**class_sz I: Overview**

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**Abstract.** class_sz is a versatile, robust and efficient code, in C and Python, optimized to compute theoretical predictions for a wide range of observables relevant to cross-survey science in the Stage IV era. The code is public at https://github.com/CCLASS-SZ/class_sz along with a series of tutorial notebooks (https://github.com/CCLASS-SZ/notebooks). It will be presented in full detail in paper II. Here we give a brief overview of key features and usage.

## 1 Introduction

With *Planck* and *WMAP* full-sky observations of the Cosmic Microwave Background (CMB), one of the key numerical and theoretical challenges was to accurately predict the CMB angular anisotropy power spectra in temperature and polarisation, sourced by primordial universe physics, Big Bang Nucleosynthesis, recombination, reionisation, and the Universe’s expansion over the full cosmic history. The first numerical code that incorporated all of the relevant physics while achieving an efficient computing time was CMBFAST in 1996 [1]. It was followed by the release of two subsequent codes built on the same set of ideas as CMBFAST: *camb* in 2000 [2] and *class* in 2011 [3]. Since then, *camb* and *class* have been used in thousands of publications, including by the *Planck* and *WMAP* collaborations, and continue to be used in the analysis pipelines of ground based CMB observatories today (e.g., the Atacama Cosmology Telescope (ACT) and the South Pole Telescope (SPT)) and tomorrow (e.g., the Simons Observatory (SO) and CMB-S4).
With ACT and SPT, as well as forthcoming SO and CMB-S4 low-noise and high-resolution multi-frequency maps of the extragalactic sky, a new scientific window is opening up: we can now measure the CMB anisotropies at arcminute scales. Their properties are dictated by the interaction of CMB photons with matter, during the formation of the Large Scale Structure (LSS) of the Universe. The dominant effects responsible for this so-called secondary CMB anisotropies are weak lensing by dense structure forming regions and inverse-Compton scattering between CMB photons and hot electrons in the Intracluster Medium (ICM) and Circum Galactic Medium (CGM), i.e., the Sunyaev–Zeldovich (SZ) effect. Furthermore, on small scales, the sky temperature anisotropy receives contributions from other sources, such as the Cosmic Infrared Background (CIB) light from star-forming galaxies and radio emission from active galactic nuclei, so that the CMB is generally a sub-dominant contribution. Thus, the small-scale temperature anisotropy is a complicated mixture sourced by different physical effects.

Fortunately, we have a good theoretical understanding of these physical effects. Within a cosmological model and with a relatively small number of astrophysical assumptions, we can precisely predict the small-scale temperature anisotropy. Moreover, using galaxy survey data, we can construct estimators based on statistical cross-correlations that can single out different physical processes. For instance, we can measure the cross-correlations between the SZ effect and galaxies at various redshifts, making a tomography of the ICM, which we can then use to test galaxy formation models, see, e.g., Ref. [4]. We can also use the cross-correlations between galaxy and CMB weak lensing to probe the growth of structure at low-z and address the S8 tension (see, e.g., Ref. [5]). These scientific opportunities are huge and constitute one of the main driving forces of the field in the post-Planck era.

Extracting scientific information from small-scale temperature anisotropy and cross-correlation measurements comes with new theoretical and computational challenges. There are two powerful theoretical frameworks that enable us to make models and predictions for the interpretation of this new data: perturbation theory (including standard perturbation theory and Effective Field Theory of LSS, e.g., Ref. [6]) and the halo model formalism (see, e.g., Refs. [7–9]). Computationally, their implementation is challenging because one has to solve high-dimensional integrals (e.g., over comoving volume, halo masses, wavenumbers etc.) relying on many ingredients (halo mass function, halo bias, loop integrals, radial profile of tracers etc.). class_sz is one of the few numerical codes that solves these challenges simultaneously for a maximum number of observables. Another notable attempt is cc1, developed within the Vera Rubin Observatory collaboration [10].

Important features and performances of the code are described in the next sections.

