

Nucleosynthesis of light trans-Fe isotopes in ccSNe: Implications from presolar SiC-X grains

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Abstract. This contribution presents an extension of our r-process parameter study within the high-entropy-wind (HEW) scenario of core-collapse supernovae (ccSNe). One of the primary aims of this study was to obtain indications for the production of classical p-, s- and r-isotopes of the light trans-Fe elements in the Solar System (S.S.). Here, we focus on the nucleosynthesis origin of the anomalous isotopic compositions of Zr, Mo and Ru in presolar SiC X-grains (SNe grains). In contrast to the interpretation of other groups, we show that these grains do not represent the signatures of a ‘clean’ stellar scenario, but rather, are mixtures of an exotic nucleosynthesis component and S.S. material. We further confirm the results of our earlier studies whereby sizeable amounts of all stable p-, s- and r-isotopes of Zr, Mo and Ru can be co-produced by moderately neutron-rich ejecta of the low-entropy, charged-particle scenario of ccSNe (type II). The synthesis of these isotopes through a ‘primary’ production mode provides further means to revise the abundance estimates of the light trans-Fe elements from so far favoured ‘secondary’ scenarios like Type Ia SNe or neutron-bursts in exploding massive stars.

1 Introduction

The nucleosynthetic origin of the stable isotopes in the light trans-Fe region between Zn ($Z = 30$) and Ru ($Z = 44$) in the Solar System (S.S.) has been a fascinating subject for astrophysicists, astronomers, nuclear chemists and physicists, and cosmochemists for over 60 years [1 - 3]. In this multidisciplinary community, it is commonly believed that these elements are produced by various contributions from three different historical stellar processes: (i) the ‘p-process’ [4, 5], (ii) the ‘weak s-process’ ([6, 7] and refs. therein), and (iii) the ‘weak r-process’ ([8 - 10] and refs. therein).

Apart from the bulk S.S. isotopic abundances [11], more recent astronomical observations of *elemental* abundances in metal-poor halo stars [12 - 18] have revived and intensified the general interest in the nucleosynthesis of these elements beyond Fe and have motivated various theoretical studies with increasing realism (see extensive references in [19]). Supplementing these studies are *isotopic* analyses of meteoritic inclusions such as

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presolar grains and Ca,Al rich inclusions (see e.g. [20 - 24]). In particular, the interpretation of the anomalous Zr, Mo and Ru isotope compositions of SiC-X grains have so far defied a straightforward p-, s- or r-process explanation, requiring alternate nucleosynthesis scenarios. One such favoured process for the production of these light trans-Fe elements is the ‘secondary’ (i.e. metallicity dependant) neutron-burst (n-burst) occurring in the shocked He-shell of exploding massive stars [25 - 27]. Each of these models considered so far, however, are unable to co-synthesise all light p-, s- and r-process isotopes in S.S. proportions [11], and struggle even more so in reproducing the abundance ratio of the two most abundant p-isotopes ⁹²Mo and ⁹⁴Mo.

We offer a solution to these problems by following up on our earlier preliminary results [28, 29] exploring the ‘primary’ production of the light trans-Fe elements in a classical core-collapse supernova (ccSN), low-entropy, neutrino-driven-wind scenario.

2 Theory: Parametric core-collapse supernova HEW model

The notion of a high-entropy-wind (HEW), or neutrino-driven-wind (NDW), arises from considerations of the newly born proto-neutron star in ccSNe. In this scenario neutrinos interact with matter of the outermost neutron-star layers, leading to proton-rich and moderately neutron-rich HEW ejecta, with initially high entropies [30, 31]. In this present paper, as in our earlier publications [28, 32, 33], the nucleosynthesis calculations up to the charged-particle (CP) freezeout were performed with continuously extended versions of the Basel network code (see [34]), following the description of adiabatically expanding homogeneous mass zones [35].

