

Physics case for an e^+e^- collider at 500 GeV and above

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Abstract. Some highlights of the physics case for running an e^+e^- collider at 500 GeV and above are discussed with a particular emphasis on the experimental access to the Higgs potential via di-Higgs and (at sufficiently high energy) triple Higgs production. The information obtainable from Higgs pair production at about 500 GeV is compared with the prospects for the HL-LHC and with the indirect information that can be obtained from a Higgs factory running at lower energies.

1 Introduction

There is wide support in the particle physics community for an e^+e^- “Higgs factory” as a near-future new particle collider. The design options of a circular or a linear collider have important implications for the c.m. energy that can be reached at these facilities. While the emission of synchrotron radiation limits the currently discussed circular e^+e^- colliders to energies up to about 350 GeV, significantly higher c.m. energies can be reached at a linear e^+e^- collider. The latter design choice also offers the possibility to start with a lower-energy machine, operating for instance at a c.m. energy of 250 GeV, and in a second stage to perform an upgrade to higher energies, either by upgrading the accelerating structures or by extending the tunnel length. In the present article^{1 2} some highlights of the physics case for running an e^+e^- collider at 500 GeV and above are discussed with a particular emphasis on the direct measurement of the Higgs pair production process $e^+e^- \rightarrow Zhh$ that becomes accessible at a c.m. energy of at least 500 GeV (in conjunction with additional information from the weak-boson fusion process $e^+e^- \rightarrow \nu_e \bar{\nu}_e hh$). Other important aspects of the physics programme of an e^+e^- collider running at a c.m. energy of 500 GeV and above will only be briefly touched upon, for more details see e.g. the recent reports [1–3] and references therein.

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2 Higgs potential, Higgs self-couplings and Higgs pair production processes

Many of the open questions of particle physics are related to the Higgs sector and in particular to the Higgs potential, which for this reason is often referred to as the “holy grail” of particle physics. In the Standard Model (SM) of particle physics a minimal form of the Higgs potential is postulated with a single Higgs boson that is an elementary particle.

The Higgs potential gives rise to electroweak symmetry breaking. Thus, information about the Higgs potential plays a crucial role in determining how the electroweak phase transition (EWPT) in the early universe took place. This in turn is important for a possible explanation of the observed asymmetry between matter and anti-matter in the universe in terms of electroweak baryogenesis. However, the actual form of the Higgs potential that is realised in nature and its physical origin are largely unknown up to now. The Higgs potential receives contributions from the detected Higgs boson h with a mass m_h of about 125 GeV and from all additional scalar fields that may be present but have not been detected so far. While the bilinear term, i.e. the coefficient of h^2 , is related to the measured value of m_h , the trilinear Higgs self-coupling, λ_{hhh} , i.e. the coefficient of h^3 , and the quartic Higgs self-coupling, λ_{hhhh} , i.e. the coefficient of h^4 , are only loosely constrained so far (and only weak bounds exist on contributions to the Higgs potential from additional fields).

The existing constraints on λ_{hhh} from the LHC have mainly been obtained from the searches for the Higgs pair production process, where in the gluon fusion channel a leading-order vertex diagram containing λ_{hhh} and the top Yukawa coupling y_t enters together with a box diagram involving the coupling factor y_t^2 . Because of a large destructive interference between the contributions from these two diagrams the total cross section for di-Higgs production changes very substantially, by about two orders of magnitude, if λ_{hhh} is varied around the SM value. The current upper bound on the di-Higgs production cross section from ATLAS and CMS translates into an upper limit on λ_{hhh} that is about 7 times larger than the (tree-level) SM value (and also a lower limit can be set), assuming that all other Higgs couplings besides λ_{hhh} are fixed to their SM values [4, 5] (this assumption can be relaxed by incorporating data from single Higgs production [6]).

While the existing bounds on λ_{hhh} are rather weak, they nevertheless already probe so far untested parameter regions of physics beyond the SM because loop corrections to λ_{hhh} can be much larger, by more than two orders of magnitude, than to the couplings of h to gauge bosons and fermions, see [7–9] for investigations of extended Higgs sectors and [10] for SMEFT analyses. A very significant upward shift in λ_{hhh} is also motivated in many scenarios giving rise to a strong first-order EWPT which is required for electroweak baryogenesis, see e.g. [11] for the case of the 2HDM, where the parameter region featuring a strong first-order EWPT and a potentially detectable gravitational wave signal at the future space-based observatory LISA is correlated with an enhancement of λ_{hhh} compared to the SM value by about a factor of 2.

