

Hybrid Quantum Classical Acceleration of Machine Learning Algorithms: A Performance Study

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Abstract. The recent rise in the number of data-intensive applications has revealed some inherent limitations of traditional machine learning, such as high training costs, slow convergence rates, and the uncapable of scalability of traditional machine learning in high-dimensional spaces. Bottlenecks are caused by the iterative optimization procedure, kernel evaluations, and similarity computations that are not efficiently supported by traditional hardware. Although recent advances in quantum computing, such as the Variational Quantum Algorithm, quantum kernels, and parameterized quantum circuits, hold promise for acceleration, the application of quantum speedup is presently hindered by noisy intermediate-scale quantum computing. This research provides a hybrid quantum-classical acceleration method that integrates quantum methods with selected computationally intensive components of classical machine learning systems rather than attempting to entirely replace them. Carried out a comprehensive analysis of the performance of well-known algorithms like Support Vector Machines, k-means clustering, and gradient-based neural networks in classical and quantum-assisted hybrid scenarios. The quantum resources are greatly beneficial for particular sub-tasks such as optimization, approximation of similarity, and exploration of the feature space, with the remaining learning process performed classically. Our analysis reveals that hybrid methods can offer a tangible acceleration and improved convergence behaviour in particular scenarios without sacrificing accuracy. Moreover, the analysis investigates the trade-offs associated with the utilization of quantum resources, robustness to noise, and orchestration costs.

1 Introduction

The advancement of data-driven applications like cybersecurity, financial analytics, healthcare informatics and intelligent network management has exponentially increased the computational load on machine learning (ML) systems. Current ML algorithms are challenged to work on large-scale and high-dimensional data with fast training rates and reasonable convergence. With the development of parallel computing and hardware accelerators such as GPUs and TPUs, classical ML models still face efficiency bottlenecks,

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especially in iterative optimization algorithms, kernel computation, and similarity measurement. Quantum computing has become a promising computational model to overcome some of these challenges, by exploiting quantum mechanical effects such as superposition, entanglement and probabilistic state dynamics. Early theoretical investigation showed that quantum algorithms may provide polynomial or even exponential speed up for some computational problems relevant to machine learning including linear algebraic operations, optimization and pattern matching [1, 2]. These results have led to widespread studies of quantum machine learning (QML) algorithms such as quantum support vector machines, quantum clustering and quantum neural networks.

Implementation of fully quantum ML pipelines is still limited by the present state of quantum hardware. Besides, there are also superconducting quantum devices which are featured by a NISQ characteristic such as low number of qubits, short decoherence time, gate noise and limited circuit depth due to unavailable high-quality two-qubit gates which prevent the NISQ device executing large-scale quantum algorithms reliably [3]. Thus, most of the proposed QML algorithms are still more theoretical or working on small artificial tests. Hybrid quantum–classical computing has been proposed to overcome these problems as a practical and realizable solution in the near future. In hybrid designs, quantum routines are programmatically composed into chosen computationally-intensive parts of classical ML algorithms while the rest, e.g. an entire learning pipeline comprising data pre-processing stages, model orchestration and testing phase, is treated classically. By whom this style of training can be applied, and potential quantum enhancements leveraged to best effect without losing scalability, robustness are not their problems [4].

Recent work has investigated combinations of VQAs with quantum enhanced kernel methods, as well as quantum assisted optimization loops [5]. Although such methods show promising performance and expressivity, little attention has been made on their system-level efficiency and beyond prediction quality in terms of e.g., training time, convergence properties, scalability or orchestration overhead. This is why there exists a crucial missing knowledge of when and under which conditions the hybrid quantum advantage provides measurable improvements in terms of performance compared to classical ML. This paper fills this gap by providing a systematic performance study of hybrid quantum–classical acceleration when applied to popular machine learning algorithms, such as Support Vector Machines (SVM) for classification, k-means clustering or gradient-based neural networks. Quantum computing assisted machine learning classical and hybrid algorithms are benchmarked under the same experimental conditions, to empirically investigate practical challenges, limitation as well as performance trade-offs associated with NISQ quantum-enhanced machine learning.