After CP (α) freezeout, the expanding (and eventually ejected) mass zones from the outer neutron-star layers have different initial entropies ($S \approx T^3/\rho$ [k_B/baryon]; T: temperature, ρ : matter density) so that the overall explosion represents a superposition of different entropy ‘intervals’, correlated with (1) different electron abundances ($Y_e = Z/A$), (2) different ratios of free neutrons to ‘seed nuclei’ (Y_n/Y_{seed}) for the ensuing r-process, and eventually also with (3) different expansion velocities (V_{exp}), which determine the respective durations of the α -freezeout (τ_α) and the r-process (τ_r). With the assumption that each equidistant entropy interval contributes an equal amount of ejected matter (see [36] for details), the above correlations within our HEW model can be expressed by a simple ‘r-process strength function’, $Y_n/Y_{seed} \approx V_{exp} \times (S/Y_e)^3$. Using this parameterised approach, our HEW model is able to reproduce the astronomical and cosmochemical observations of different r-process ‘components’ using different S and Y_n/Y_{seed} ranges. The sum total of this multiplicity of r-process types has resulted in our complex S.S. r-process ‘blend’ composition.

Taking $Y_e = 0.45$ to represent a typical case of a moderately neutron-rich ejecta, the lowest entropy range ($S \leq 50$) represents the normal, rapid α -rich freezeout without free neutrons ($Y_n/Y_{seed} \approx 10^{-14}$), with a primary production of mainly stable or close to stable isotopes in the region of Fe to Sr (see second column of Table 1 in [32]). Moving onto a higher S-range ($50 < S \leq 100$; see column 3 of Table 1 in [32], with $Y_n/Y_{seed} \approx 1$ for $S = 100$) there are not yet enough free neutrons available to start a real neutron-capture (r-) process. However, under these S -conditions at freezeout, the seed composition is already shifted to the neutron-rich side of β -stability, including the well-known β -delayed neutron isotopes in the $80 < A < 100$ mass region. In the next higher S -range ($100 < S \leq 150$) of our HEW model, the density of free neutrons ($1 \leq Y_n/Y_{seed} \leq 13$) becomes high enough to start a ‘weak’ r-process up to the rising wing of the $A \approx 130$ S.S.-r N_\odot peak. Finally, for high entropies of $150 < S \leq 280$, now with $Y_n/Y_{seed} \approx 155$, our HEW parameter approach predicts quite a robust ‘main’ r-process starting with the $N = 82$ r-progenitor isotopes of ⁴³Tc to ⁴⁵Rh

at the onset of the $A \approx 130$ peak extending beyond the $N_{\odot,r}$ peak at the $N = 126$ shell closure up to the actinide region.

Initially, the HEW model was successfully applied to the light trans-Fe elemental abundance patterns of metal-poor halo stars [32, 34] and later the S.S. isotopic abundances [28] whereby we discussed for the first time the possibility of a *primary* co-production of all p-, s- and r-process isotopes between ^{64}Zn and ^{104}Ru within the low-S, CP component of the HEW. As an example, the co-production of all 7 Mo isotopes over different S intervals is illustrated in Fig. 1. Now we focus our attention on a third set of observations: the anomalous isotopic pattern of the three neighbouring even-Z elements Zr, Mo and Ru in presolar silicon carbide X-grains [20, 21] building on our earlier work [19, 28, 37].

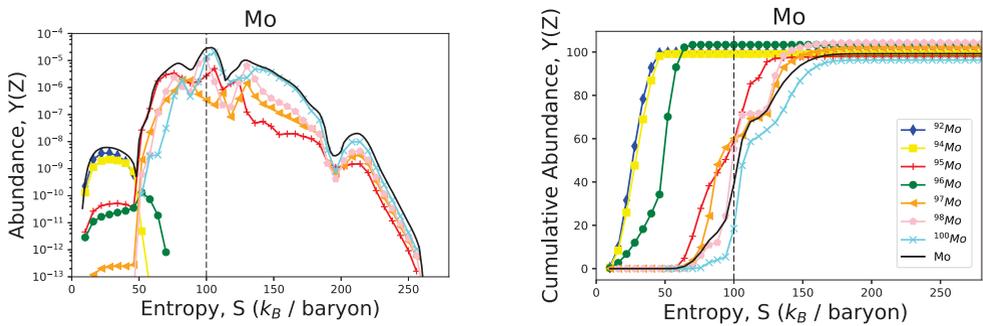


Fig. 1. Isotopic yields (left) and cumulative isotopic yields (right) for Mo as a function of cumulative entropy bins, for the case $Y_e = 0.45$. CP component ($S \leq 100$) and n-capture component ($S > 100$).

