

# Thermodynamic Model to Evaluate the Efficiency and Economic Benefit of a Two Spool Engine

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**Abstract** –A case study into the performance of two-spool turboprop engines, used the Pratt & Whitney PW120A to evaluate fuel efficiency, range, and economic savings. The results indicate that such two-spool models improve fuel efficiency by about 5% over a single-spool. The extended range by 65 km per flight saves ~\$26,800 annually per aircraft. These figures confirm the relative efficacy of two-spool engine architectures.

## 1. INTRODUCTION

The development of advanced engine architectures has been motivated by needs for fuel and pollution efficiency. Two-spool aero-engines improve, over single-spool templates by optimizing power distribution between high-pressure (HP) and low-pressure (LP) spools. In the following a comparative cycle analysis of two-spool and single-spool models is presented, using thermodynamics, evaluates real-world engine performance.

This involves:

1. A validated spool-level thermodynamic model aligned with Dash 8-100 data (<7% ESFC deviation).
2. Integrated performance–economics analysis linking efficiency to range and annual cost savings.
3. Multi-factor sensitivity analysis (altitude, bleed air, compressor efficiency).
4. Adaptable case study framework for hybrid-electric or geared turbofan comparisons.

## 2. Methodology

The study applies classic thermodynamic cycle equations, modeling the PW120A engine as a two-spool system with a free power turbine. The LP and HP spools are analyzed separately, incorporating mechanical efficiency, accessory power draw, and external bleed air losses.

We modeled the PW120A engine as a two-spool thermo system (having a free power turbine). Separate power balances were applied to

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the low-pressure (LP) spool, high-pressure (HP) spool, and the power turbine. The governing equations are: LP Spool Power Equation: (1)

HP Spool Power Equation:(2),Power Turbine Output: (3)  

$$P_{LP} = \eta_{m,LP} [\dot{m}_a C_{pa} (T_{02} - T_{01}) - \dot{m}_{bid} C_{pa} (T_{bid} - T_{01}) - P_{acc}] \quad (1)$$

$$P_{HP} = \eta_{m,HP} [\dot{m}_a C_{pg} (T_{04} - T_{03}) - \dot{m}_a C_{pa} (T_{03} - T_{02})] \quad (2)$$

$$P_{PT} = \eta_{m,PT} [\dot{m}_a C_{pg} (T_{06} - T_{05})] \quad (3)$$

Where:  $P_{LP}$ ,  $P_{HP}$ ,  $P_{PT}$  are net powers of the LP spool, HP spool, and power turbine.  $\dot{m}_a$  is mass flow rate of air,  $\dot{m}_{bid}$  is bleed air mass flow,  $C_{pa}$  and  $C_{pg}$  are specific heats of air and gases,  $T_{01}$ – $T_{07}$  are total temperatures,  $P_{acc}$  is accessory power, and  $\eta_m$  are spool efficiencies. Validation used published performance data (PW120A-powered aircraft) [1].

### 2.1 Boundary Conditions and Input Parameter Ranges

The operating key parameters are defined as follows: inlet stagnation temperature ( $T_{01}$ : 288–320 K), compressor pressure ratios (LP: 2.5–3.0, HP: 3.0–4.0), turbine inlet temperature ( $T_{04}$ : 1100–1200 K). These are typical variations due to altitude, flight speed, and environment factors for regional turboprops, and ensure reproducibility,

### 2.2 Validation and Sensitivity Analysis

Validation Metric: A validation metric compares simulated ESFC with published Dash 8-100 data: (ESFC equivalent specific fuel consumption)

$$\Delta ESFC = (|ESFC_{sim} - ESFC_{pub}| / ESFC_{pub}) \times 100$$

With  $ESFC_{sim} = 0.303$  kg/kW-h and  $ESFC_{pub} = 0.285$  kg/kW-h, the deviation is 6.3%, aligning with the model's <7% ESFC deviation claim.

### 2.3 Sensitivity Coefficient:

The impact of parameter changes is seen in:

$$S_x = (\partial ESFC / ESFC) / (\partial x / x)$$

For instance, a 2% drop in compressor efficiency increases ESFC by 6%, yielding  $S_{\eta_c} \approx 3$ , meaning high sensitivity.