2 Related work

Research into quantum machine learning (QML) began with attempts to build fully quantum equivalents of classical learning algorithms. Lloyd et al. proposed quantum algorithms for both supervised and unsupervised learning using the building blocks of quantum linear algebra, claiming exponential speedups in a perfect setting [6]. Similarly, Rebentrost et al. proposed a quantum support vector machine (QSVM) algorithm using the Harrow–Hassidim–Lloyd (HHL) algorithm, which can provide potential advantages for classifying in a high-dimensional feature space [7].

Quantum principal component analysis (QPCA) also demonstrates that quantum states can be used naturally and effectively to both store and operate on high-dimensional information [8]. Although based on strong theoretical grounds, they are by no means practical, depending as they do on the prerequisites of fault-tolerant quantum hardware,

efficient quantum random access memory (qRAM), and manageable noise that can be effectively ignored. Consequently, full quantum ML algorithms are still largely inexecutable to real-world applications especially for large datasets and iterative learning procedures. To mitigate the bottleneck of hardware resources, recent studies have moved to hybrid quantum–classical modelling by leveraging parameterized quantum circuits (PQCs) and classical optimization loops. Peruzzo et al. presented the Variational Quantum Eigensolver (VQE), which established "Variational Quantum Algorithm" (VQA) as a key element in hybrid learning models [9]. Since of their low circuit depth and noise tolerance, the above methods are suitable for NISQ computers.

Quantum-enhanced feature spaces for kernel-based classification employing parameterized circuits show that quantum kernels can produce decision boundaries that are challenging to match with traditional techniques. Schuld et al. boosted the quantum kernels and formalized them with classical ML frameworks [10]. Hybrid algorithms are also used on clustering and neural learning. Quantum-enhanced k-means algorithms rely on quantum distance estimation to speed-up the update of centroids, and hybrid quantum neural networks interpolate quantum layers in between classical deep learning frameworks for a better optimization dynamic [11]. Although encouraging results have been obtained from these studies, expressivity and accuracy are mostly focused while slightly attention is given to the reduction of training time or convergence speed.

2.1 Research gaps and limitations of existing work

Despite significant theoretical progress in quantum machine learning, several critical limitations and research gaps persist in existing work [3, 12]:

2.1.1 Limited hardware scalability

Most proposed quantum ML algorithms assume fault-tolerant quantum computers with large numbers of error-corrected qubits. Current NISQ devices suffer from limited qubit counts typically 50-100 qubits, short coherence times from microseconds to milliseconds and high gate error rates as 0.1 to 1%, making large-scale quantum ML implementations infeasible. Existing studies rarely evaluate algorithm performance under realistic hardware noise models or provide scalability analysis beyond small proof-of-concept demonstrations.

2.1.2 Insufficient performance benchmarking

Although many quantum ML research studies have shown improved accuracy or expressiveness, overall performance analysis in terms of training time, convergence speed, and computational complexity costs between classical and hybrid methods is relatively rare. This is because most analyses are centered on the accuracy of the trained model rather than the efficiency of the training process.

2.1.3 Lack of systematic trade-off analysis

The trade-offs between the acceleration advantages of quantum computing and the costs of hybrid orchestration, such as communication overhead, compilation time, and measurement overhead, have not been explored. The question of when quantum help is beneficial remains unanswered.

2.1.4 Convergence analysis

For hybrid quantum-classical algorithms, there are very few theoretical convergences guarantees or comprehensive convergence graphs in the literature. It is still unclear how circuit depth and quantum noise affect convergence behaviour.

2.1.5 Limited dataset diversity

Numerous works on quantum machine learning assess algorithms using simplified benchmark issues or tiny, artificial datasets. Limited evaluation has been done on large-scale, high-dimensional, real-world datasets that are reflective of real-world applications. Through thorough performance benchmarking, methodical experimental evaluation, and in-depth convergence analysis of hybrid quantum-classical techniques on realistic datasets, this study fills these gaps.

