

# Thermal behavior analysis of monolayer and bulk $UAl_3$ at room temperature

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**Abstract.**  $UAl_3$  has been widely used as a target material for the production of  $^{99}Mo$ . To safely produce radioactive isotopes from  $UAl_3$ , it is crucial to understand and predict the thermal behavior of  $UAl_3$ . Directly measuring the thermal properties of  $UAl_3$  due to the radiation generated in nuclear fuel material is challenging. As an alternative, using the molecular dynamics (MD) simulator LAMMPS, the thermal conductivities of monolayer and bulk  $UAl_3$  are predicted. In this study, it is primarily observed that the absence of the third-order anharmonic constant along the z-axis contributes to a higher thermal conductivity of monolayer  $UAl_3$  compared to bulk  $UAl_3$ . Furthermore, the calculated thermal conductivity of bulk  $UAl_3$  falls within the range of the measured values in the literature.

## 1 Introduction

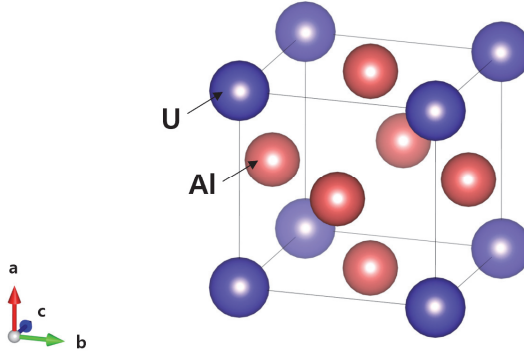
$^{99}Mo$ , formed through the nuclear fission of low-enriched uranium with  $^{235}U$  content of less than 20 wt.%, is a parent isotope of  $^{99m}Tc$ , widely utilized in medical imaging diagnostics.  $^{99m}Tc$  is known for its short half-time (half-life: 6 hours) and low radiation energy, resulting in low internal radiation exposure. Its excellent tissue penetration properties contribute to high diagnostic accuracy.  $^{99m}Tc$  can be synthesized in the form of labeled compounds that accumulate in most organs of the body, making it widely utilized in various diagnoses [1]. Currently, South Korea relies partially on imports for medical and industrial isotopes. To promote domestic self-sufficiency and facilitate international exports of the isotopes dependent on imports, 15 MWt open-tank-in-pool type Kijang research reactor (KJRR) is under construction. The target material to be used for  $^{99}Mo$  production in KJRR consists of a meat with spherical uranium aluminide ( $UAl_x$ ) particles dispersed in a pure aluminium matrix, surrounded by a cladding material made of aluminium alloy [2]. The uranium density of the meat is 2.6 g-U/cm<sup>3</sup> and the uranium enrichment is 19.75 wt.%  $^{235}U$ .  $UAl_x$  is predominantly composed of  $UAl_3$ , with the remainder being  $UAl_4$ . The target material is scheduled for neutron irradiation over a period of 7 days in KJRR, with an expected burnup of less than 5%  $^{235}U$ .

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## 2 Theoretical method

The crystal structure of  $UAl_3$  belongs to the cubic space group  $Pm\bar{3}m$ , as illustrated in Fig. 1, with a lattice constant of 4.26 Å. The MD simulator used for the thermal behavior analysis of  $UAl_3$  is LAMMPS (large-scale atomic/molecular massively parallel simulator) [3]. LAMMPS, developed collaboratively by Sandia national laboratory and Lawrence Livermore national laboratory, is an open-source, parallelized molecular dynamics package capable of solving large-scale problems. It supports parallel processing using MPI (message passing interface).



**Fig. 1.** Crystal structure of  $UAl_3$

The MD simulates the motion of molecules by calculating the forces between them, exploring the properties of materials. In other words, it iteratively calculates Newton's equations of motion for particles at the current time ( $t$ ) to determine the positions, velocities, forces, and other attributes of particles at the next time ( $t+\Delta t$ ), ultimately computing various physical properties. In MD, the most computationally demanding aspect is typically the calculation of forces between each pair of particles, which is done using a potential function.

The interatomic potential energy used in this study is defined using the many-body potential, MEAM (modified embedded-atom method) potential [4]. In the MEAM, the total energy of a system is approximated as:

$$E = \sum_i \left[ F_i(\bar{\rho}_i) + \frac{1}{2} \sum_{i \neq j} \phi_{ij}(r_{ij}) \right]$$

$F_i(\bar{\rho}_i)$  presents the embedding energy, indicating the energy change when an impurity atom occupies the site of  $i$ -atom with the background electron density of  $\bar{\rho}_i$ . As  $\bar{\rho}_i$  is determined by s, p, d, and f atomic electron densities, the term  $F_i(\bar{\rho}_i)$  reflects the many-body effects. The term  $\phi_{ij}(r_{ij})$  represents the pair potential when atoms  $i$  and  $j$  are separated by a distance  $r_{ij}$ . Table 1 lists the potential parameters for the Al-U [5] used in this study.