3 Observations: presolar silicon carbide-X grains

Silicon carbide (SiC) grains are one of the best studied presolar grain types (see [38, 39] and refs. therein). The majority of SiC grains (*mainstream grains*) have compositions (e.g. low $^{12}\text{C}/^{13}\text{C}$, high $^{14}\text{N}/^{15}\text{N}$ relative to S.S.) indicative of formation around thermally pulsating asymptotic giant branch (AGB) stars, whereas a rare subtype ($\approx 1\%$; *Type-X grains*) have isotopic signatures (elevated ^{12}C , ^{15}N , ^{28}Si relative to S.S. and excesses of ^{26}Mg , ^{44}Ca , ^{49}Ti) that are more characteristic of explosive scenarios such as ccSNe ([21], [26] and refs. therein). The light element (up to Fe) compositions permit us to regard SiC-X grains as supernova condensates (SUNOCONS; see [26] and refs. therein), but the light trans-Fe isotopic compositions of SiC-X grains have so far evaded a straightforward classical (p-, s-, r-) interpretation ([21, 22]), showing instead some agreement with the n-burst model of [25, 26].

In this contribution we focus largely on Mo, due to the increased robustness of the Mo isotope data. Using the standard cosmochemical conventions (e.g. see [19]), the isotopic compositions of the grains ($^i x/^k x$; $x = \text{Mo}$) are reported as deviations from the S.S. composition ($^i x/^k x_{\odot}$) in parts per thousand ($\delta^i x_k$), where i represents the target isotope and k represents the normalisation isotope. The grains are characterised by a large range of isotopic deviations from S.S.: i.e. depletions in the classical p- ($^{92,94}\text{Mo}$) and r- (^{100}Mo) isotopes, enrichments in the largely s-isotopes ($^{95,98}\text{Mo}$), whereas the s-only isotope (^{96}Mo) is present in almost identical abundances as ^{97}Mo (the normalising isotope). As for Zr, the SiC-X grains are characterised by depletions relative to ^{90}Zr ($^i \text{Zr}/^{90}\text{Zr} \leq 0.5$, $i = 91, 92, 94, 96$). The Ru isotope signatures in these grains are more complex and the analysis hindered as Ru isotope data are only available for two SiC-X grains, with relatively large uncertainties. Regardless, we find that the lighter isotopes ($^{96,98,99,100}\text{Ru}$) are on average under-abundant relative to ^{101}Ru , whereas ^{104}Ru is present in similar proportions as ^{101}Ru ,

and ^{102}Ru is over-abundant relative to ^{101}Ru . In all cases it is evident that the complex isotopic signature of these grains is not representative of a classical p-, s- or r-process.

Plotting the isotopic data in *cosmochemical* three-isotope space (e.g. $^{100}\text{Mo}/^{97}\text{Mo}$ - $^{113}\text{Mo}/^{97}\text{Mo}$; as explained in [19]), the SiC-X grains define a linear correlation for Mo and Zr isotopes (Fig. 2). These linear trends with the S.S. composition at one extreme and the SiC-X grain B2-05 on the other end (see Fig. 2) are interpreted as *mixing lines*, which strongly suggest that SiC-X grains are admixtures of two distinct nucleosynthetic components (or end members), as already recognised by [22]. Whereas the data support one end-member having a S.S. composition, we do not claim that the composition of B2-05 (other extreme of mixing line) reflects that of the second end-member, but rather B2-05 is the ‘purest’ grain with the cleanest signature of the SiC-X grain source. Thus we argue that SiC-X grains do not represent pure nucleosynthetic signatures from a single process but are best explained as a mixture of an exotic nucleosynthesis component - SiC-X end-member (SiC-X_{EM}; approximated by grain B2-05) - with homogenised stardust of S.S. composition. The isotopic compositions of grain B2-05 can thus be used to constrain the isotopic signatures of the stellar source where SiC-X grains formed (see second column, Table 1).