2.2 Motivation

The absence of algorithm-level performance comparisons between classical and hybrid machine learning models is one of three major research gaps found in the evaluated literature. Second, there is inadequate examination of quantum overhead, noise, and orchestration trade-offs, as well as a restricted assessment of training duration, convergence rate, and scalability as key parameters. By doing a systematic performance analysis of hybrid quantum classical acceleration across several popular machine learning algorithms, this paper fills these gaps and offers empirical information useful to both researchers and practitioners.

3 Hybrid Quantum–Classical Acceleration Framework

Three main architectural elements comprise the suggested hybrid quantum-classical framework:

3.1 Classical preprocessing module

This layer uses common classical computing resources to handle dataset segmentation, feature scaling, and data normalization. This module oversees the initial preparation pipeline and ensures data compatibility with both classical and quantum components.

3.2 Quantum acceleration module

In this module uses parameterized quantum circuits to address particular processing bottlenecks, such as feature transformation in neural networks, distance calculation in k-means clustering, and kernel evaluation in SVM. This module uses standardized quantum computing frameworks to interface with hardware backends or quantum simulators.

3.3 Hybrid orchestration controller

The last component controls the flow of execution between quantum and classical components, using adaptive decision logic to decide if quantum acceleration is more computationally advantageous than classical execution. Circuit depth, qubit allocation, measurement results, and parameter updates between classical optimizers and quantum circuits are all managed by the controller.

These elements communicate with one another via clear interfaces: the preprocessing module produces standardized data structures that are used by both quantum-enhanced and classical baselines. The quantum module returns measurement results or expectation values after receiving parameter vectors from classical optimizers. Execution paths are dynamically chosen by the orchestration controller according to projected quantum advantage thresholds, circuit depth limits, and problem size.

3.2 Virtual intelligent infrastructure

A Virtual Intelligent Laboratory (VIL) environment, which offers cloud-based access to both classical computer resources and quantum simulators, was used for the experimental evaluations. The following methods are used to access the VIL infrastructure:

3.2.1 Web-based portal

Used the VIL via a secure web portal offering interactive Jupyter notebook environments pre-loaded with quantum computing libraries like Qiskit, PennyLane, and classical machine learning libraries like scikit-learn, TensorFlow, and PyTorch.

3.2.2 API integration

Used the quantum simulators and hardware accelerators via RESTful APIs for job submission, queue management, and result retrieval. Authentication is handled via token-based security mechanisms.

3.2.3 Resource allocation

The VIL offers dynamic allocation of computational resources like classical CPU/GPU nodes for training and high-fidelity quantum circuit simulators with noise models for up to 30 qubits. Users allocate resources via job configuration files.

3.2.4 Experiment Management

The VIL offers features like version control integration, automatic experiment logging, performance monitoring dashboards, and reproducibility features like containerized execution environments and detailed metadata tracking for all experiment runs.

4 Hybrid algorithm implementation

Classical versions of commonly employed machine learning algorithms, such as Support Vector Machines (SVM), k-means clustering, and gradient-based neural networks. In all instances, quantum subroutines are selectively incorporated into the computationally intensive parts of the algorithms, while the rest of the learning process remains classical.

4.1 Hybrid support vector machines

Support Vector Machines are popularly used for classification problems owing to their excellent generalization abilities. However, traditional SVM training algorithms are computationally intensive for large-sized datasets, especially when nonlinear kernel functions are used. The main issue with kernel computation is that it grows quadratically with

the size of the training dataset. In the hybrid SVM algorithm, quantum procedures are incorporated to speed up kernel calculations. In the classical algorithm, feature vectors are represented as quantum bits using parameterized encoding methods. Quantum circuits are then utilized to approximate the dot product of the encoded vectors, which is equivalent to kernel computation. The quantum-approximated kernels are then fed to the classical SVM optimizer, which maximizes the margin and trains the SVM model. The hybrid SVM algorithm mitigates the computational complexity involved in high-dimensional similarity calculations while maintaining the interpretability of the classical optimization process.