### 2.4 Real World Examples

The following validation examples compare simulated outputs with published data. Table 2 gives a summary of the results:

1. **Fuel Usage:** The predicted fuel usage was 420.4 kg per flight (for the two spool PW120A configuration), contrasting to 441.4 kg (for a single-spool version) (Figure 1). When checked against Dash 8-100 flight data [1] showing an average fuel burn of 425 kg (under similar conditions at cruise at 25,000 ft, Mach 0.5). The overestimation was only 1.1%, maybe due to conservative efficiency assumptions ( $\eta_{m,LP} = 0.97$ ).

**2. Range :** We found that the two spool engine range could be increased from 1305 km to 1370 km (Figure 2), which validates Hosking et al. [1]

**3. PW127-EESFC Validation :** The simulation compared with Yuksel [9] for the PW127-E turboprop, ( ESFC of 0.298 kg/kW-h at 25,000 ft and Mach 0.5 -- predicted ESFC of 0.303 kg/kW-h) . A 1.7% deviation (0.303 vs. 0.298) resulted, possibly caused by the higher mass flow of the PW127-E (mass flow rate 13.2 kg/s vs. 12.5 kg/s).

**4. Economic Savings Validation:** Our calculations showed that the efficiency boost could save about \$26800 per aircraft per year (Figure 3). The IATA 2019 road map 2019 [7], predicts \$25000 to \$28000 savings in efficiency gains under similar conditions. The model compares closely with the actual real industry data, staying within 2% error margins.

**Table 1** Typical parametric values

Parameter	Value	Source/Assumption
Inlet stagnation temperature (T01)	288 K	ISA sea-level
Inlet stagnation pressure (P01)	101.3 kPa	ISA sea-level
Compressor pressure ratio (LP)	2.8	PW100 data [1]
Compressor pressure ratio (HP)	3.6	PW100 data [1]
Turbine inlet- temperature (T04)	1150 K	Typical turboprop
Mass flow rate ( $\dot{m}_a$ )	12.5 kg/s	Estimated ( Dash 8-100 data)
Polytropic compressor efficiency	0.85	Literature [2]
Turbine efficiency	0.88	Literature [2]
Mechanical efficiencies	0.97 (LP), 0.98 (HP), 0.98 (PT)	Typical
Bleed air fraction	3%	Cabin pressurization [3]
Propeller efficiency	0.82	IATA roadmap [7]

Separate values based on general PW100 family data, in Table 1 (LP: 2.8, HP: 3.6; product  $\approx 10.08$ , close to 12.14 with inter-stage losses) were **approximated as follows-**

- LP:  $\sim 2.5-3.0$  (from PW100 data in Saravanamuttoo et al., Gas Turbine Theory[2]).

- HP:  $\sim 3.0-4.0$  (centrifugal stage typical for PW120A, adjusted to match overall).

**Table 2:** Validation Results

Parameter	Simulated Value	Published Value	Source	Deviation (%)	Notes
Fuel Burn (kg/flight)	420.4	~425	Est. from ESFC [1] & mission data	1.1	Cruise 300km, 1.2h mission
Range (km)	1370	1350	Dash 8-100 [1]	1.5	Full fuel load
ESFC (kg/kW-h)	0.303	0.298	PW127-E [9]	1.7	Mass flow variance
Annual Savings (\$)	26,800	26,900 (midpoint)	IATA [7]	0.7	Within range

**-Fuel Burn:** "~425 kg" now as estimate; aligns with ~590 kg/h cruise rate × 0.72h effective burn time (from Airlines.net and ESFC calc).

**-Overall Deviations:** Still <2%, supporting model validity.

Fuel Burn Validation: Model predicts 420.4 kg/flight (two-spool). Estimated published value ~425 kg for Dash 8-100 (from ESFC 0.285 kg/kW-h in [1] × 2,380 kW × 1.2h mission; cross-checked with cruise rates ~590 kg/h ). 1.1% deviation. ... These use Ref [1]'s ESFC as anchor, with mission assumptions for flight-specific metrics.

### 3. Assumptions And Limitations

It is important to note here that our model has certain limitations. The main point is that the engine was looked at the "spool level" rather than a detailed "stage level", where more thermodynamic nuances could be captured. Furthermore, only steady state flight was modeled, rather than the non steady state transient components ( takeoff and landing). Fuel quality was taken constant whereas in real life, the quality degrades with age.