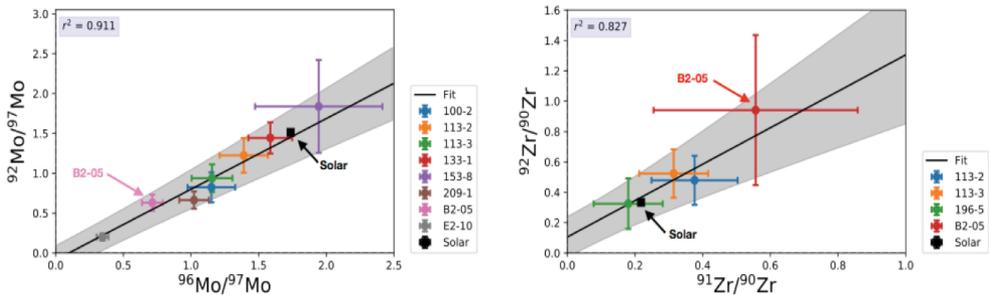


Fig. 2. Mo and Zr three-isotope plots for SiC-X grains (2σ uncertainties). 2D data fit (line), associated 2σ errorband (shaded area) and quality of fit (r^2) also shown. See [19] for details on grain E2-10 (excluded from this analysis).

4 Searching for the stellar source of SiC-X grains

We now consider new and updated classical models (s-, r-, p-, n-burst) alongside our HEW scenario as potential candidates for the exotic SiC-X end-member (SiC-X_{EM}). Selected isotopic ratios from these stellar sources (described below and in more detail in [19]) are given in Table 1, alongside the experimental constraints on the SiC-X_{EM} composition.

Classical and updated s-, r-, p-process: s-process models from [40] through to [41], and the diverse scenarios highlighted in the F.R.U.I.T.Y database [42], are all generally characterised by the absence of ^{92}Mo , and high $^{96}\text{Mo}/^{97}\text{Mo}$ and $^{98}\text{Mo}/^{97}\text{Mo}$ relative to SiC-X_{EM}, ruling out the s-process as the nucleosynthetic source of SiC-X grains (see Fig. 3). r-process yields are inferred using the r-residual method using the same aforementioned s-process models [40 - 42]. The resulting r-process signatures are over-abundant in ^{100}Mo relative to SiC-X grains, and show no signs of $^{92,94}\text{Mo}$ (classical p-only) or ^{96}Mo (shielded from the r-process pathway by ^{96}Zr) making the r-process an unlikely candidate. The improved yields (see [19]) of p-process nucleosynthesis in Type-Ia SNe [43] are preferred over earlier work on electron-capture SNe of AGB stars [44]. Despite the ‘secondary’ nature of this process, resulting from the use of an enhanced s-seed distribution in the progenitor AGB star, large excesses in the p-nuclides ($^{92,94}\text{Mo}$) and under-abundances of ^{97}Mo relative to all other Mo isotopes allow us to eliminate p-process nucleosynthesis [43] as the source of SiC-X grains.

n-burst: as already discussed in [22] and shown in Table 1 and Fig. 3, the *n*-burst model [25] succeeds to some extent in explaining the anomalous Mo (and Zr) isotope signatures in SiC-X grains, and to a lesser extent Ru (where too little $^{96,98}\text{Ru}$ is synthesised). However we remind the reader that (1) the concordance for $^{95}\text{Mo}/^{97}\text{Mo}$ between the *n*-burst model [26, 27] and data results solely from SiC-X grains having a close to S.S. $^{95}\text{Mo}/^{97}\text{Mo}$ value *and* the *n*-burst model naturally predicting S.S. $^{95}\text{Mo}/^{97}\text{Mo}$ values due to its dependence on an initial S.S. seed composition, and (2) although the $^{92}\text{Mo}/^{97}\text{Mo}$ and $^{94}\text{Mo}/^{97}\text{Mo}$ predictions from the *n*-burst satisfy the requirements for the SiC-X_{EM} composition (see Table 1), ^{92}Mo and ^{94}Mo are ultimately synthesised in very small quantities ($^{92,94}\text{Mo}/^{97}\text{Mo} \approx 10^{-3}$). These points suggest that most of the p-only ^{92}Mo and ^{94}Mo present in SiC-X grains arise largely from the S.S. component and not the *n*-burst component. The same is true for ^{96}Ru and ^{98}Ru (see Table 1).

