 \pm 0.21$
$\omega\chi_{b2}$	$12.9 \pm 4.8$	3.5	$0.60 \pm 0.23 \pm 0.15$
$(3\pi)\text{non-}\omega\chi_{b1}$	$23.6 \pm 6.4$	4.9	$0.52 \pm 0.15 \pm 0.11$
$(3\pi)\text{non-}\omega\chi_{b2}$	$15.6 \pm 5.4$	3.1	$0.61 \pm 0.22 \pm 0.28$

**Figure 8.** Projections of: (left)  $M(\pi^+\pi^-\pi^0)$  for  $9.8 < M(\gamma Y(1S)) < 10$  GeV, (center)  $M(\gamma Y(1S))$  in the  $\omega$  region, (right)  $M(\gamma Y(1S))$  outside of the  $\omega$  region.

Finally, we search for  $Y(6S) \rightarrow \omega\chi_{bJ}, \phi\chi_{bJ}$  using scan data near 10.867 and 11.020 GeV [13]. We observe  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\chi_{b1}$  near  $Y(6S)$  and find evidence for  $\omega\chi_{bJ}$  while there is no significant signals for  $\phi\chi_{bJ}$  from 10.96 to 11.05 GeV.

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## References

- [1] E. Guido *et al.*, Phys. Rev. D **96**, 052005 (2017)
- [2] C. Patrignani *et al.*, Chin. Phys. C **40**, 100001 (2016)
- [3] E. Guido *et al.*, Phys. Rev. Lett. **121**, 062001 (2018)
- [4] M.B. Voloshin, Mod. Phys. Lett. A **26**, 773 (2011)
- [5] U. Tamponi *et al.*, Phys. Rev. Lett. **115**, 142001 (2015)
- [6] F.-K. Guo, C. Hanhart and U.-G. Meissner, Phys. Rev. Lett. **105**, 162001 (2010)
- [7] S. Godfrey and J.L. Rosner, Phys. Rev. D **66**, 014012 (2002)
- [8] D.-Y. Chen, X. Liu and T. Matsuki, Phys. Rev. D **87**, 094010 (2013)
- [9] U. Tamponi *et al.*, Eur. Phys. J. **78**, 633 (2018)
- [10] S. Esen *et al.*, Phys. Rev. D **87**, 031101 (2013)
- [11] B. Wang, D.Y. Chen and X. Liu, Phys. Rev. D **94**, 094039 (2016)
- [12] X.H. He *et al.*, Phys. Rev. Lett. **113**, 142001 (2014)
- [13] J.H. Yin *et al.*, arXiv:1806.06203