**Table 1.** Potential parameters of Al-U

Potential parameter	Value
$\alpha$	5.5364807
$E_c$	4.0435039
$r_e$ (Å)	3.0432685
$\bar{\rho}_{U/Al}^0$	2.2488211
$C_{min}(112)$	1.2094229
$C_{min}(121)$	0.2558103
$C_{min}(122)$	0.2019148
$C_{min}(221)$	0.4418066
$C_{max}(112)$	1.4792962
$C_{max}(121)$	2.0880558
$C_{max}(122)$	1.9424523
$C_{max}(221)$	1.0510265

$\alpha$  :  $\alpha = (9B\Omega E_c)^{1/2}$ , B is the bulk modulus and  $\Omega$  is the equilibrium atomic volume

$E_c$  : cohesive energy

$r_e$  : equilibrium nearest-neighbor distance

$\bar{\rho}_{U/Al}^0$  : background electron density for Al-U alloy

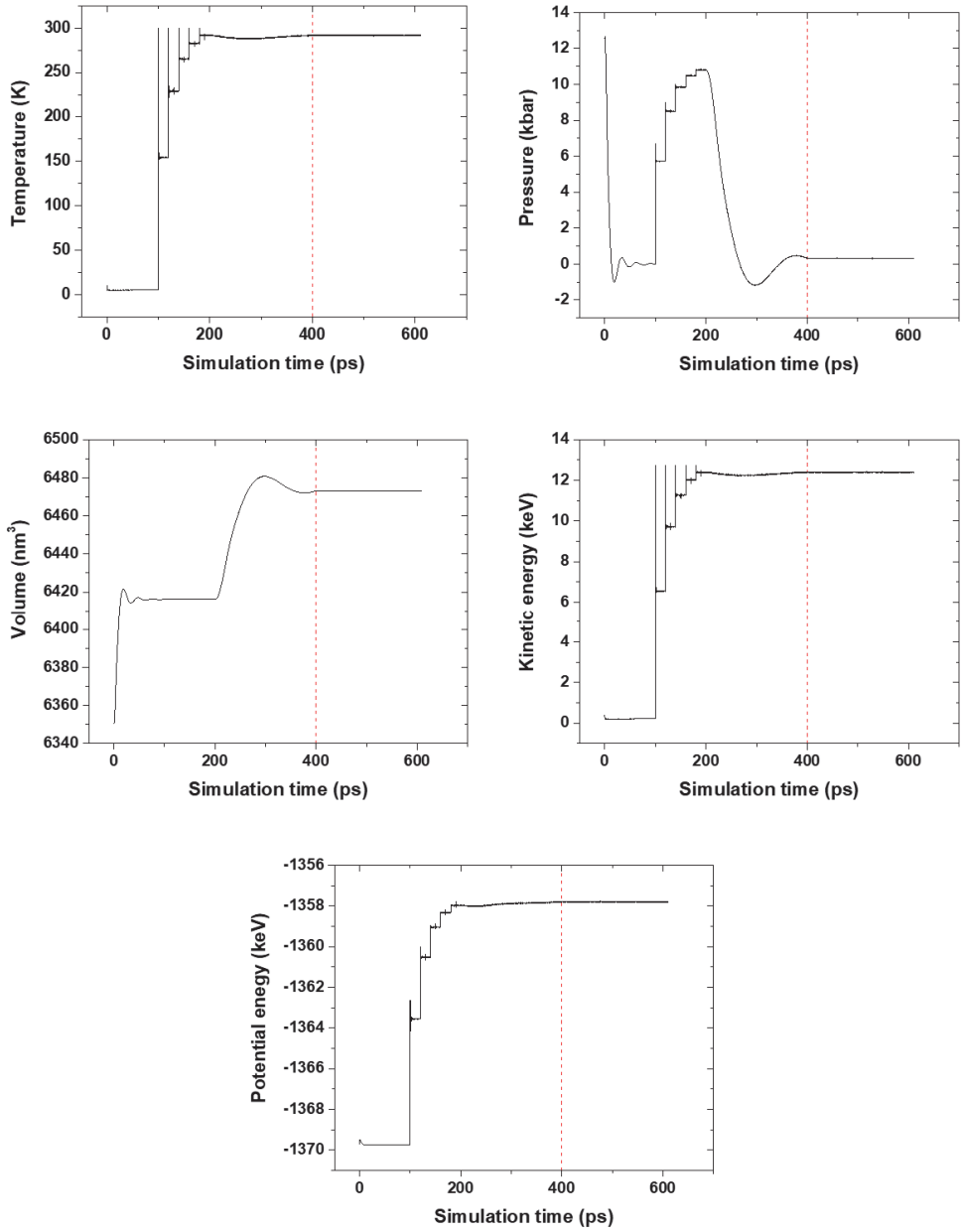
$C_{min}$ ,  $C_{max}$  : account for many-body screening effects