2 Structure of class_sz

class_sz is built based on the Boltzmann code class; thus, everything that can be computed by class can be computed by class_sz. In class_sz, we have added three “modules” to the original class code. These are: class_sz.c: the core of the code, where all the important quantities are computed (e.g., power spectra, bispectra, halo mass function etc); class_sz_tools.c: less central functions, such as numerical routines for integration or interpolations; class_sz_clustercounts.c: SZ cluster number counts calculations. The python wrapper of class is extended to class_sz. We have added all required class_sz functions in classy.pyx to "cythonize" them. In addition, we created a submodule in the class_szfast.py file dedicated to interface neural network emulators with the C code (see 4 and ??).
3 General features, availability and tutorials

We have invested significant efforts to make the code as fast as possible. Notably, all large “for loops” are parallelized with OpenMP; integrals are either solved with an adaptive solver (borrowed from CosmoTherm [11]) or with Fast Fourier Transforms with the fftw3 library and the FFTLog algorithm when relevant. For a number of cosmological models, including Λ Cold Dark Matter (CDM), wCDM, and Σ\(m_ν\) + ΛCDM, class_sz can call high accuracy neural network emulators to predict the CMB \(C_ℓ\)'s and matter power spectrum. As a rule of thumb, we aim for all our calculations (for a given observable) to be completed in less than 0.2s\(^2\).

The code is available on GitHub https://github.com/CLASS-SZ/class_sz where it is regularly updated. Installation instructions are given in the README file and documentation will soon be provided. Once installed, one can carry out calculations using the C executable or within python code using the python wrapper classy_sz. A Google colab notebook with example calculations is available online at class_sz_colab.ipynb and can be run from any internet browser. In addition, we have provided an extensive set of notebooks that show how to obtain most classy_sz outputs, in a self-explanatory way. These notebooks are stored at: https://github.com/CLASS-SZ/notebooks.

4 Fast calculations of CMB and matter power spectra and fast MCMC’s

We have imported the high accuracy cosmopower\(^3\) emulators for CMB TT, TE, EE angular anisotropy power spectra developed in Ref. [12], building on previous work from Ref. [13]. This allows class_sz to predict these spectra in less than 50 ms, compared to around a minute if the calculations were to be done with class for the same accuracy requirements. Our accuracy requirements are such that our results are converged to better than 0.03σ’s of CMB-S4 across the entire multipole range between \(ℓ = 2\) and \(10^4\).

This means that we can run Markov Chains Monte Carlo (MCMC) analyses of CMB power spectra data and reach convergence within a few minutes, compared to \(\approx 1\) week if we were to run the analysis with class tuned at the same accuracy. See class_sz_tutorial.ipynb and cobaya notebooks.

The matter power spectrum is the fundamental building block for the modelling of all LSS observables. It is often computed by camb or class, which solve the density perturbation evolution equations. We have also imported matter power spectra emulators (developed in Ref. [12] too), so we can completely bypass the perturbation module of class and obtain interpolators for the linear and non-linear matter power spectra covering redshifts between 0 and 5 and wavenumbers between \(10^{-4}\) and 50 Mpc\(^{-1}\) in \(\approx 0.1\)s compared to minutes for the equivalent class calculation. Note that currently our non-linear prescription is the fiducial hmcode [14] calculation (i.e., dark-matter only) but we are planning to interface a wide range of power spectra emulators in the near future.

5 Bispectra: Effective formulas and halo model

We compute matter bispectra and bispectra between different tracers. For matter bispectra, we have implemented the standard perturbation theory Tree-level prediction as well as effective formulas from Ref. [15] and Ref. [16] to predict the bispectrum for non-linear scales. We

\(^2\)Of course, this depends on scales and number of cores used.

\(^3\)https://github.com/alessiospuriomancini/cosmopower
have also implemented the halo model bispectrum, predicting separately the 1, 2 and 3-halo terms. Currently implemented halo model bispectra include the matter bispectrum, the tSZ bispectrum and hybrid bispectra involving kSZ, tSZ, galaxies, and CMB weak lensing.

6 Halo mass function, halo bias and scale-dependent bias from primordial non-Gaussianity

Predictions for halo model observables are ensemble averages of radial tracer profiles over halo masses and redshifts. The abundance of halos as a function of mass and redshift is characterized by the halo mass function. In class_sz we have implemented several halo mass functions including the widely used Tinker formulas [17, 18], as well as other fitting formulas [19]. Other mass functions based on emulators are currently being implemented4. Similarly, we have fitting formulas for the first and second order biases following Ref. [18] and Ref. [20], respectively.

It is well-known that local primordial non-Gaussianity generates a scale dependence in the halo bias and that the effect is larger on large scales. class_sz can compute this scale-dependent effect following the standard calculation (see Ref. [21]). If the user requests $f_{NL} \neq 0$, the effect is propagated to all calculations that depend on the halo bias.