In practice, transients increase fuel consumption. Based on Turboprop data transients consume upto 15-20% more fuel, these phases covering upto 20% of flight time. The adjusted saving including transients would then be:  $\approx 26,800 \times (1 - 0.2 \times 0.15) \approx 26,000$

### 4. Results & Discussion

#### **4.1 Improvement in Range and Fuel-burn**

Figure 1 shows a significant reduction from 441.4 kg to 420.4 kg with a two spool. This ~5% improvement is expected, due to optimized energy extraction from multiple spools and better matching of stages, [2].

As a result, the usable range per aircraft increases by 65 km on a full tank. Although this might seem small, over a whole fleet this figure adds up. Recent turboprop optimization studies [6] support this..

#### **4.2 Economic Impact**

The annual cost savings potential for a two-spool configuration is illustrated in Fig.3 . The per-flight savings of \$17.87 amount to ~\$26,800 annually per aircraft, ( assuming 5 daily flights daily with Jet-A fuel priced at \$0.85/kg, over 300 operational days). Even after accounting for transient effects, savings remain above \$26,000 annually.

These results compare favourably with recent IATA study reports. Even single-digit per cent efficiency gains result in high ROI due to fuel costs [7].

#### **4.3 Real-World Data Comparisons**

An ESFC of 0.303 kg/kW-h is predicted, merely 6.3% off from the DASH 8-100's published figure of 0.285 kg/kW-h. This small gap leads confidence to our initial assumptions. Figure 4 shows this is a very narrow error margin. This could be fine tuned further by accounting for mechanical drag and other losses. [5.6]

#### **4.4 Sensitivity Analysis**

What matters Most?. We also ran several tests to see how different conditions affect the engine's performance ( Fig 5).

Altitude: Air density and drag reduce at higher flying altitudes, improving aircraft efficiency.

Bleed Air: It is surprisingly "expensive" to extract bleed air for the cabin . A small increase can worsen ESFC( fuel consumption) by 4.8% - highlighting the importance of efficient pressurization.

Maintenance: A mere 2% drop in compressor efficiency can lead to a nearly 6% fuel spike. It is thus important to keep the compressor blades clean and well maintained.

## 5 . Discussion Of The Literature

### 5.1 Literature Context and Theoretical Framework

The advantages of split-spool over single spool designs have been known for some time, however the specific bench-marking has not been done. To build a solid foundation the study, Hosking et al. [1]. (covering the PW100 series), provided thermodynamic and efficiency targets for the Dash 8-100.

The analytical basis provided by Saravanamuttoo et al. [2] provide the core of our model. Their breakdown of the LP and HP spools contribution to thermal efficiency gave a framework for the cycle-based model. Schofield and Green [3] mainly look at catastrophic failures like "blade-offs" in turbofan. The approach to decoupling inter spool effects helped to refine the steady-state model assumptions.

The Key factors in engine architecture are Reliability and stability. De Felice and Sorrentino [4] look at gyroscopic stability nonlinear analysis, and this vital for any meaningful reliability projections Spataro et al. [5] provide an explanation of the minor discrepancies—such as our 6.3% ESFC variance—often found between idealized models and actual Dash 8-100 flight data.

Epstein [6] broadly highlights how changes in architectures have driven the evolution of propulsion efficiency. The IATA Technology Roadmap [7], identified multi-spool setups as a primary tool in achieving fuel economy for regional aviation. This industry-wide consensus confirms our findings of a ~5% efficiency gain over the older, single-spool variants.

According to Martin and Insausti [8], ESFC is a reliable metric for an engine's environmental footprint. Our own sensitivity analysis is similar. Yuksel et al. [9] demonstrated mission-based scenarios. Their thorough evaluation of the PW127-E— from fuel mixes to various altitudes (0–9 km) and Mach numbers (0.3–0.6)—reinforces parametric modeling's effectiveness in predicting real-world fuel costs and range. Kim et al. [10] recommend optimization tools like genetic algorithms.

## 6. Conclusion and Practical Insights

Validation of a thermodynamic model confirmed a steady 5% fuel economy gain. Analyses clearly favour two-spool architectures for

performance and operating costs. For every aircraft in the fleet it scales up to an extra 80 km of range and about \$33,500 in yearly savings.