## 2.1 System minimization

For system stabilization, the Polak-Ribière version of the conjugate gradient method, known for faster convergence than gradient descent, was utilized. The time-integration algorithm employed the Velocity-Verlet method, which offers lower errors and simpler programming compared to the Euler method. Initial velocities of atoms were assigned using Gaussian random numbers. The ensemble methods NVE (microcanonical ensemble) and NPT (isothermal-isobaric ensemble) were applied.

The periodic boundary conditions for both the monolayer and bulk  $UAl_3$  are set as  $2347 \times 7 \times 1$  and  $2347 \times 7 \times 5$  which contain 65,716 and 328,580 atoms, respectively.

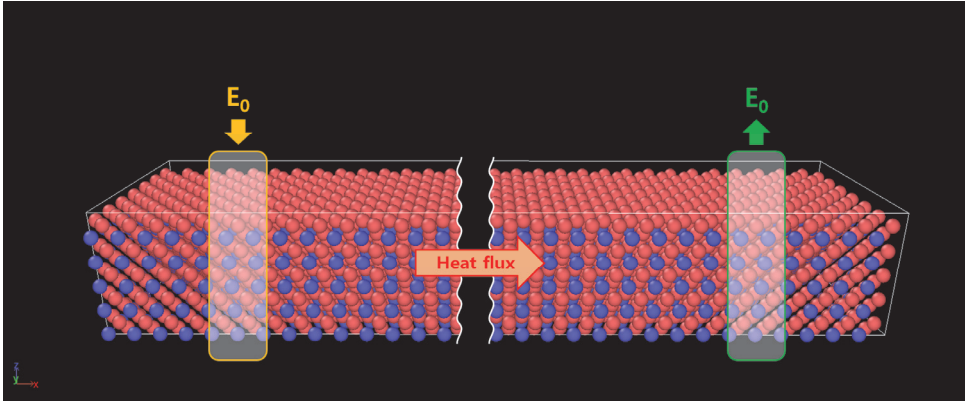
Figure 2 depicts the changes in temperature, pressure, and volume of the system, as well as the kinetic energy and potential energy of particles during the relaxation process. It is observed that each of these values generally stabilize after simulation time of approximately 400 ps.



**Fig. 2.** System relaxation process of  $UA_{13}$  (2347×7×5)

## 2.2 Calculation of thermal conductivity

The thermal conductivity evaluation method employed non-equilibrium molecular dynamics using direct methods [6] similar to experimental measurements. Applying heat at the 1/4 position and removing heat at the 3/4 position along the x-axis of the system, as depicted in Fig. 3, yields the heat flux ( $J_x$ ) by equation (1) when the system reaches equilibrium. Consequently, the temperature gradient ( $dt/dx$ ) of the system is calculated, and ultimately, the thermal conductivity ( $k_x$ ) is obtained through Fourier’s law in equation (2).



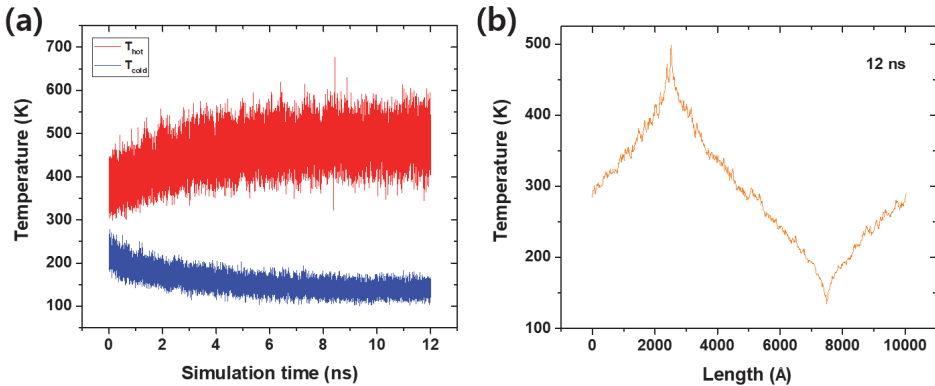
**Fig. 3.** Schematic of the simulation system to calculate thermal conductivity of UAl<sub>3</sub>

$$J_x = -\frac{1}{2} \frac{E_0}{A \times \Delta t} \quad (1)$$

$E_0$  represents the heat added to or removed from the system,  $\Delta t$  is the time interval during which the heat is applied, and  $A$  is the cross-sectional area of the system.