7 Thermal and kinetic SZ

class_sz uses the halo-model to compute auto- and cross-power spectra involving the thermal Sunyaev–Zeldovich (tSZ) effect. Several pressure profile models are implemented, including the Arnaud et al. [22] and the Battaglia et al. [23] generalized Navarro Frenk White (NFW) fitting formulas. One can request the radial pressure profile as a function of radius, or integrated quantities such as the mean Compton-$y$ parameter relevant to CMB spectral distortion. The thermal SZ power spectrum was the first observable to be implemented in class_sz and is described in detail in Ref. [24]. We show the integrand of $C_{\ell}^{\text{tSZ}}$ in Figure 1. An interactive version of this image is available online5. It is also possible to compute the tSZ power spectrum corresponding to a sub sample of halos determined by a selection function as was done in Ref. [25], which can shed light on the mass-dependence of the hydrostatic mass bias and the possible role of relativistic SZ [26]. We note that the class_sz Compton-$y$ calculations were used to benchmark the ccl implementation.

For the kinetic Sunyaev–Zeldovich (kSZ) effect, various gas density profiles that are currently available in class_sz include a simple NFW scaled by the baryon fraction, as well

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4see, e.g., https://github.com/SebastianBocquet/MiraTitanHMFemulator
5http://borisbolliet.github.io/Attachements/class_sz_szkernel-html.html
as the more realistic Battaglia et al. [27] (gNFW) and Schneider et al. [28] (Baryonic Correction Model) formulas that were directly fitted to hydrodynamical simulations. From these profiles, one can then compute the contributions to the angular power spectra of the kSZ effect based on a formula valid at small scales (see Ref. [29] for details).

8 Galaxy power spectra, shear and intrinsic alignment

Galaxy power spectra can be computed either within a linear bias model, e.g., $P_{gg} = b^2 P_L$, or from Halo Occupation Distributions. The HODs currently available are described in Ref. [30] where they were used with class_sz to characterize the galaxy-halo connection of the unWISE galaxies. Galaxy lensing magnification is implemented too (see Ref. [30]). We compute galaxy weak lensing power spectra, either in the linear bias approximation or within the halo model, and if requested, convert them to shear correlation functions in position space using mcfit\(^6\) Melin transforms [31]. Our class_sz shear calculations were benchmarked against those presented in Ref. [32]. Similarly, galaxy angular power spectra can be converted into clustering 2-point correlation functions so that class_sz can be used to perform 3x2 analyses as in Ref. [33]. For intrinsic alignment we have a simple Non Linear Alignment model that follows Ref. [34]. More intrinsic alignment models including TATT and halo-models will become available in the near future.

9 Cosmic infrared background

We have two halo models for the CIB: the Shang et al. [35] and the Maniyar et al. [36] models. The Shang et al. model was used in, e.g., the Planck 2013 CIB paper [37], the Websky simulations [38], and in Ref. [39]. The Maniyar et al. model implementation was carefully benchmarked against the original code\(^7\). We can compute auto- and cross-frequency power spectra at any frequency, as well as prediction for the CIB monopole. Ref [40] have used the CIB monopole implementation to predict the distortion caused by inverse Compton scattering of CIB photons against hot ICM electrons, see Ref.[40], although not accounting for intra-cluster scattering [41].

10 Cross-correlations

All the tracers described above can be cross-correlated and their cross-power spectra can be computed with class_sz. For instance, the cross-power spectrum between tSZ and CMB lensing measured from Planck PR4 data was analysed with class_sz in Ref. [42]. Another recent work that relied on class_sz for cross-correlation modelling is Ref. [43] where the authors proposed new component separation methods that incorporate information from cross-correlations between galaxies, CIB, and tSZ to better extract the CMB from multi-frequency maps. As a last example, a unique feature of class_sz is the prediction for projected-field kSZ\(^2\)-LSS power spectra (we refer to Ref. [29] for details).

11 SZ cluster counts

With precise weak lensing mass calibration that will be enabled by VRO and Euclid data, we expect promising constraints on the fundamental parameters of the universe from SZ selected

\(^6\)https://github.com/eealregit/mcfit
\(^7\)https://github.com/abhimaniyar/halomodel_cib_tsz_cibxtsz
cluster cosmology. Given a survey noise map and completeness function, class_sz can predict the abundance of SZ selected clusters in SZ signal-to-noise and redshift bins. Scaling relations and completeness functions for Planck (see Ref. [44] for a cluster cosmology analysis with class_sz), ACT and SO-like surveys are already implemented. In addition to predicting the cluster abundance, if a catalogue data is assumed, class_sz can also compute binned (see, e.g., Ref. [45]) and unbinned (see, e.g., Ref. [46]) likelihood values. The unbinned likelihood was developed in parallel to a new code called cosmocnc (Ref. [47]), specifically dedicated to cluster cosmology and which, for this particular purpose, is more general than class_sz.

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