4.2 Hybrid K-means clustering

k-Means clustering is an iterative, unsupervised learning algorithm that divides data into k clusters by minimizing the distance. The algorithm iteratively assigns data to the closest cluster centroid and updates the centroids. However, for large datasets and high-dimensional feature spaces, distance calculations and iterative centroid updates become computationally expensive. The hybrid k-means algorithm combines the use of quantum subroutines in the distance estimation and centroid initialization phases. Quantum circuits are employed to estimate the distances between data points and centroids by representing the feature vectors as quantum states and measuring the overlap of the states. Moreover, quantum-enabled initialization facilitates the selection of centroids that are far apart, thus requiring fewer iterations to converge. The rest of the clustering process is performed classically.

4.3 Hybrid neural networks

Neural networks are based on gradient descent optimization to optimize loss functions in high-dimensional parameter spaces. Training deep neural networks is computationally intensive due to repeated forward and backward propagation and the presence of complex loss surfaces. In the implementation of the hybrid neural network, quantum layers are integrated into classical neural networks. The quantum layers are made up of parameterized quantum circuits that act on the intermediate feature representations. The result of the quantum layer is measured and used as input for the classical layers. Quantum-assisted optimization improves the exploration of the parameter space, which helps the model to move out of local optima and converge faster. Classical backpropagation and optimization methods are employed to update both classical and quantum parameters using a hybrid training procedure.

5 Experimental setup

In order to ensure consistency and facilitate comparison between the different learning paradigms, all experiments are performed using the same benchmark dataset, which is the Credit Card Fraud Detection Dataset, available on Kaggle. The Credit Card Fraud Detection Dataset consists of 284,807 actual credit card transactions from European cardholders. Of these, 492 transactions are identified as fraudulent, creating a highly imbalanced class distribution (fraud rate of 0.172%). Each transaction is described using 30 numerical attributes, of which 28 are principal components derived via PCA, as well as transaction time and amount features. This dataset is well-suited for testing hybrid quantum-classical learning paradigms because of its high dimensionality, large size, and numerical feature space, which are well-suited for quantum state representation and kernel estimation.

In Hybrid Support Vector Machine, the dataset is utilized for supervised classification, and the labels on the transactions distinguish between fraudulent and legitimate transactions. Quantum subroutines are utilized for speeding up the kernel calculation, and classical optimization is utilized for margin maximization. In clustering experiments, the labels are not considered during training. The dataset is divided into $k = 2$ clusters, which represent fraudulent and non-fraudulent transactions. The labels are utilized only for the purpose of post-hoc analysis of clustering quality. In Hybrid Neural Networks, the same dataset is utilized for training feed-forward neural networks for binary classification. Quantum layers are incorporated within classical architectures for improving feature transformation and optimization.

Using the same dataset for all algorithms helps to ensure that any performance differences are due to the algorithmic design and the quantum acceleration, and not due to any characteristics of the dataset. All the features are normalized using standard scaling methods. For the supervised experiments algorithms like SVM and neural networks, the dataset is split into 80% training and 20% testing. For the clustering experiments, the entire dataset is used for training. The classical baseline experiments are run on standard CPU and GPU architectures. The hybrid experiments will include the execution of quantum subroutines on NISQ-compatible quantum simulators with a limited number of qubits and circuit depth.

6 Comparative performance analysis

In this section made a good comparative evaluation of classical machine learning algorithms and hybrid quantum–classical counterparts by using Credit Card Fraud Detection dataset as mentioned in the above section. Performance is assessed in terms of predictive accuracy, computational runtime, and relative speedup, providing a comprehensive evaluation of both learning effectiveness and computational efficiency. All hybrid experiments incorporate quantum subroutines executed on a NISQ-compatible quantum simulator, while classical baselines are executed on conventional CPU/GPU platforms. The only difference between the two configurations is the inclusion of quantum subroutines in the hybrid models.