$$J_x = -k_x \frac{dT}{dx} \quad (2)$$

The timestep in this study is 1 fs. The example of the temperature profile for UAl<sub>3</sub> is shown in Fig. 4. It is observed that the system reaches a steady state at a simulation time of approximately 12 ns in Fig. 4(a).



**Fig. 4.** Temperature profiles of UAl<sub>3</sub> (2347×7×1)

## 2.3 Phonon analysis

For the analysis of thermal behaviour, phonon dispersion was calculated using ‘Phonon’ [7] fix provided by LAMMPS. The ‘Phonon’ fix receives the temporary positions of atoms in an equilibrium system, transforms it into reciprocal space to obtain the Green’s function coefficients. After a specific measurement, the time average of Green’s function coefficients is evaluated, and over a sufficiently long simulation, it can resemble an ensemble average. The force constant matrix is created based on the generated dynamical matrix. The results are recorded in log files and binary files. The binary files utilize the ‘Phana’ code for phonon frequency calculations. After reaching equilibrium, the ‘Phana’ code produces phonon dispersion curves.

## 3 Results and Discussion

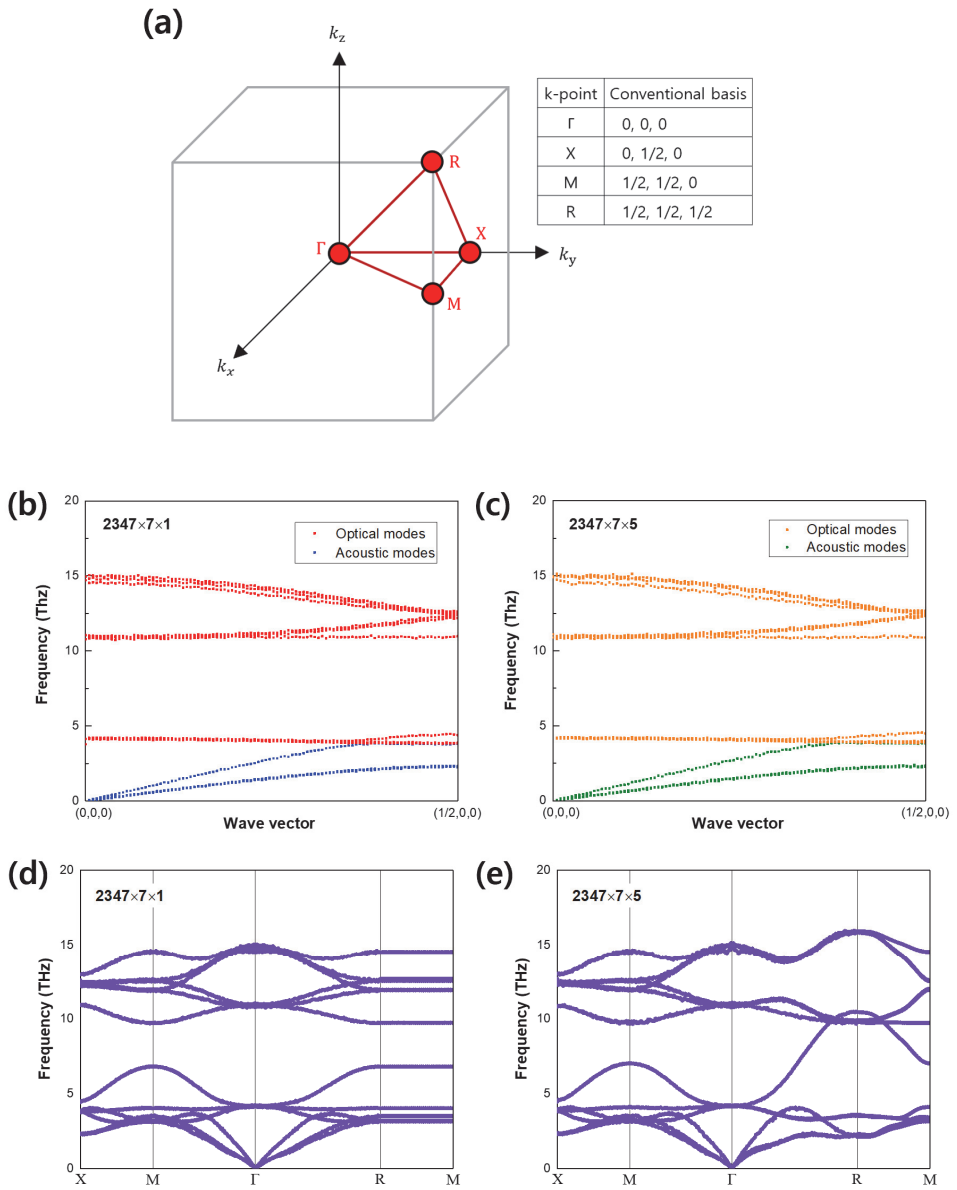
The thermal conductivities at room temperature for monolayer and bulk  $\text{UAl}_3$  calculated from time-averaged temperature profiles such as Fig. 4(b) are  $\sim 20.0$  W/m-K and  $\sim 9.4$  W/m-K, respectively.