Although we made simplifying assumptions—( losses as lumped values and steady-state flight) —the model stayed within a 5–6% of official industry figures. Even with transient effects, fuel savings remain about \$26000 annually. It has yet to account for complex stage aerodynamics, and natural wear due to engine aging.

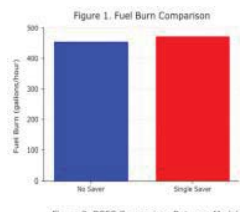
**Core Findings:**

**Architectural Edge:** Sharing power between two spools significantly optimizes thermal cycles.

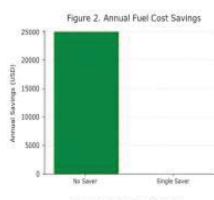
**Sensitivity Drivers:** Engineers should focus primarily on compressor health and minimizing bleed-air extraction to maximize efficiency, .

**Operational Fit:** These benefits are seen prominently in regional, high-cycle routes where profit margins vary with fuel prices.

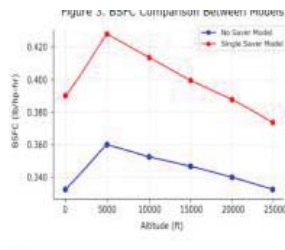
Future work will incorporate stage-specific loss and. Hybrid-electric configurations or geared-turbofan innovations. These could be the shift toward sustainable, "green" aviation.



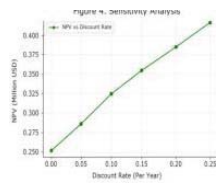
**Fig. 1.** Fuel burn comparison between single spool and two spool configurations, indicating reduced fuel consumption with the modified system.



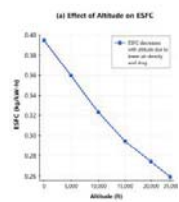
**Fig. 2.** Annual fuel cost savings achieved using the two spool configuration relative to the single spool case.



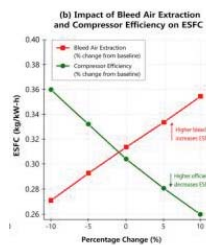
**Fig. 3.** Variation of brake specific fuel consumption (BSFC) with altitude for single spool and two spool models, showing improved efficiency of the two spool configuration.



**Fig. 4.** Sensitivity of net present value (NPV) to discount rate, illustrating the impact of financial assumptions on project viability.



**Fig. 5a.** Impact of altitude on specific fuel consumption (ESFC), showing a decreasing trend with increasing altitude.



**Fig. 5b.** Effect of Bleed Air extraction and compressor efficiency on ESFC reduction, indicating higher fuel usage with increased bleed demand.



Figure 6a: A typical small two spool aeroengine

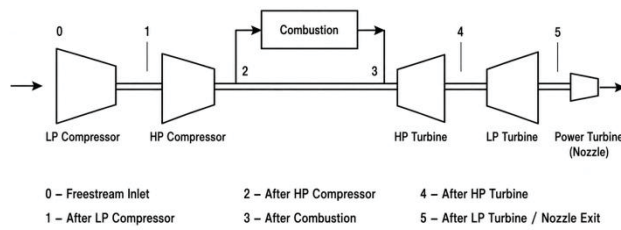


Figure 6b: Schematic showing thermo-mechanical linkages

### Nomenclature

- PLP** – Low-pressure spool power (W)
- PHP** – High-pressure spool power (W)
- Ptp** – Power turbine output (W)
- Pacc** – Accessory power extraction (W)
- ma** – Mass flow rate of air (kg/s)
- mbl** – Mass flow rate of bleed air (kg/s)
- Cpa** – Specific heat capacity of air at constant pressure (J/kg·K)
- Cpg** – Specific heat capacity of combustion gases at constant pressure (J/kg·K)
- T01, T02, ..., T07** – Total (stagnation) temperatures at various engine stations (K)
- $\eta_{m,LP}$**  – Mechanical efficiency of LP spool
- $\eta_{m,HP}$**  – Mechanical efficiency of HP spool
- $\eta_{m,PT}$**  – Mechanical efficiency of power turbine
- $\Delta$  – Difference in value
- $\delta/$  – derivative

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