At an e^+e^- linear collider with a c.m. energy of at least 500 GeV the Higgs pair production process $e^+e^- \rightarrow Zhh$ (and also the weak-boson fusion process $e^+e^- \rightarrow \nu_e\bar{\nu}_e hh$) can be measured directly and in a model-independent way. This is a qualitatively new feature distinguishing the physics capabilities of an e^+e^- collider at 500 GeV and above from the ones of Higgs factories at lower energies such as the CEPC, the FCC-ee and a lower-energy version of an e^+e^- linear collider. The impact of the direct measurement of the Higgs pair production processes on the determination of λ_{hhh} will be discussed in the next section.

First experimental constraints on the quartic Higgs self-coupling λ_{hhhh} can be obtained at the HL-LHC, see [12, 13] for recent exploratory studies, and be further improved at future

lepton colliders with c.m. energies beyond 1 TeV [12, 14–16], see the discussion in Sect. 6 below.

3 Determination of λ_{hhh} from the Higgs pair production processes at a 550 GeV e^+e^- collider in comparison to the prospects at the HL-LHC

While the current projections for the HL-LHC (for the combined integrated luminosity that is expected to be collected by ATLAS and CMS) yield an experimental uncertainty for λ_{hhh} of about 50% at the 68% C.L. if the SM value is realised in nature [17], the projected accuracy at a 550 GeV linear e^+e^- collider is about 20%, combining the results from the Zhh and $\nu_e\bar{\nu}_e hh$ channels [18] (an update reflecting various analysis improvements is currently prepared [19]). Because of the reduced cross section as a consequence of the destructive interference of the contributing diagrams, the projected accuracy at the HL-LHC degrades to about 84% if the value of λ_{hhh} that is realised in nature is actually twice as large as the SM prediction (this would be favoured in scenarios giving rise to a strong first-order EWPT, see above). Since on the other hand the interference contributions in the Zhh channel at a 550 GeV linear e^+e^- collider are constructive, the accuracy improves to about 9% in this case, such that the linear collider accuracy is almost an order of magnitude better than the one at the HL-LHC.³ This is illustrated in Fig. 1, where for the HL-LHC a cross section extrapolation has been used. The significant degradation of the HL-LHC accuracy on λ_{hhh} if the actual value is higher than the SM prediction has also been found in a recent projection from the ATLAS Collaboration [20]. In Fig. 1 the improvements in accuracy from additional e^+e^- data at 1 TeV are also displayed.

4 Comparison with the sensitivity of e^+e^- Higgs factories at lower energies

Since the Higgs pair production processes are beyond the kinematic reach of circular e^+e^- Higgs factories such as the CEPC and the FCC-ee, at those facilities one needs to resort to the indirect sensitivity of observables measured at lower energies to loop contributions involving λ_{hhh} . Specifically, the single Higgs observables receive one-loop contributions that depend on λ_{hhh} , while in the predictions for the electroweak precision observables at the Z pole and for the W-boson mass λ_{hhh} enters at the two-loop level. An analysis of the sensitivity to a certain parameter via loop contributions is necessarily restricted to the specific model or the specific theoretical framework that is chosen for the theoretical prediction. A well-known example is the derivation of indirect constraints on the Higgs-boson mass within the SM via a global fit of the loop contributions (the so-called “blue band” plot) [22] prior to the discovery of h . The results of this global fit were correctly interpreted at the time as indirect constraints within a specific model (in this case the SM) rather than a “measurement” of the mass of a particle that at that time was not yet discovered. It should be noted that regarding the indirect determination of λ_{hhh} via loop contributions the situation is much more difficult than for the case of the Higgs-boson mass within the SM. While the latter is a free parameter that can be freely varied within the SM while all other parameters are kept fixed, λ_{hhh} is not a free parameter of the SM, so that a variation of λ_{hhh} “within” the SM is a priori impossible.

³While it is likely that future projections for the HL-LHC will exhibit an improved prediction over the present case, due to the strong drop in the di-Higgs cross-section at the HL-LHC for values of λ_{hhh} that are larger than the SM prediction it seems rather unlikely that the accuracy reachable at the HL-LHC in this region will be competitive with the one at an e^+e^- collider with a c.m. energy of about 500 GeV.