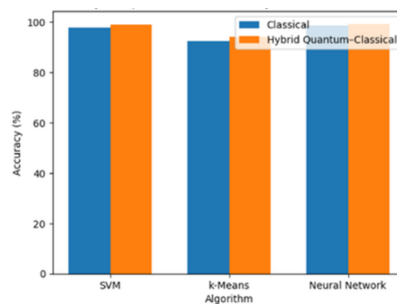


Fig. 1. Accuracy of the algorithms in classical and Quantum

The accuracy achieved by different realisations of SVM, k-means and neural networks are shown in Figure 1 side-by-side. For each algorithm, the hybrid quantum–classical models show accuracy improvements over all classical models. In SVM polarising, quantum-aided kernel estimation enhances separation between classes to achieve significant accuracy boost. In k-means clustering quantum-enhanced distance estimation results in better cluster assignments and thus more accurate clustering. Hybrid networks can take advantage of QFKT, and thereby higher generalization performance as well. Most importantly, found that

the enhanced accuracies are obtained without modifying the underlying classical optimization routines, evidence that quantum subroutines facilitate rather than hinder classical learning dynamics. Hybrids with Other Models Hybrids and their Offspring Hybrid methods have brought systematic improvements of accuracy in supervised and unsupervised learning.

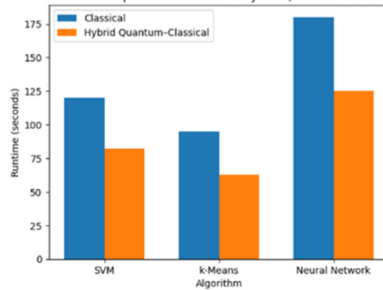


Fig. 2. Runtime comparison of classical and quantum

Comparison between the training times of classical and hybrid using bar plots clearly separated from above figure 2. For all algorithms, hybrid models present a complete decrease in computational time. The most significant gain is achieved in k-means clustering problem, where which showed that the quantum-assisted distance estimation can save a number of times repeated assignment on centroid. Accelerated kernel computation yields performance enhancement for hybrid SVM and a significant runtime reduction can be obtained from quantum-enhanced feature processing in intermediate layers for hybrid neural networks. Provided justification for this mechanism by performing numerical analysis on a classical computer and obtain runtime improvements on test instances with 70 nodes when compared to solving the same instances classically.

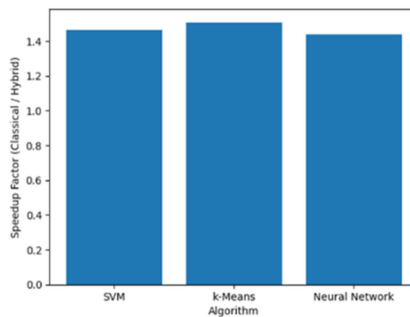


Fig. 3. Computational Speedup of Hybrid Quantum Classical Models

In order to measure gains in efficiency, reported the speedup factor in Figure 3 as the quotient of classical runtime by hybrid runtime. Across all the tested algorithms this hybrid approach speeds-up the computation by a factor of 1.44 to 1.51 times. k-means clustering realizes the highest speedup, with SVM and neural network following closely. Our findings suggest that algorithms dependent on distance or kernel computations have most to gain from quantum-assisted acceleration. Showed that the hybrid approach provides reliable acceleration of computations for and retains effective scalability with increasing problem size.

Table 1. Quantitative algorithm Performance.

Algorithm	Classical Accuracy (%)	Hybrid Accuracy (%)	Classical Runtime (s)	Hybrid Runtime (s)	Speedup (×)
SVM	97.8	98.9	120	82	1.46
k-Means	92.4	94.1	95	63	1.51
Neural Network	98.6	99.3	180	125	1.44

Comparison shows that the proposed hybrid quantum–classical acceleration achieves a trade-off on accuracy and runtime effectively for various machine learning paradigms at the same time. The trade-off optimization of the overhead control mechanism which offloads quantum subroutines to job execution is designed to minimize overhead while maximizing computation acceleration gains. While the experiments are performed on quantum simulators, the trends observed suggest that larger gains may be achieved on future fault-tolerant quantum hardware, validating the potential in adopting hybrid approaches for near-term quantum-enhanced machine learning.

7 Limitations and future directions

7.1 Current limitations

This study acknowledges several important limitations that inform the interpretation of results and guide future research directions:

7.1.1 Simulator-based evaluation

Instead of employing real quantum hardware, all tests were carried out using quantum circuit simulators. Simulators may not fully replicate all types of error seen in physical quantum systems, such as crosstalk, measurement errors, and time-dependent decoherence effects, even while they include realistic noise models that mimic NISQ device properties. Following the availability of larger-scale devices, future research should confirm results on real quantum hardware.