The higher thermal conductivity of the monolayer than the bulk can be attributed to the faster phonon group velocity of the monolayer compared to the bulk, as observed in other materials [8]. However, the acoustic phonon group velocities along the  $(1/2, 0, 0)$  calculated from Figs. 5(b) and 5(c), indicate a nearly indistinguishable similarity between monolayer  $\text{UAl}_3$  and bulk  $\text{UAl}_3$ .

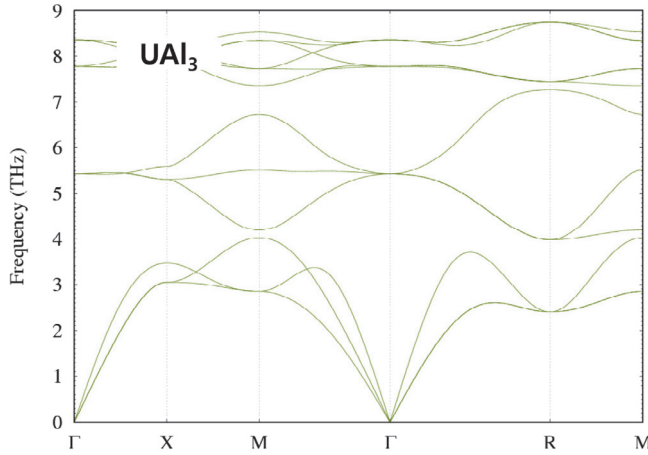
In the case of the monolayer, the absence of the third-order anharmonic constant along the z-axis has been reported to lead to a lower phonon scattering rate (inverse of phonon lifetime) calculated using the third-order anharmonic constant [8], contributing to explaining the higher thermal conductivity of the monolayer compared to the bulk. In Figs. 5(d) and 5(e), it is confirmed that due to the absence of the third-order anharmonic constant along the z-axis, the phonon group velocity along the R–M path of the phonon dispersion curve for monolayer  $\text{UAl}_3$  becomes zero, unlike bulk  $\text{UAl}_3$ .

The thermal conductivity of  $\text{UAl}_3$  calculated by MD simulations in this study was found to be lower than the values computed using ab initio molecular dynamics (AIMD) calculations in the literature [9]. In the phonon dispersion relations for bulk  $\text{UAl}_3$  calculated using AIMD calculation in Fig. 6, the acoustic phonon modes influencing thermal conduction are distinctly separated from the optical phonon modes. However, in the phonon dispersion relations obtained in this study, it is observed that acoustic and optical phonon modes overlap in Fig. 5. This overlap is considered one of the reasons explaining the lower thermal conductivity calculated by MD simulations.

In conclusion, the calculated thermal conductivity ( $\sim 9.4$  W/m-K) of the bulk  $\text{UAl}_3$  falls within the measured range of 4.18 to 12.55 W/m-K in the literature [10]. When considering the absence of phonon-defect scattering and phonon-electron scattering, MD simulations in this study seem to effectively simulate the thermal behavior of the bulk  $\text{UAl}_3$ .



**Fig. 5.** Phonon dispersion relations of  $UAl_3$  : (a) Brillouin zone of  $Pm\bar{3}m$ , (b,d) monolayer  $UAl_3$ , (c,e) bulk  $UAl_3$



**Fig. 6.** Phonon dispersion relations of  $\text{UAl}_3$  obtained using AIMD calculations at 300K [9]

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