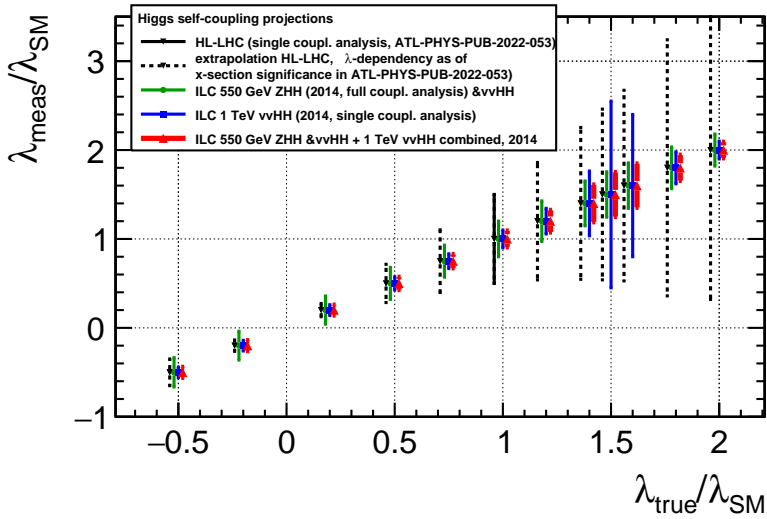


Figure 1. Projected accuracies for λ_{hhh} at the HL-LHC and a 550 GeV e^+e^- collider in dependence of the actual value of λ_{hhh} that is realised in nature [21].

Instead, one needs to employ a consistent framework for parameterising possible deviations from the SM, such as an EFT with a complete set of higher-dimensional operators.

In general, the loop contributions involving λ_{hhh} compete with much larger lowest-order contributions, with other loop contributions (e.g. a top-quark loop) that are numerically dominant and potentially also with loop contributions arising from physics beyond the SM (BSM). The indirect sensitivity to λ_{hhh} via loop effects is limited by the experimental errors of the considered observables as well as by the theoretical uncertainties that are induced by unknown higher-order contributions and by the experimental errors of the input parameters (in particular α_{em} , α_s , m_t , m_b , ...).

In an EFT approach that is consistently carried out at next-to-leading order (NLO) a large number of additional EFT operators enter compared to the ones contributing at leading order. While such additional operators contributing at NLO have recently been identified [23, 24], in the EFT fits that were carried out so far to investigate the sensitivity of the CEPC and the FCC-ee to λ_{hhh} these contributions were not yet taken into account. Furthermore, even a complete basis of dimension-6 operators at NLO in a SMEFT approach is still far from being unique in the description of possible physics scenarios. This refers on the one hand to the possible inclusion of dimension-8 (and higher-dimensional) operators and the related question of the range of validity of the EFT approach, and on the other hand to the fact that possible effects of light additional particles (below the heavy new physics scale that is used for the SMEFT expansion) are not accounted for in a SMEFT prescription.

The discussion above implies that it is a key question to what extent the indirect determinations via loop contributions at the CEPC and the FCC-ee will be able to associate a significant deviation of λ_{hhh} that may be realised in nature correctly with a non-SM value of λ_{hhh} in view of the plethora of other possible BSM contributions that enter at the same loop order and of the involved experimental and theoretical uncertainties. This has not been

demonstrated up to now. In fact, in the EFT fits carried out in this context so far no deviations of the prospective experimental measurements from the SM predictions were considered.

While in general Higgs couplings are not directly associated with physical observables, so that a model-independent measurement of a Higgs coupling is impossible as a matter of principle at any future collider, the situation regarding the determination of λ_{hhh} from the measurement of the Higgs pair production processes at the (HL-)LHC, an e^+e^- linear collider with a c.m. energy of at least 500 GeV or a $\gamma\gamma$ collider with a sufficiently high c.m. energy [25] is much more favourable than via loop effects to lower-energy observables. This is due to the fact that λ_{hhh} already enters at leading order and competes with much fewer contributions that enter at the same order. The robustness of the interpretation of the results obtained in this way within SMEFT has been demonstrated in [26]. The importance of the direct measurement of the Higgs pair production processes at lepton colliders in this context has also been pointed out, for instance, in [27–29]. A detailed comparison of the capabilities of e^+e^- colliders operating above and below the threshold for Zhh production, employing global fits for scenarios where the value of λ_{hhh} that is actually realised in nature significantly differs from the SM prediction, is on the way [30].