HEW component: Continuing with the analysis initially presented in [19, 28, 29, 34, 36] we compute the Mo isotope ratios for cumulative entropy zones (from $S = 10$ k_B/baryon up to ≈ 270 k_B/baryon). For each cumulative entropy band, we mix the corresponding (cumulative) isotopic ratios with a S.S. composition to generate mixing lines. A 2D ordinary least squares fit of the mixing lines to the SiC-X data in three-isotope space are used to constrain the optimum values of cumulative entropies (*S*-range) to consider. The best fit for Mo isotopes is obtained for the case $Y_e = 0.45$ with cumulative- $S \approx 94$ k_B/baryon. Corresponding Mo isotope ratios are shown in Table 1 (column 3) and Fig. 3. These predictions – ‘primary’ HEW scenario – for $^{92}\text{Mo}/^{97}\text{Mo}$ and $^{94}\text{Mo}/^{97}\text{Mo}$ fall within the range of allowed SiC-X_{EM} compositions and are comparable to the ‘secondary’ *n*-burst predictions (Fig. 3). The $^{95}\text{Mo}/^{97}\text{Mo}$ value, which assumes close to S.S. values, is almost reproduced in our model (see Table 1), and the heavier isotopes $^{98}\text{Mo}/^{97}\text{Mo}$ and $^{100}\text{Mo}/^{97}\text{Mo}$ fall within a factor of two of the corresponding SiC-X_{EM} values. Finally, although ^{96}Mo is under produced ($^{96}\text{Mo}/^{97}\text{Mo} = 6.69 \times 10^{-5}$), it does satisfy the SiC-X_{EM} constraint ($^{96}\text{Mo}/^{97}\text{Mo} \leq 0.638$). A similar analysis for Zr reveals that the best fit between HEW theory and SiC-X data occur for slightly different conditions ($Y_e = 0.43$, cumulative- $S \approx 76$ k_B/baryon), whereas preliminary analyses of Ru require slightly higher electron fractions and entropies ($Y_e \approx 0.47$, cumulative- $S \approx 120$ k_B/baryon). Overall, the best HEW model fits for Zr, Mo and Ru occur for the low- S , CP-component of the HEW for a very small Y_e - S parameter window, indicating a consistent set of astrophysical conditions in the HEW of ccSNe.

TABLE 1: Mo isotope compositions of SiC-X end-member and various nucleosynthetic processes.

	SiC-X _{EM} ^a	This work ^b	<i>n</i> -burst ^c	S.S.(s) ^d	S.S.(r) ^e	SN-Ia ^f
ⁱ Mo/ ^k Mo:						
$^{92}\text{Mo}/^{97}\text{Mo}$	≤ 0.528	2.74×10^{-3}	1.43×10^{-3}	0	0	≈ 27
$^{94}\text{Mo}/^{97}\text{Mo}$	≤ 0.238	1.73×10^{-3}	3.28×10^{-3}	0.013	0	≈ 18
$^{95}\text{Mo}/^{97}\text{Mo}$	≈ 1.649	2.321	1.540	1.801	1.382	≈ 5
$^{96}\text{Mo}/^{97}\text{Mo}$	≤ 0.638	6.69×10^{-5}	0.010	3.27	0	≈ 4
$^{98}\text{Mo}/^{97}\text{Mo}$	≤ 1.133	1.654	0.379	3.28	1.247	≈ 4
$^{100}\text{Mo}/^{97}\text{Mo}$	≤ 0.390	0.637	0.095	0.072	2.683	≈ 2
$^{92}\text{Mo}/^{94}\text{Mo}$	≥ 2.578	1.587	0.437	0	0	1.527

^a SiC-X_{EM} limits. ^b Best case scenario for HEW nucleosynthesis occurs at $Y_e = 0.45$, $S_{\text{cum}} = 94$ (for Mo). ^c *n*-burst yields [22, 26]. ^d s-process yields [41]. ^e r-residuals [11, 41]. ^f p-process yields [43].