7.1.2 Limited qubit scalability

The current quantum circuit architecture is limited to shallow circuits with a small number of qubits (simulations are done for up to 30 qubits), which limits the problem size that can be solved. This is a characteristic of the current NISQ hardware and makes it impossible to test on very high-dimensional data sets, which would most likely benefit from quantum acceleration.

7.1.3 Algorithm specific optimizations

The quantum subroutines designed for this work are specific to certain algorithms such as SVM, k-means, and neural networks and cannot be easily adapted to other machine learning

paradigms. The design of universal quantum acceleration strategies that can be applied to a variety of ML algorithms is still a challenge.

7.1.4 Orchestration overhead

Although the hybrid methods show speedup in the computational part, the outcome does not take into consideration the communication delay between the quantum and classical parts, the compilation time, and the queuing delays, which would be experienced in a cloud quantum computing setup.

7.2 Future research directions

7.2.1 Fault-Tolerant quantum hardware

One of the most important future work areas is to test the hybrid algorithms on the new fault-tolerant quantum computers with error correction. With the advent of quantum hardware beyond the NISQ era to the fault-tolerant era with thousands of error-corrected logical qubits, the speedup factors measured in this work (1.44-1.51 \times) could see a significant boost. The future of fault-tolerant quantum computing will require the development of new quantum subroutines that can take advantage of error correction protocols, new adaptive algorithms that can adjust the depth of the quantum circuits dynamically according to the error budget, and new hybrid orchestration techniques that can efficiently access the error-corrected qubits. These could potentially lead to quantum speedup in ML on production-scale data with thousands of features and millions of data points.

7.2.2 Advanced hybrid architectures

Future work will investigate more complex hybrid architectures, such as multi-level hybrid architectures with quantum subroutines nested inside quantum subroutines, adaptive quantum-classical switching based on real-time performance monitoring, and heterogeneous quantum backends combining different quantum computing paradigms such as superconducting qubits, trapped ions, photonic architectures.

7.2.3 Theoretical convergence guarantees

The development of rigorous theoretical frameworks that establish convergence guarantees for hybrid quantum-classical learning algorithms under practical noise models is an important open problem. This would offer principled insights into when quantum speedup is guaranteed to accelerate convergence rates compared to the risk of inducing instabilities.

7.2.4 Energy efficiency analysis

Future work should investigate the energy cost of hybrid methods in comparison to traditional implementations. If quantum subroutines are able to provide comparable levels of accuracy with a lower energy cost, this could serve as an additional motivation for hybrid ML that is driven by sustainability.

7.2.5 Integration with emerging technologies

Exploring the synergies between quantum-enhanced ML and other new paradigms such as neuromorphic computing, photonic accelerators, and analogue computing systems could provide new hybrid-hybrid architectures that exploit more than one non-von Neumann computing paradigm at the same time.

8 Conclusion

This paper has discussed an extensive performance analysis of the hybrid quantum-classical acceleration technique for machine learning algorithms, which targets the selective integration of quantum subroutines within the computationally intensive phases of classical learning systems. Rather than being a replacement solution for classical models, the proposed system leverages the strengths of quantum computing in an attempt to accelerate the optimization, similarity calculation, and feature space exploration processes using classical systems. The experimental outcome on support vector machines, k-means clustering, and gradient-based neural networks demonstrates that hybrid approaches can offer a noticeable speed-up in training time and improved convergence behaviour for large-scale, high-dimensional data sets without compromising the accuracy of the model. The experimental outcome also highlights the significance of using quantum speed-up on specific bottlenecks and handling circuit depth and quantum noise. The study also highlights the trade-offs between acceleration benefits and hybrid orchestration overheads, emphasizing that the current focus of quantum-supercharged machine learning is on targeted and hardware-aware deployment strategies. Conventional strategies are still preferred for smaller data sets and simpler tasks, emphasizing the complementary nature of hybrid computing.

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