5 Further guaranteed physics at 500 GeV

Besides the direct measurements of the Higgs pair production cross sections $e^+e^- \rightarrow Zhh$ and $e^+e^- \rightarrow \nu_e\bar{\nu}_e hh$, further guaranteed measurements that can be carried out at an e^+e^- linear collider with a c.m. energy of about 500 GeV comprise for instance the Higgs couplings to fermions and bosons in the single Higgs production channels $e^+e^- \rightarrow Zh$ and $e^+e^- \rightarrow \nu\bar{\nu}h$. These measurements profit from the increased luminosity and from the information provided by beam polarisation and by the measurements of the relevant observables at different energy stages.

Another very important process that becomes accessible is $e^+e^- \rightarrow t\bar{t}h$, for which a c.m. energy slightly above 500 GeV is beneficial. The direct measurement of this process is advantageous for the determination of the top Yukawa coupling in comparison to indirect constraints via loop contributions in a similar way as discussed above for the trilinear Higgs-boson self-coupling. Running an e^+e^- collider at this c.m. energy also enables a rich programme of top-quark and electroweak physics.

6 Guaranteed physics beyond 500 GeV

Regarding Higgs physics, the measurements of the Higgs couplings to fermions and bosons profit in particular from the high statistics in the weak-boson fusion channel $e^+e^- \rightarrow \nu\bar{\nu}h$ at high energies. For Higgs pair production the importance of the $e^+e^- \rightarrow \nu_e\bar{\nu}_e hh$ channel as compared to the $e^+e^- \rightarrow Zhh$ channel also grows with increasing c.m. energy, but the transition to the case where the weak-boson fusion channel dominates happens at significantly higher c.m. energies than for the single Higgs production case (depending on the actual value of λ_{hhh} that is realised in nature).

A qualitatively new feature at c.m. energies of about 1 TeV and above is the sensitivity to the triple Higgs-boson production process $e^+e^- \rightarrow Zhhh$ and $e^+e^- \rightarrow \nu\bar{\nu}hhh$, which provides experimental access to the quartic Higgs-boson self-coupling λ_{hhhh} . Because of its dependence also on the trilinear Higgs-boson self-coupling λ_{hhh} (some contributions to the triple Higgs-boson production process even involve the square of λ_{hhh}), the triple Higgs-boson production process also provides complementary information on λ_{hhh} that can be combined with the results that are obtained from the Higgs pair production process.

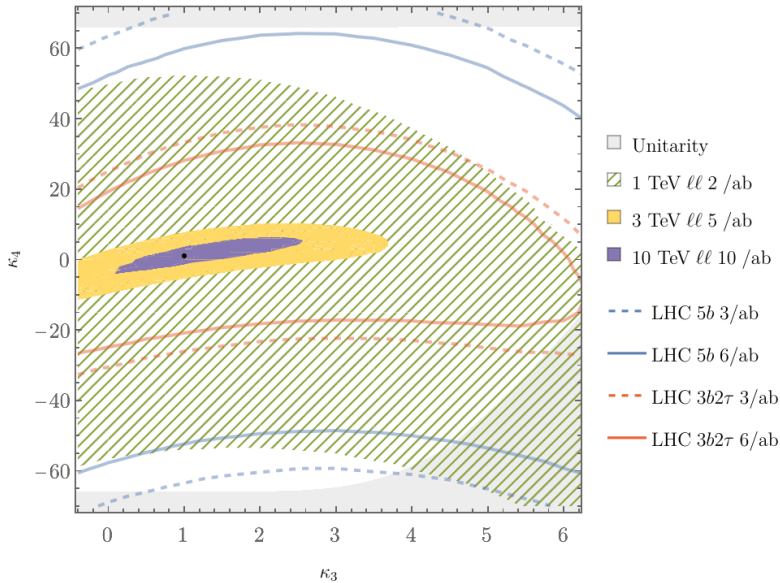


Figure 2. Prospects of future lepton colliders with a c.m. energy of 1 TeV, 3 TeV and 10 TeV for constraining the trilinear (horizontal axis) and quartic (vertical axis) Higgs-boson self-couplings, both normalised to the tree-level values in the SM, at the 95% C.L. in comparison to the projected 95% C.L. contours for the $5b$ and $3b2\tau$ analyses at the HL-LHC [12]. The shaded gray area indicates the region that is excluded by the bound from tree-level perturbative unitarity.