5 Conclusions

In the present paper we have shown selected results from an extension of our earlier large-scale parameter study of the ccSN-HEW scenarios with a focus on its low-entropy ($S \leq 100 - 150$, $Y_n/Y_{seed} \leq 1$) charged-particle component. We confirm that for moderate electron abundances in the range $0.44 \leq Y_e \leq 0.49$, all p-, s- and r-process isotopes in the light trans-Fe region between Zn ($Z = 30$) and Ru ($Z = 44$) can be co-produced in substantial yields. In this nucleosynthesis scenario, no initial S.S. or S.S.-modulated ‘seed’ composition (already containing the p-isotopes) is invoked as in e.g. [26, 43]. Hence, the low- S component of the ccSN-HEW seems to be the main site of the *primary* production of the light p-isotopes, even resulting in a fair reproduction of the S.S. abundance ratio of the two most prominent p-isotopes ^{92}Mo and ^{94}Mo .

Furthermore, particular attention has been directed towards the nucleosynthesis interpretation of the anomalous isotopic compositions of the stable isotopes of Zr, Mo and Ru reported in SiC-X grains. Our geochemical analysis demonstrates that the measured grain data do not represent ‘clean’ nucleosynthesis signatures, but are a mixture of a minor, initially unknown exotic component with S.S. material. Therefore, discussions about the possible isotopic origins of these admixtures (SiC-X grains), e.g. as presented in [45] are questionable. Only after correcting for this S.S. ‘contamination’, by way of identifying the purest grain, may we proceed with explaining the isotopic compositions of these grains, which we do so in a consistent and realistic astrophysical way within a narrow band of $Y_e - S$ conditions in the charged-particle component of our ccSN-HEW. Finally we postulate that these S.S.-corrected SiC-X grain compositions are probably the only ‘clean’ signature of a standard ccSN-HEW scenario identified so far – without containing additional r-process admixtures from other explosive scenarios such as magnetorotational SN-Jets or neutron-star merger events usually observed in metal-poor halo stars.

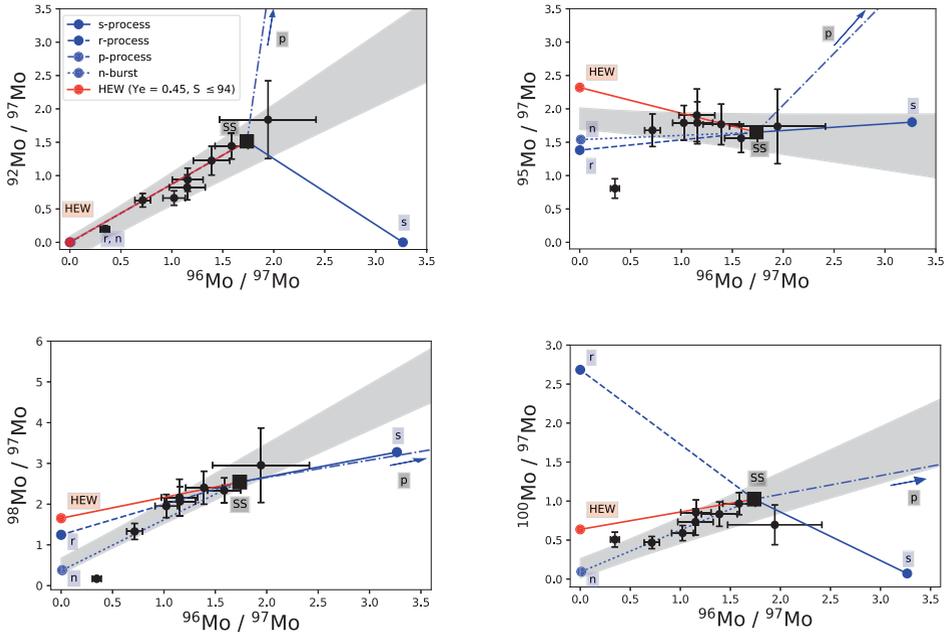


Fig. 3. Mo three-isotope plots for SiC-X grains with mixing lines for various nucleosynthetic end-members (see main text). Data uncertainties are 2σ . The error bands obtained from the 2D data fits (as in Fig. 2) are displayed as shaded areas. Filled circles indicate end-member compositions.

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