Fig. 2 shows the sensitivity of future lepton colliders with a c.m. energy of 1 TeV, 3 TeV and 10 TeV to set constraints on the trilinear (horizontal axis) and quartic (vertical axis) Higgs-boson self-couplings, both normalised to the tree-level values in the SM [12]. The prospective sensitivities shown here are obtained just from the triple Higgs-boson production processes, i.e. without additional information from Higgs-boson pair production and single Higgs-boson production. The prospects for the lepton colliders are compared to the ones for the HL-LHC obtained in a recent exploratory study for the $5b$ channel and the $3b2\tau$ channel [12]. These prospective bounds go significantly beyond the current theoretical constraints from tree-level perturbative unitarity, which are also displayed in Fig. 2. The displayed results indicate that the HL-LHC is competitive to a 1 TeV lepton collider in constraining λ_{hhhh} , while the higher-energetic lepton colliders (see also [14–16]) can significantly improve on the HL-LHC capabilities.

7 Sensitivity to new particles at 500 GeV and beyond

An increase in the c.m. energy of an e^+e^- collider obviously extends the kinematic reach for detecting BSM particles. A typical search process at an e^+e^- collider is the pair production of new particles. It has been demonstrated by detailed studies for many examples of BSM scenarios that the obtained exclusion and discovery reach is very robust and that the properties of the detected particles can be determined with high precision, see e.g. [1].

Concerning recent possible hints for BSM particles from the LHC searches, a hypothetical additional Higgs boson at 95 GeV [31–33] could be copiously produced [34] and studied in detail at a 250 GeV e^+e^- Higgs factory [35, 36] if it has a sufficiently large coupling to the

Z boson. However, if this is not the case the most promising production channels at an e^+e^- collider might be the production together with a $t\bar{t}$ pair or the production of a pair of the Higgs boson at 95 GeV together with a Z boson (possibly via the detected Higgs boson h as an intermediate state). The exploration of those channels would require a significantly higher c.m. energy, preferably of 500 GeV or higher. The interpretation of the very significant excess over the perturbative QCD background in the $t\bar{t}$ search channel observed very recently by the CMS Collaboration [37] in terms of a CP-odd Higgs boson at about 360 GeV could be testable (depending on the details of the production process) at an e^+e^- collider with a c.m. energy significantly above 500 GeV (since an excess at the $t\bar{t}$ threshold could also be caused by BSM particles with masses far above the $t\bar{t}$ threshold [38], c.m. energies even above 1 TeV might be required for testing such a scenario). Information from an e^+e^- collider with sufficiently high c.m. energy could be instrumental for distinguishing the interpretation of the CMS signal in terms of a $t\bar{t}$ bound state from possible BSM scenarios.

8 Conclusions

An e^+e^- collider running at a c.m. energy of 500 GeV or above has a very rich physics programme consisting of guaranteed measurements and a high sensitivity for detecting possible new particles. Among the guaranteed measurements the direct and model-independent measurement of the Higgs pair production process $e^+e^- \rightarrow Zh h$ is a qualitative game-changer distinguishing the physics capabilities of an e^+e^- collider at 500 GeV and above from the ones of Higgs factories at lower energies such as the CEPC, the FCC-ee and a lower-energy version of an e^+e^- linear collider.

The information on the trilinear Higgs-boson self-coupling that can be obtained from the Higgs pair production process is crucial for gaining experimental access to the Higgs potential, the “holy grail” of particle physics which is the key to many of the most pressing questions about the fabric of nature. The capabilities of an e^+e^- collider with a c.m. energy of about 550 GeV for determining the trilinear Higgs-boson self-coupling go significantly beyond the prospective HL-LHC sensitivities. This holds for the case where the value of the trilinear Higgs-boson self-coupling that is realised in nature agrees with the SM prediction, and becomes even more pronounced for the case, typically favoured in scenarios giving rise to a strong first-order EWPT that could explain the observed asymmetry between matter and anti-matter in the universe, where the actual value of the trilinear Higgs-boson self-coupling is somewhat higher than the SM value. The determination of the trilinear Higgs-boson self-coupling from the Higgs pair production process is also superior to the indirect constraints on λ_{hhh} that can be obtained at lower-energetic Higgs factories via loop effects involving λ_{hhh} that compete with a large variety of other contributions entering at the same order. As furthermore discussed above, the highest-energetic lepton colliders provide sensitivity for constraining the quartic Higgs self-coupling.

The unique capabilities in measuring the Higgs pair production processes in combination with the significantly extended reach for BSM searches are a strong motivation for designing a future e^+e^- Higgs factory such that an upgrade to at least 500 GeV is possible.

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